

Testing CPT symmetry in ortho-positronium decays with the J-PET detector

July 8th 2022

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on behalf of the J-PET Collaboration
Jagiellonian University



Motivation: discrete symmetry tests with o-Ps \rightarrow 3γ decays

- Discrete symmetries are scarcely tested with leptonic systems
- Prominent results from neutrinos oscillation experiments
 - Dirac phase, $\delta_{CP} \sim 3\sigma$ level [T2K, *Nature* 580 (2020) 339]
- Electron EDM $< 1.1 \times 10^{-29}$ [ACME, *Nature* 562 (2018) 355]
- Positronium – the lightest purely leptonic bound state, the only system consisting of charged leptons used for tests of CP and CPT to date

How can we test discrete symmetries in the positronium system?

- Searches for **prohibited positronium annihilations**
- SME-based searches for CPT violation proposed with **positronium spectroscopy** [Phys. Rev. D92 (2015) 056002]

• Searches for non-vanishing symmetry-odd correlations

$$C_{CP} = (1.3 \pm 2.1 \pm 0.6) \times 10^{-3}$$

PRL 104 (2010) 083401

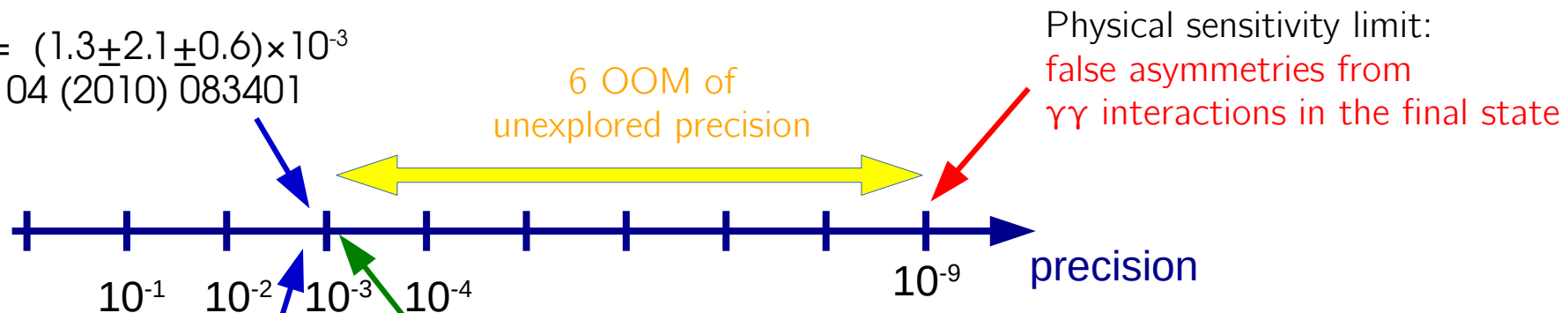
$$C_{CPT} = (2.6 \pm 3.1) \times 10^{-3}$$

PRL. 91 (2003) 263401



$$C_{CPT} = (6.7 \pm 9.5) \times 10^{-4}$$

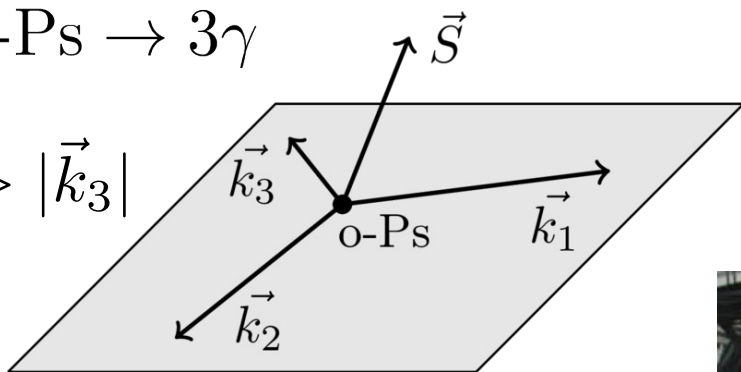
Nat. Commun. (2021) 12:5658



Testing discrete symmetries with angular correlations in o-Ps $\rightarrow 3\gamma$ decays

$$e^+e^- \rightarrow \text{o-Ps} \rightarrow 3\gamma$$

$$|\vec{k}_1| > |\vec{k}_2| > |\vec{k}_3|$$



$$\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2) \quad \text{T \& CPT-violation sensitive}$$

$$\vec{S} \cdot \vec{k}_1 \quad \text{CP-violation sensitive}$$

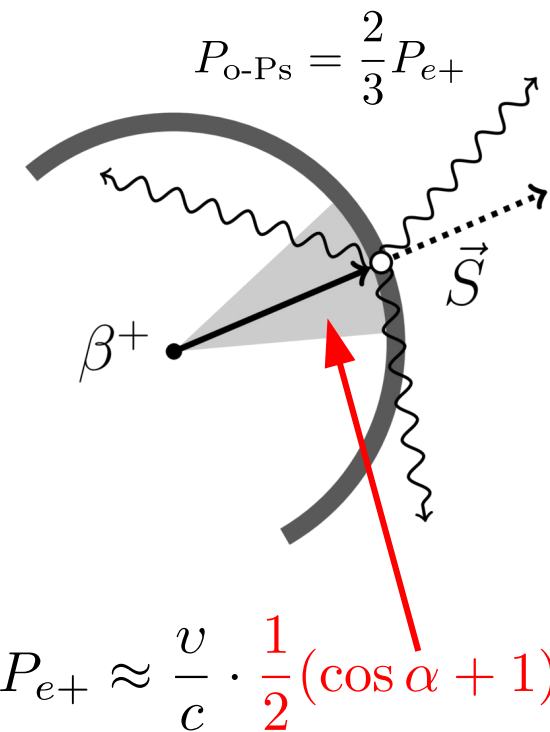
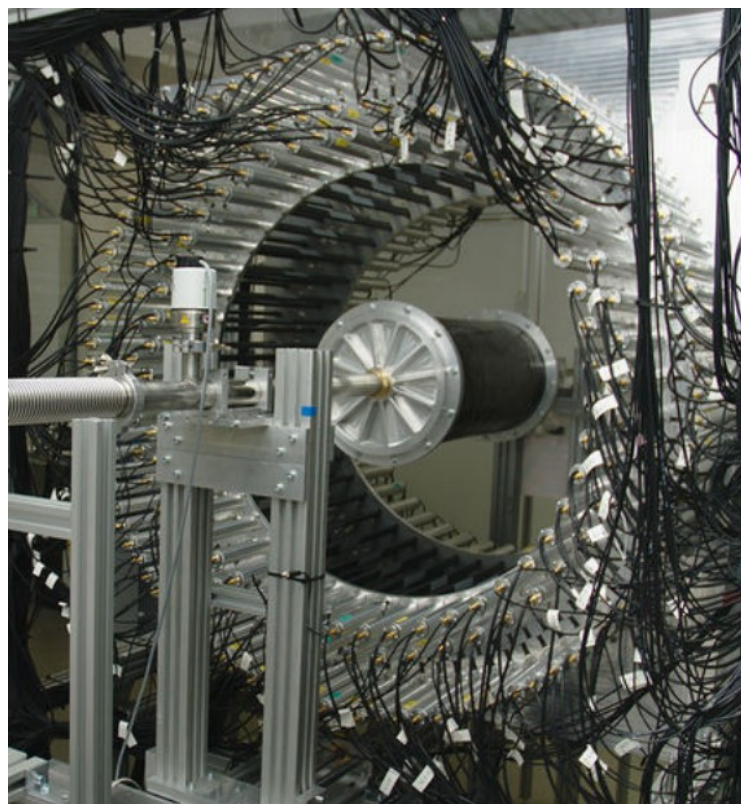
$$\langle \hat{O} \rangle \stackrel{?}{=} 0 \quad \text{for an odd operator}$$

$$\Leftrightarrow \text{CPT}(\hat{O}) = -1$$

$$\Leftrightarrow \mathcal{T}(\hat{O}) = -1$$

Event-by-event spin estimation

Using an extensive-size o-Ps production and annihilation medium

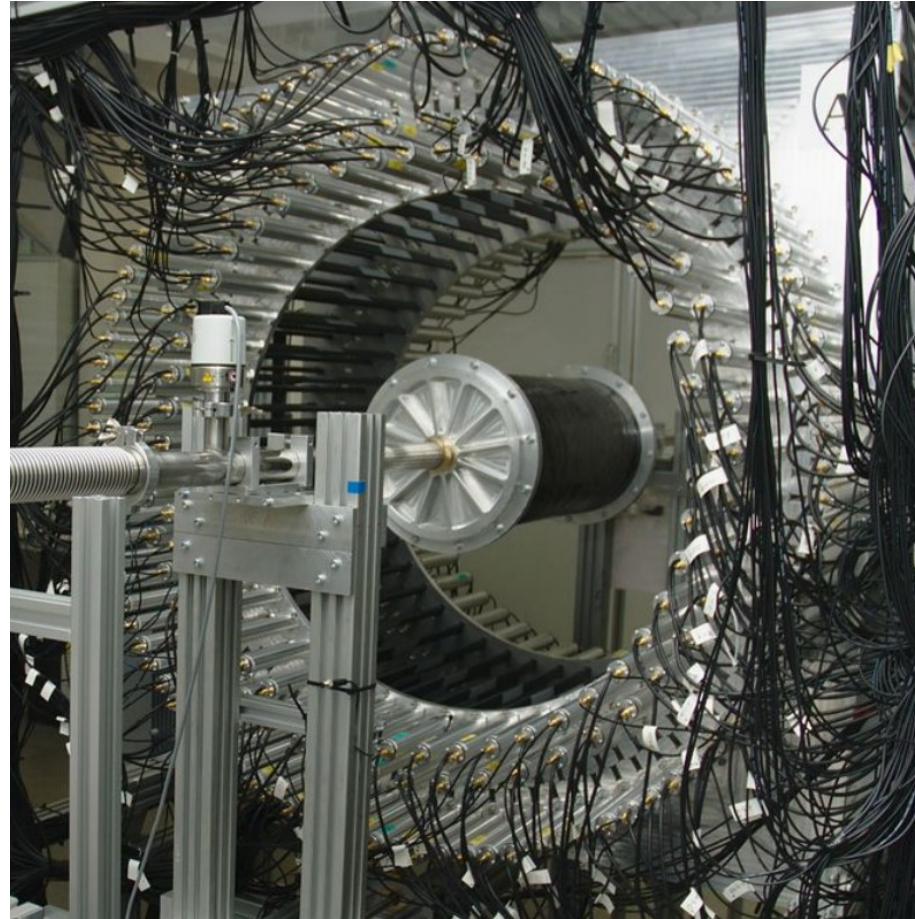
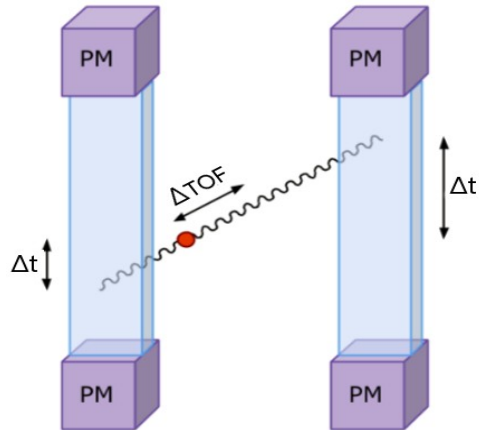


[W. Bernreuther *et al.*, *Z. Phys.* C41 (1988) 143]

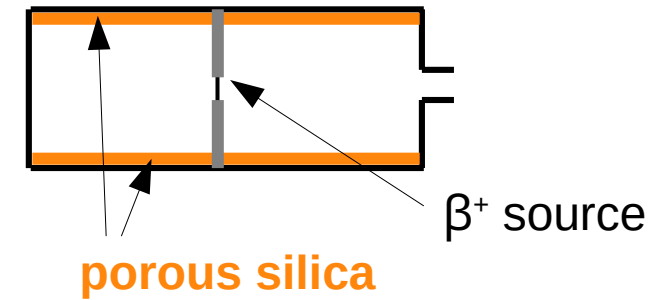
[P. Moskal *et al.*, *Acta Phys. Polon.* B47 (2016) 509]

The J-PET detector and ortho-positronium production

- Conceived as the 1st Positron Emission Tomograph based on plastic scintillators
- At the same time a robust photon detector for fundamental research!
- 192 scintillator strips (50 cm long) arranged in 3 concentric layers



- Extensive-size chamber, $R=12$ cm
- Walls coated with porous silica material enhancing o-Ps formation
- 10 MBq β^+ emitter (^{22}Na) placed in the center of the chamber



See yesterday's talk by Shivani in *Technology and Industrial Applications*

[J-PET: NIM A 764 (2014) 317-321]
[J-PET: NIM A 764 (2014) 186-192]
[J-PET: NIM A 786 (2015) 105-112]
[J-PET: NIM A 775 (2015) 54-62]

J-PET vs previous measurements

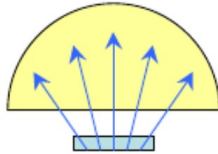
Gammasphere

PRL. 91 (2003) 263401

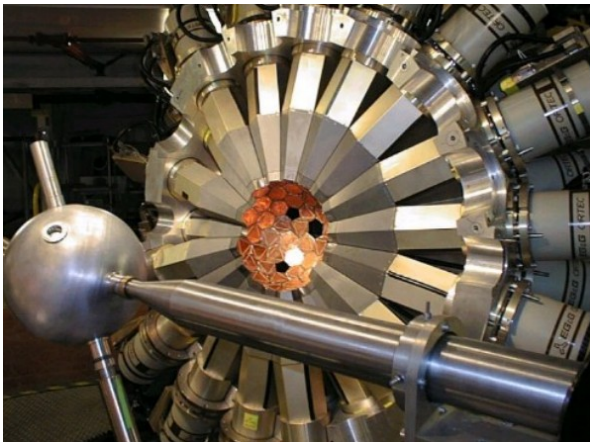
$$C_{\text{CPT}} = (2.6 \pm 3.1) \times 10^{-3}$$

$$\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2)$$

$$P_{e^+} = \frac{v}{c} \cdot 0.686$$



- Limiting e+ emission direction
- 1 Mbq β^+ emitter activity
- 4π detector but low angular resolution

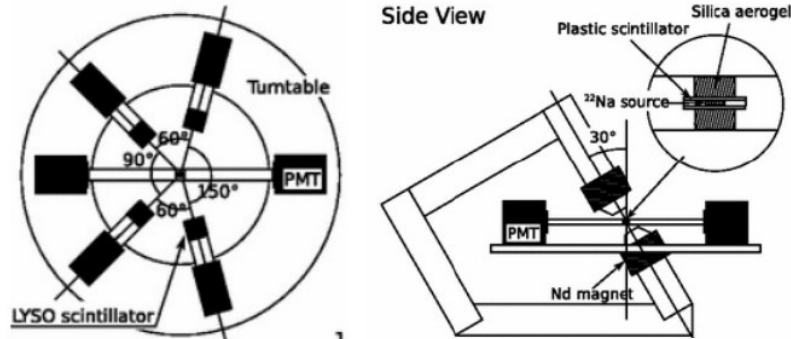


Yamazaki et al.

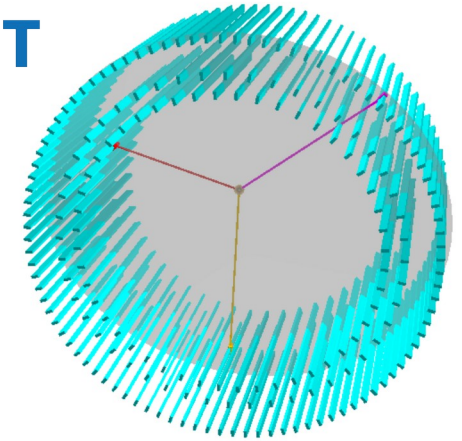
PRL 104 (2010) 083401

$$C_{\text{CP}} = (1.3 \pm 2.1 \pm 0.6) \times 10^{-3}$$

$$(\vec{S} \cdot \vec{k}_1)(\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2))$$



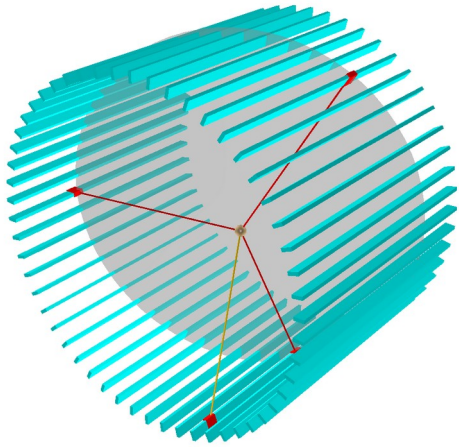
- Polarized o-Ps using external B field
- Inclusive measurement
- Only certain angular configurations



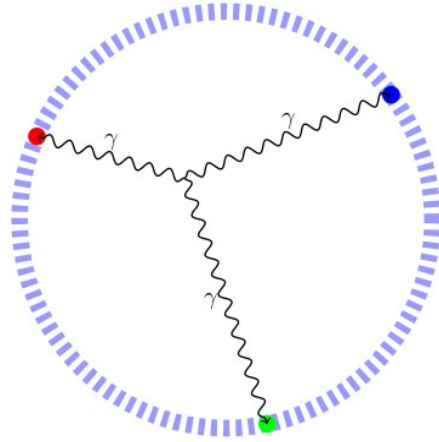
- Recording multiple geometrical configurations
- e+ spin estimated event-by-event

$$P_{e^+} \approx \frac{v}{c} \cdot 0.91$$
- Plastic scintillators = fast timing \rightarrow using high β^+ emitter activity (tested up to 10 Mbq)
- Recording all 3 annihilation photons
- Angular resolution at 1° level

Reconstruction of $o\text{-Ps} \rightarrow 3\gamma$ decays in J-PET

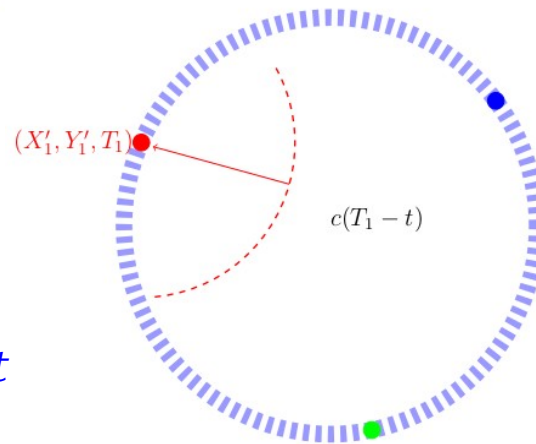


1. Find the decay plane containing the 3 hits in the J-PET barrel



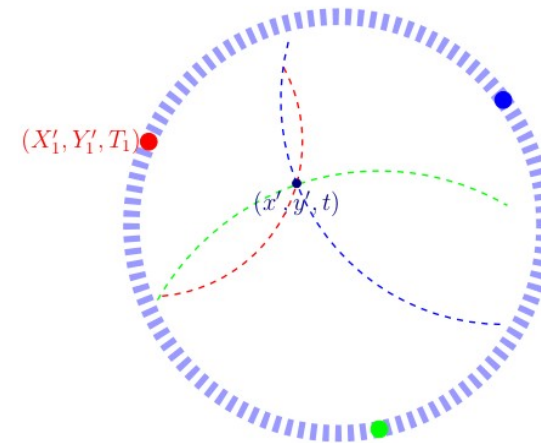
2. Transform the hit coordinates to a 2D coordinate system in the decay plane
 $(X_i, Y_i, Z_i, T_i) \rightarrow (X'_i, Y'_i, 0, T_i)$

3. For each of the recorded γ hits, define a circle of possible origin points of the incident γ assuming $o\text{-Ps}$ decay at time t



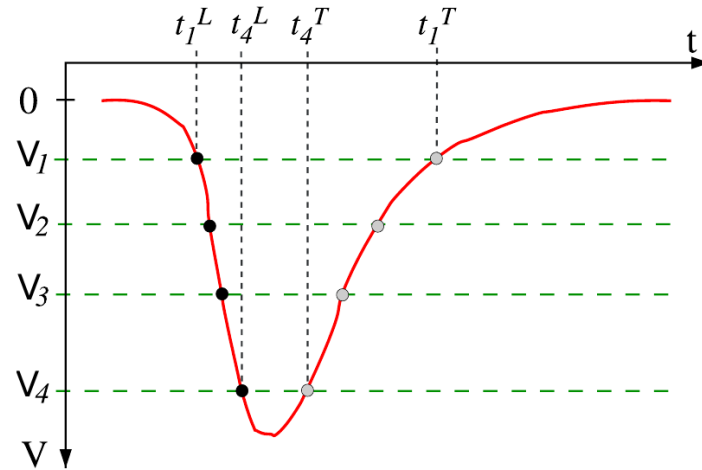
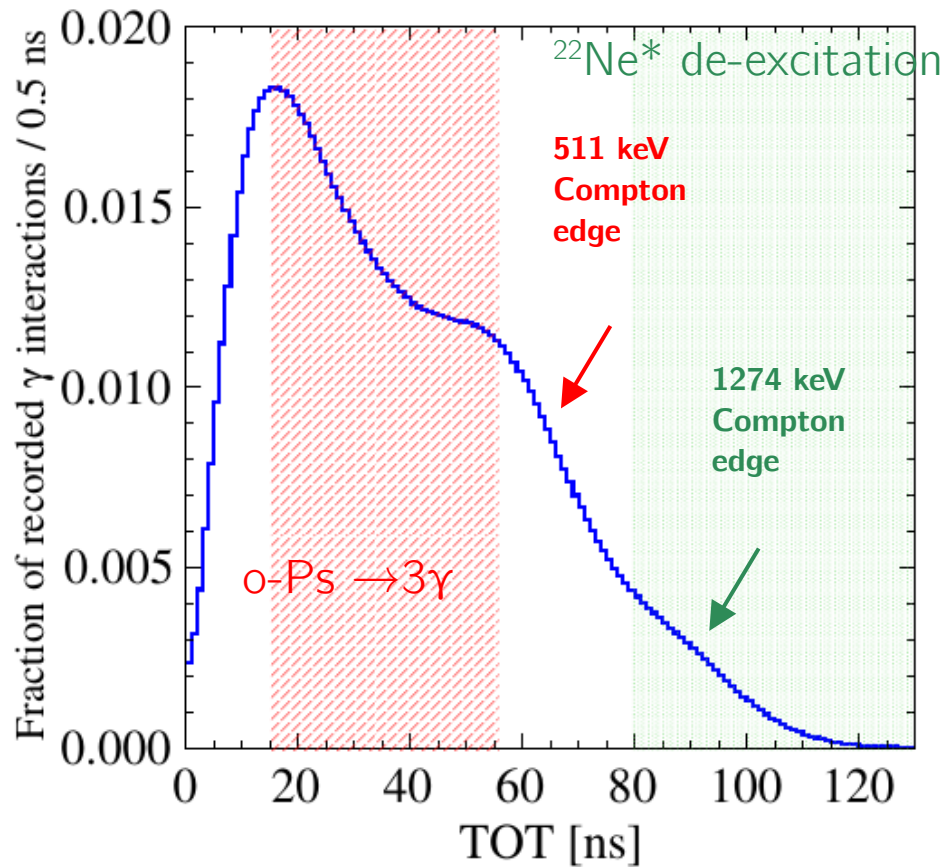
4. The decay point (x', y') in the decay plane and time t is an intersection of 3 such circles:

$$(T_i - t)^2 c^2 = (X'_i - x')^2 + (Y'_i - y')^2, \quad i = 1, 2, 3$$

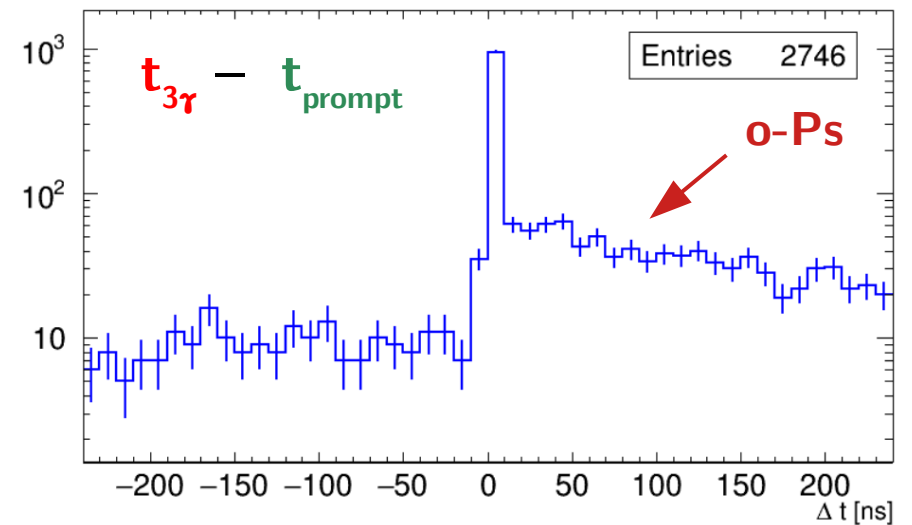


Identification of o-Ps $\rightarrow 3\gamma$ events in J-PET

Using total Time Over Threshold (TOT) of PMT signals from a scintillator strip \rightarrow a measure of γ deposited energy



Confirming o-Ps presence with positron lifetime distribution

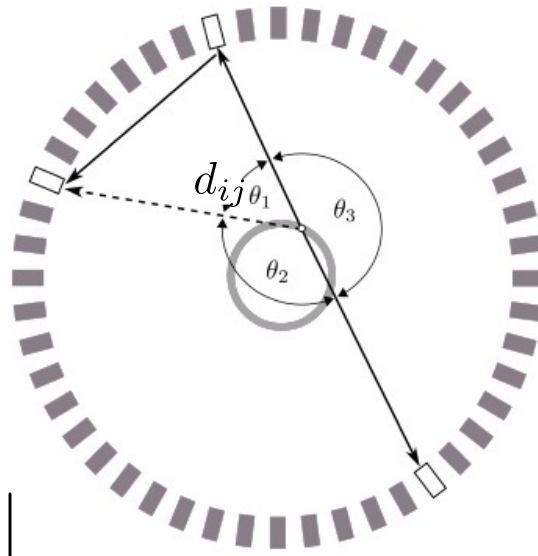


Treatment of main background sources

Secondary Compton scatterings

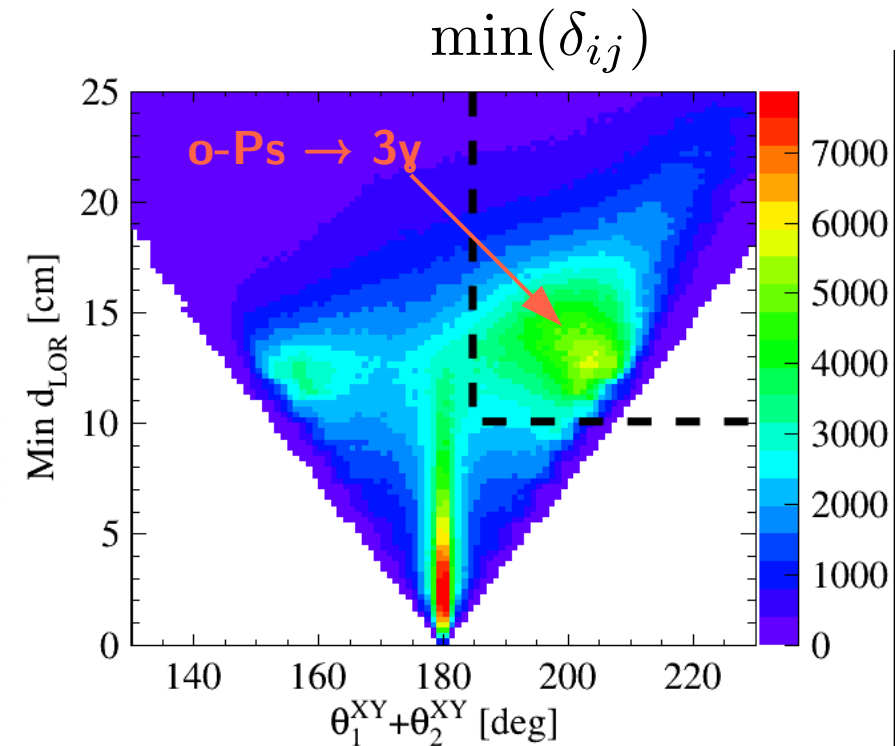
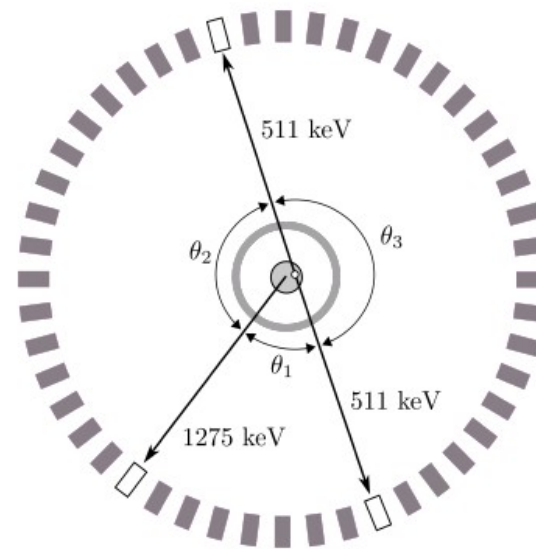
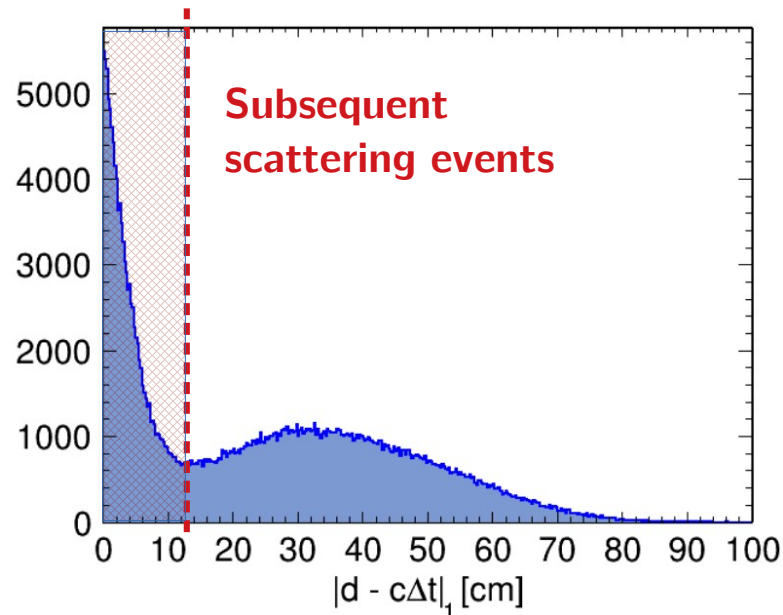
- Secondary Compton-scattered photons may be recorded by J-PET again
- For each pair of annihilation photon candidates i and j ($i,j=1,2,3$) we compute:

$$\delta t_{ij} = |d_{ij} - c\Delta t_{ij}|$$



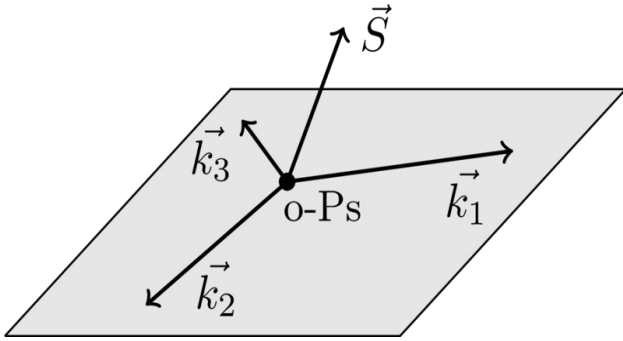
2γ from the β+ source setup

- Using angular topology of the event in XY detector plane
- Considering all hypothetical back-to-back 2γ pairs (tomographic “Lines Of Response”)



Evaluation of the CPT-asymmetric observable

$$\hat{S} \cdot (\vec{k}_1 \times \vec{k}_2) / |\vec{k}_1 \times \vec{k}_2| = \cos\theta$$



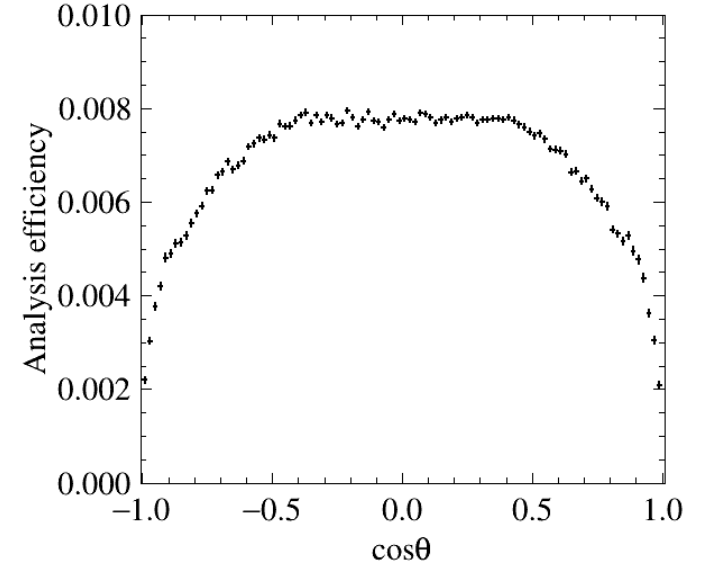
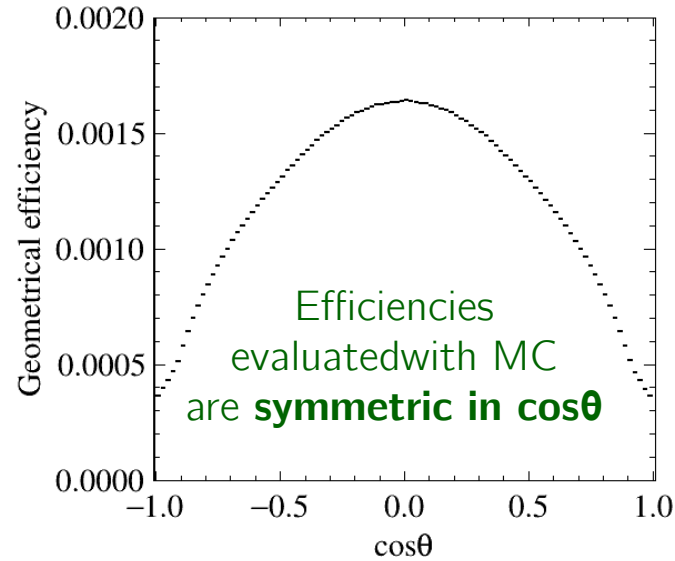
Standard asymmetry:

$$A = \frac{N_+ - N_-}{N_+ + N_-} \quad N_+ \Leftrightarrow \cos\theta > 0$$

is generalized by the **mean value of $\cos\theta$** :

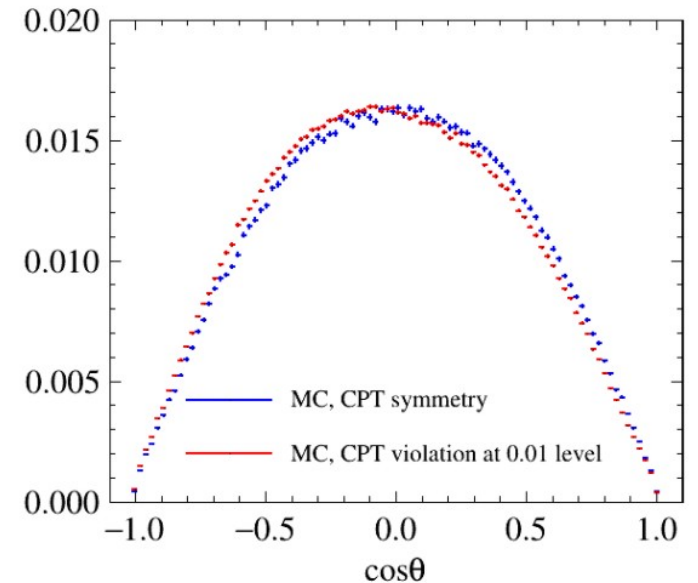
$$\frac{\int N(\cos\theta) \cos\theta}{\int N(\cos\theta)}$$

J-PET is sensitive to the full range of the operator



Expected effect with CPT-asymmetric simulations (exaggerated violation)

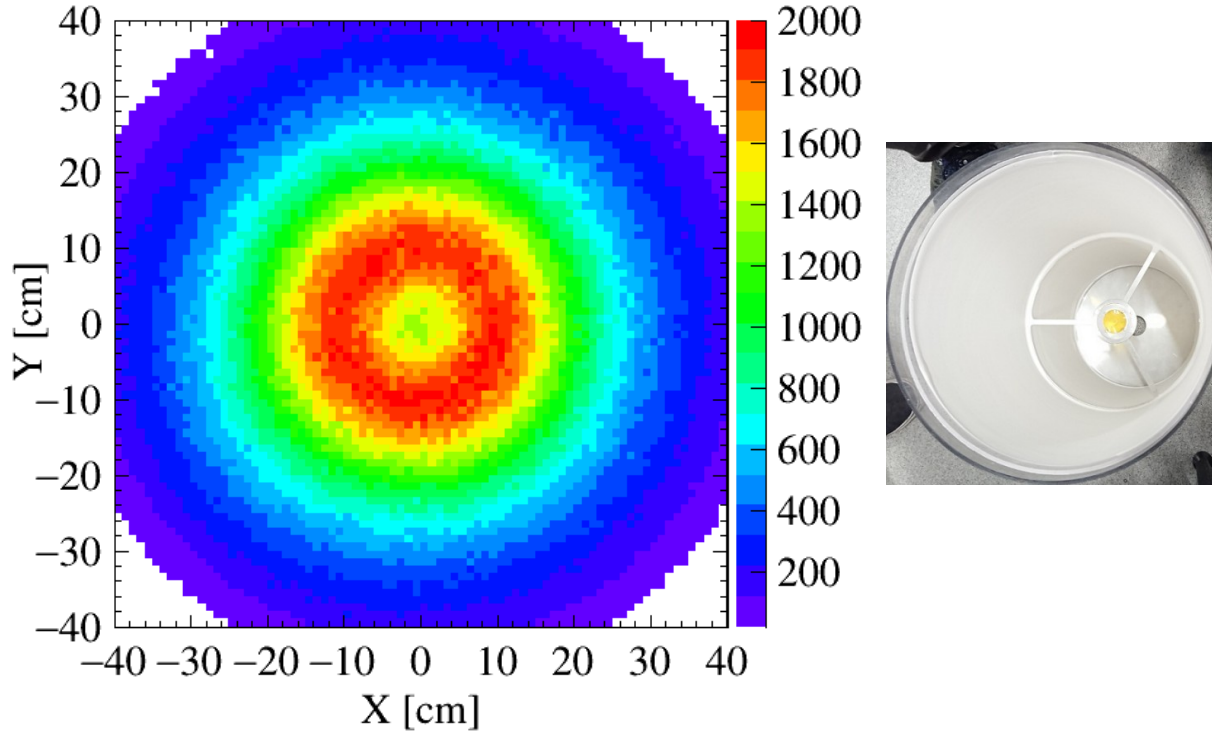
[Symmetry 12 (2020) 8, 1268]



Results of the 1st CPT test with J-PET

Using 2×10^6 of identified o-Ps \rightarrow 3γ annihilations

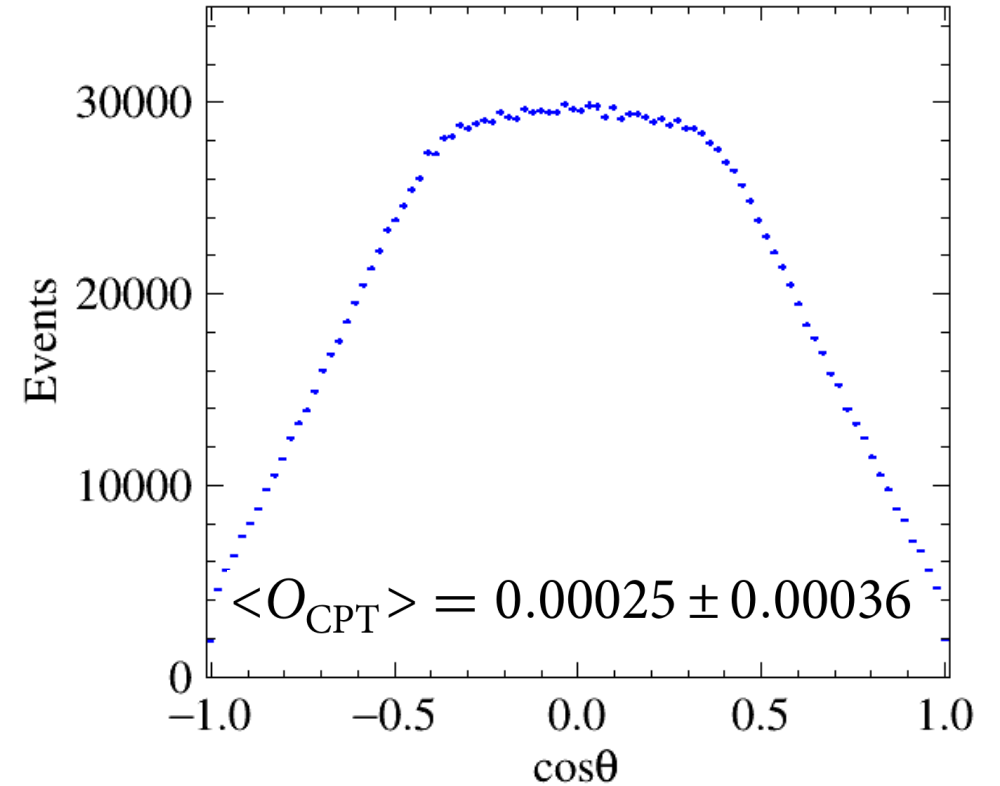
3γ image of the o-Ps production chamber in the transverse view of the detector



The first image of an extensive-size object obtained with o-Ps \rightarrow 3γ annihilations

Nature Commun. 12, 5658 (2021)

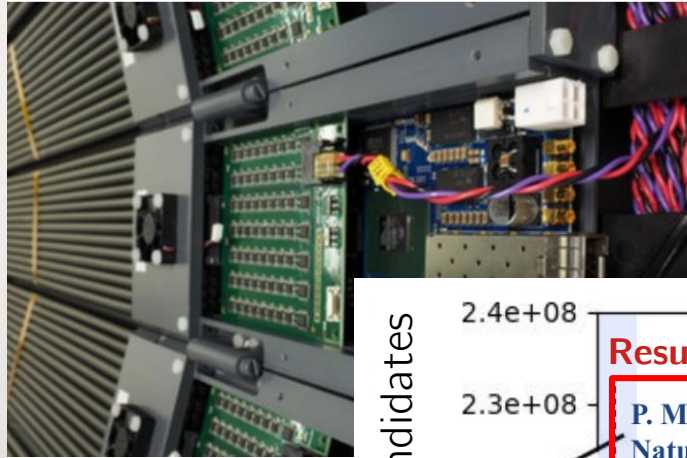
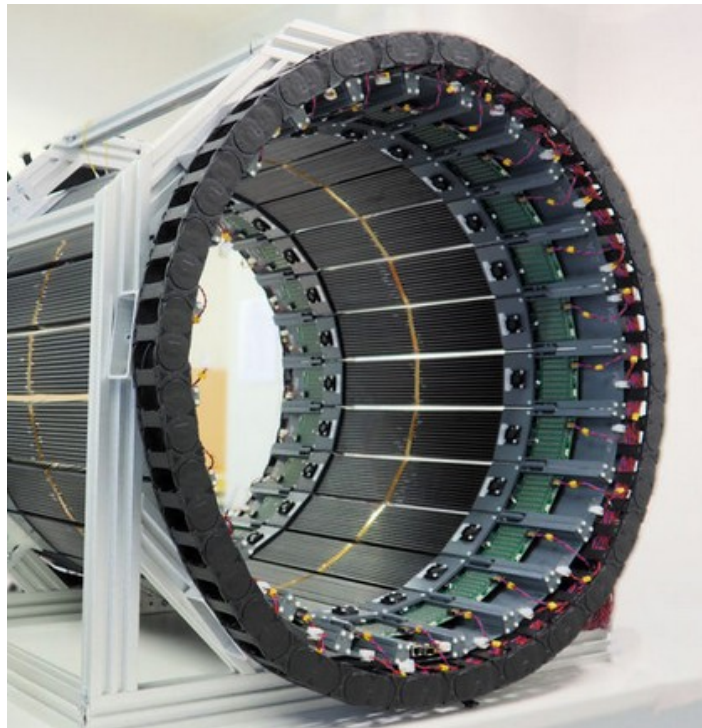
$$\hat{S} \cdot (\vec{k}_1 \times \vec{k}_2) / |\vec{k}_1 \times \vec{k}_2| = \cos\theta$$



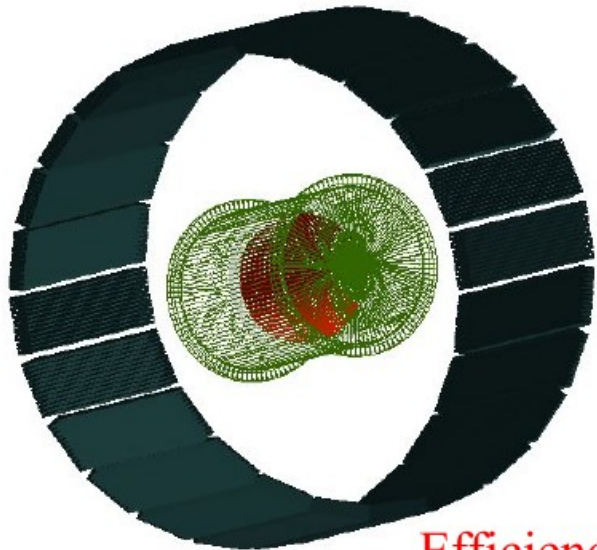
$$C_{\text{CPT}} = \langle O_{\text{CPT}} \rangle / P = 0.00067 \pm 0.00095$$

37.4% (polarization-dominated)

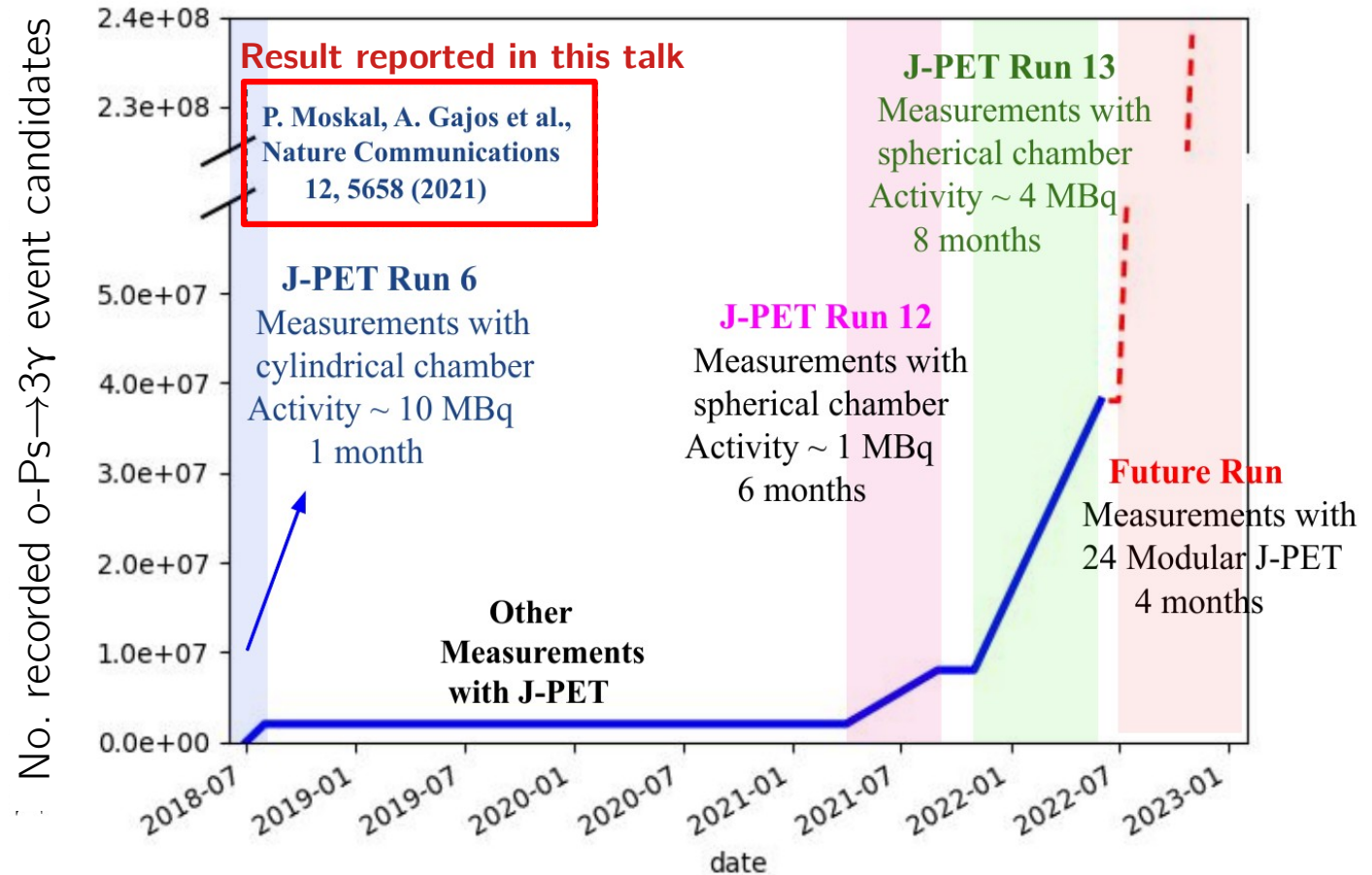
Towards the sensitivity of 10^{-5}



- New J-PET with dense geometry & digital SiPM readout
- Spherical annihilation chamber to enhance e^+ utilization



Efficiency ~ 11
w.r.t present J-PET



Summary and further perspectives

- The J-PET detector is capable of exclusive registration of $o\text{-Ps} \rightarrow 3\gamma$ annihilations
 - Full event reconstruction including determination of the annihilation point in an extensive-size medium
 - Estimation of $o\text{-Ps}$ spin on an event-by-event basis
 - The first image of an extensive-size object obtained solely with $o\text{-Ps}$ annihilations
- **Sub-permil precision of the CPT test reached with the first J-PET measurement**
- **J-PET aims at the sensitivity of the CP and CPT symmetry tests at the level of 10^{-5} with an improved positronium production and photon detection setup**

Thank you for your attention!

This work is supported in the framework
of the TEAM
POIR.04.04.00-00-4204/17
Programme of the Foundation for
Polish Science

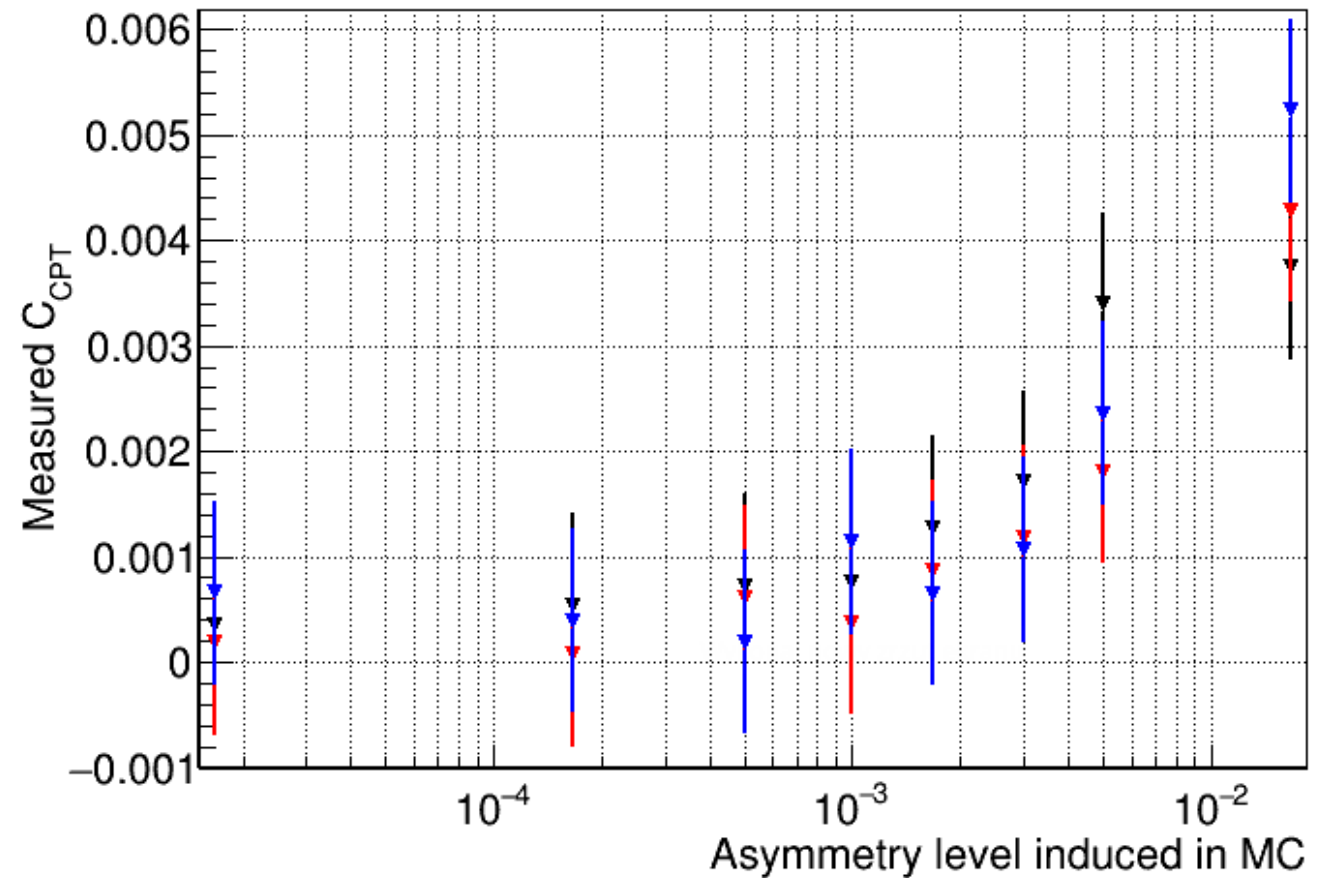


Backup Slides

Evaluation of the experiment's sensitivity

- MC-simulating same statistics as experimental data
 - Artificially inducing different levels of CPT violation
- Applying identical analysis as used on data
- Testing observed level of violation (C_{CPT})

Different colors denote independent simulations

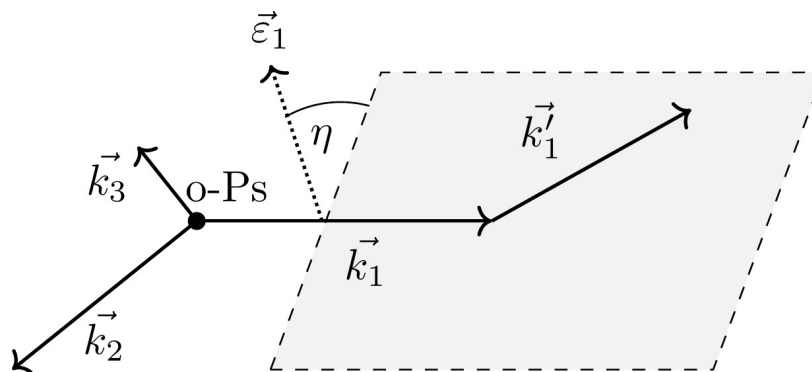
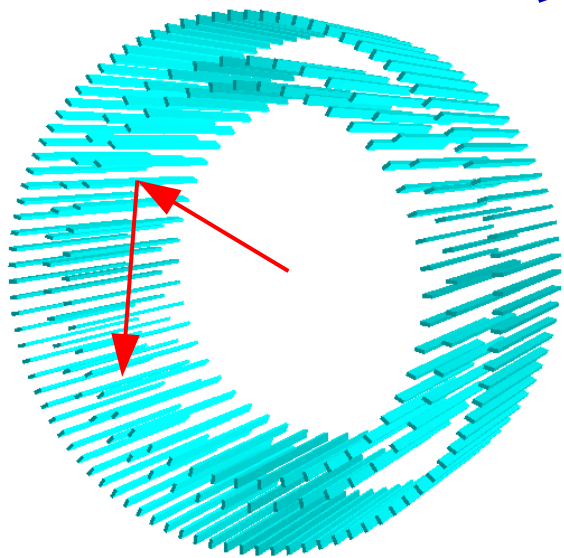


Testing discrete symmetries with ortho-positronium

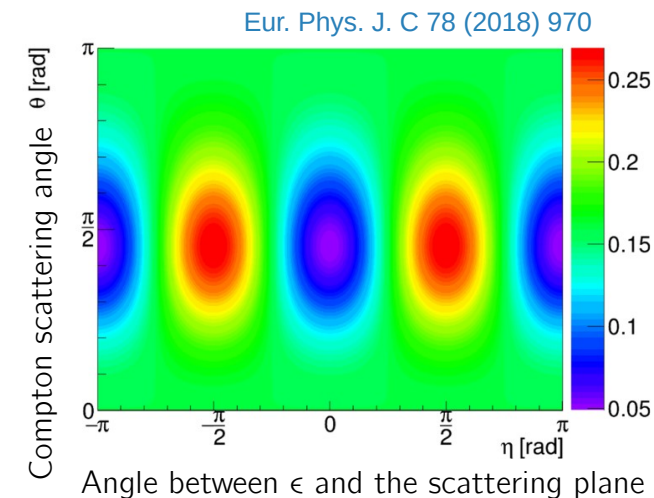
If polarization direction of the photons (ϵ) can be estimated, a new class of operators becomes available for measurement!

operator	C	P	T	CP	CPT
$\vec{S} \cdot \vec{k}_1$					
$\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2)$	+	-	+	-	-
$(\vec{S} \cdot \vec{k}_1)(\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2))$	+	+	-	+	-
$\vec{k}_2 \cdot \vec{\epsilon}_1$	+	-	-	-	+
$\vec{S} \cdot \vec{\epsilon}_1$	+	-	-	-	+
$\vec{S} \cdot (\vec{k}_2 \times \vec{\epsilon}_1)$	+	+	-	+	-
	+	-	+	-	-

[W. Bernreuther *et al.*, *Z. Phys. C*41 (1988) 143]
 [P. Moskal *et al.*, *Acta Phys. Polon. B*47 (2016) 509]



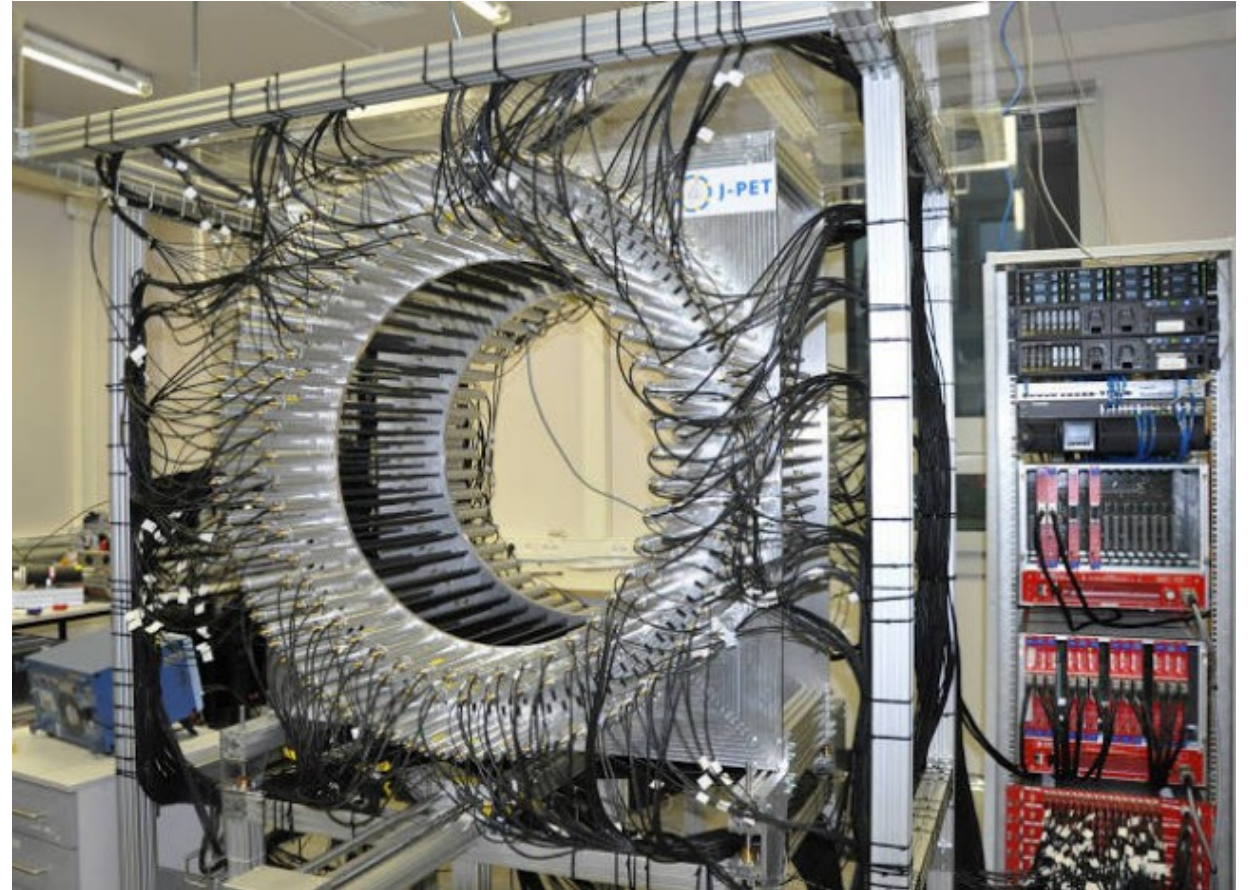
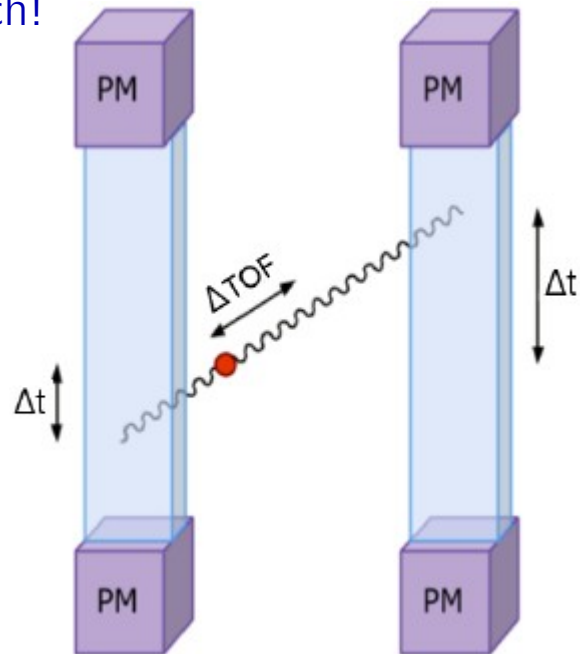
$$|\vec{k}_1| > |\vec{k}_2| > |\vec{k}_3|$$



J-PET can determine the scattering plane in events with secondary Compton scatterings!

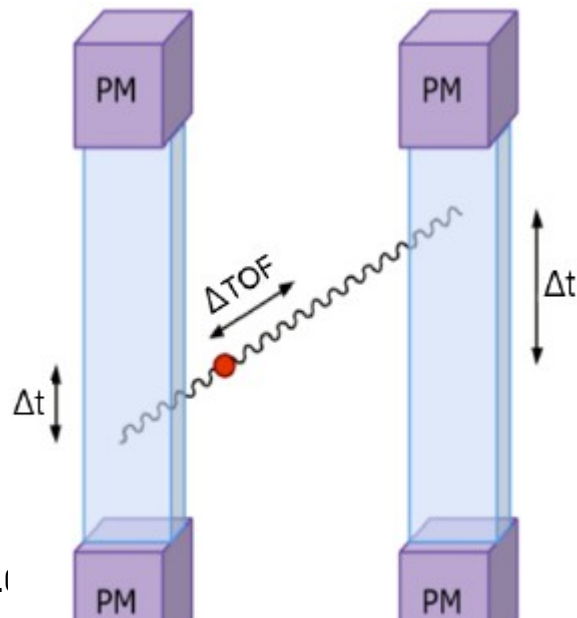
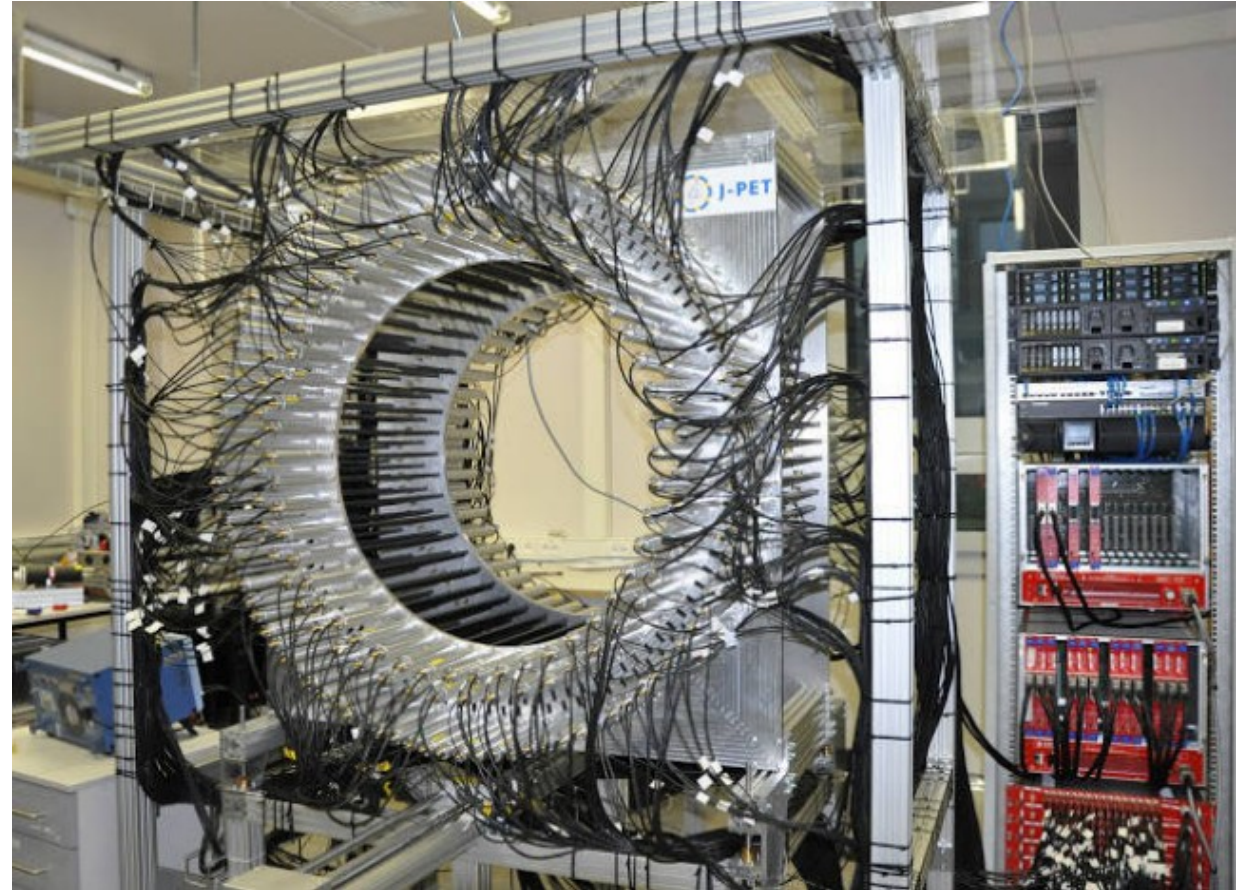
The J-PET Detector

- Constructed at the Jagiellonian University
- First PET device using strips of plastic scintillators
- At the same time: a robust photon detector for fundamental research!

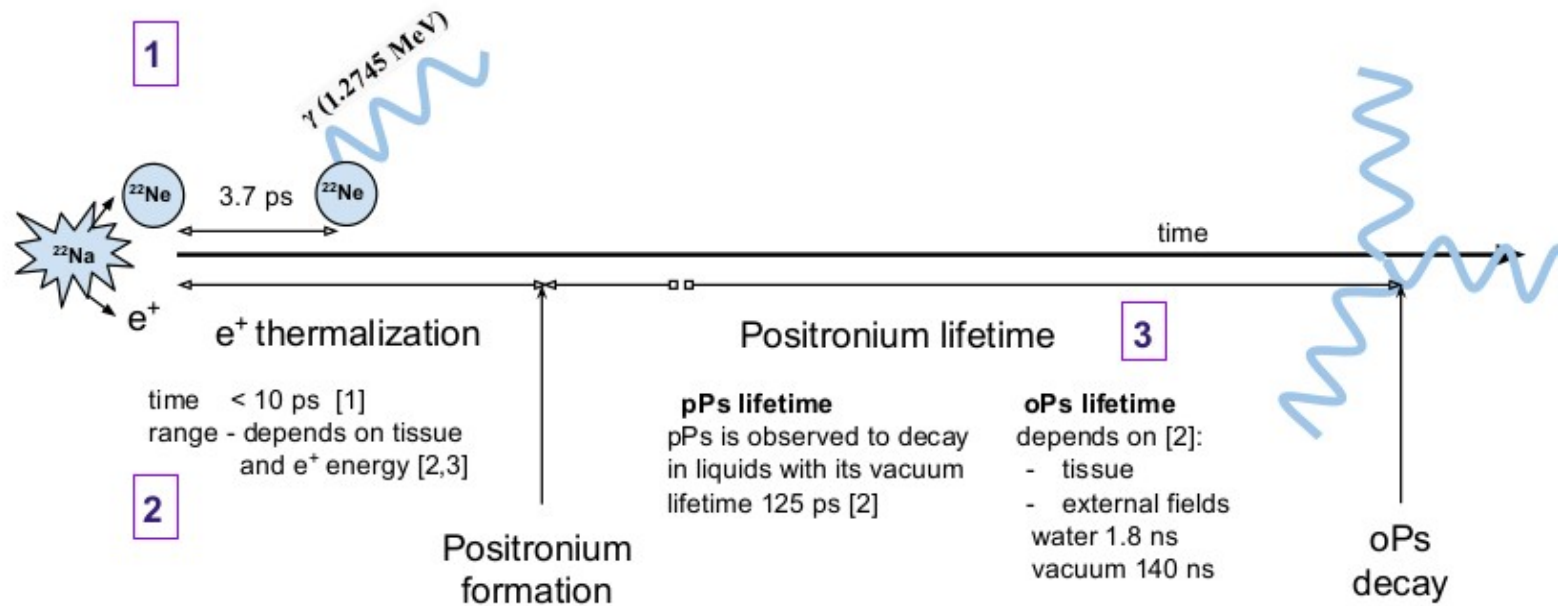


The J-PET Detector

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O-Ps creation and decay



[1] P. Kubica and A. T. Stewart, Phys. Rev. Lett. 34 (1975) 852

[2] M. Harpen Med.Phys. 31 (2004) 57-61

[3] J Cal-Gonzalez et al, Phys. Med. Biol. 58 (2013) 5127-5152

Distinguishing $o\text{-Ps} \rightarrow 3\gamma$ and $e^+e^- \rightarrow 2\gamma$

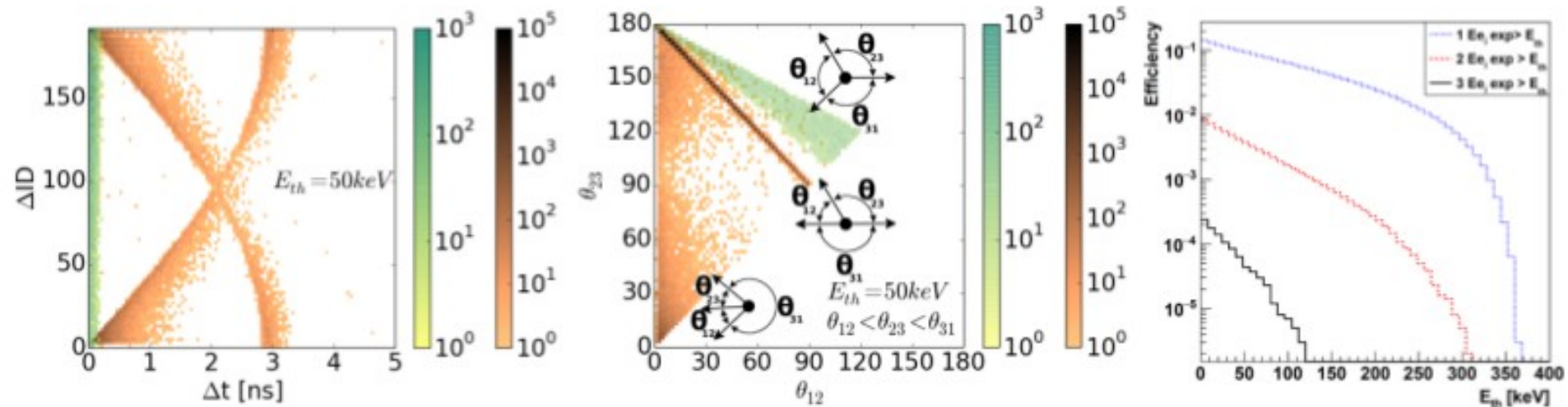
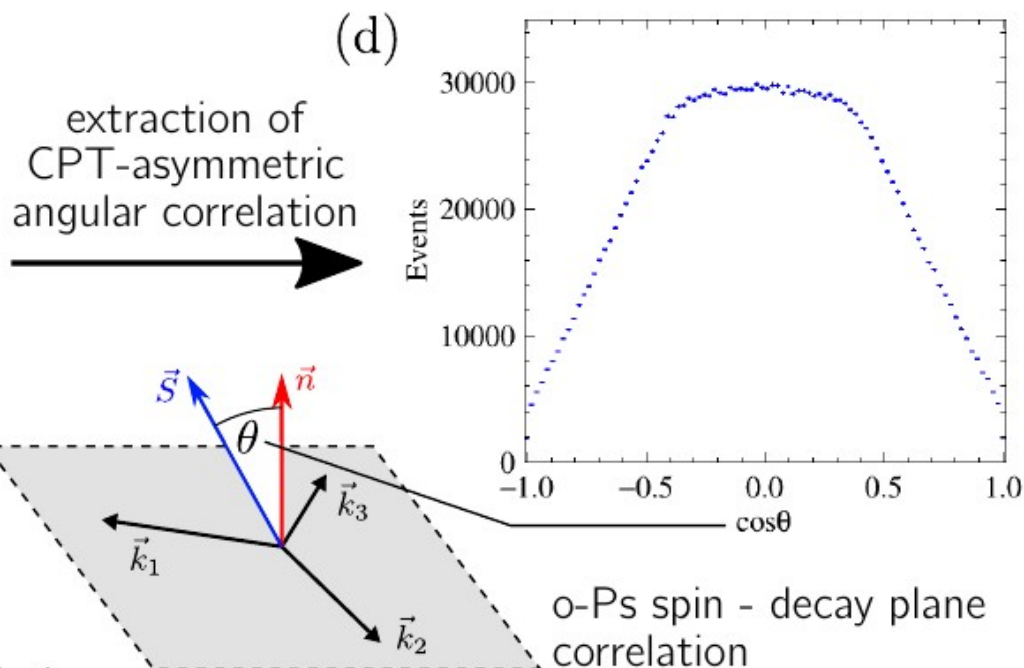
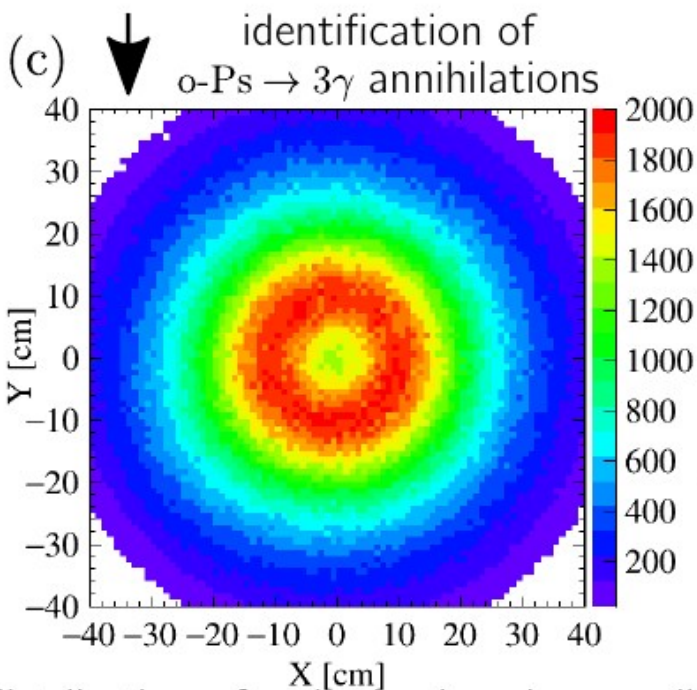
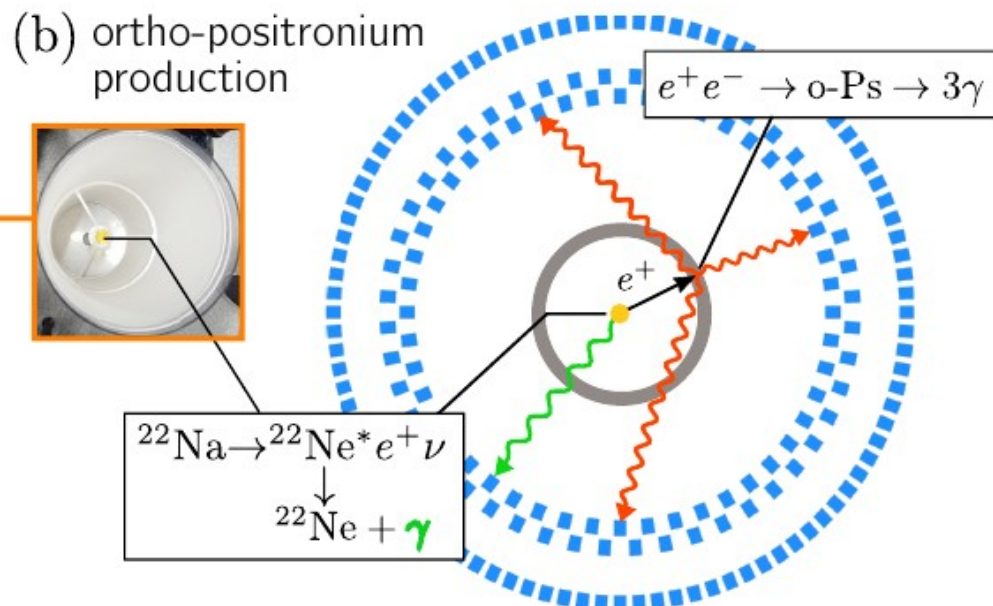
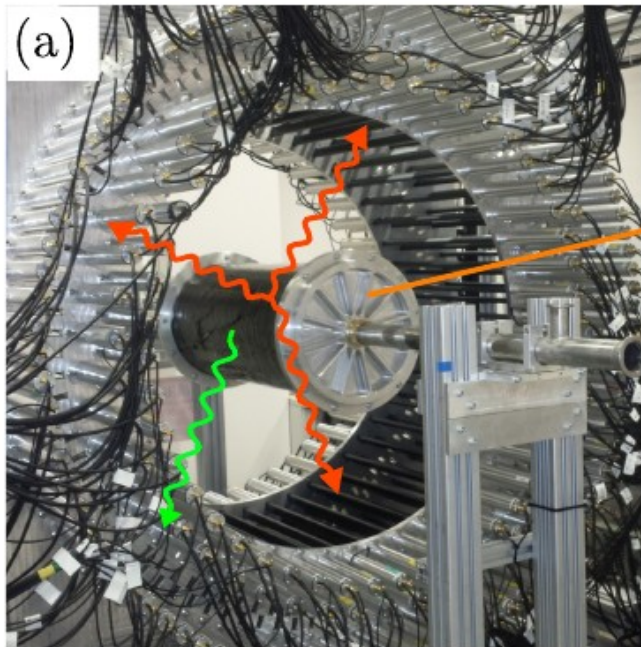
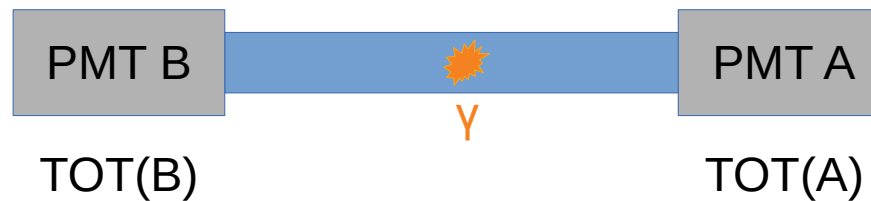


Figure 9. (Left) Simulated distributions of differences between detectors ID (ΔID) and differences of hit-times (Δt) for events with three hits registered from the annihilation $e^+e^- \rightarrow 2\gamma$ (gold colours) and $o\text{-Ps} \rightarrow 3\gamma$ (green colours). **(Middle)** Distribution of relative angles between reconstructed directions of gamma quanta. The numbering of quanta was assigned such that $\theta_{12} < \theta_{23} < \theta_{31}$. Shown distributions were obtained requiring three hits each with energy deposition larger than $E_{th} = 50 keV$. Gold colour scale shows results for simulations of $e^+e^- \rightarrow 2\gamma$ and green scale corresponds to $o\text{-Ps} \rightarrow 3\gamma$. Typical topology of $o\text{-Ps} \rightarrow 3\gamma$ and two kinds of background events is indicated. **(Right)** Detection efficiency of the J-PET detector for registration of one, two and three gamma quanta from $o\text{-Ps} \rightarrow 3\gamma$ decay. The efficiency is shown as a function of threshold energy applied in the analysis to each gamma quantum.

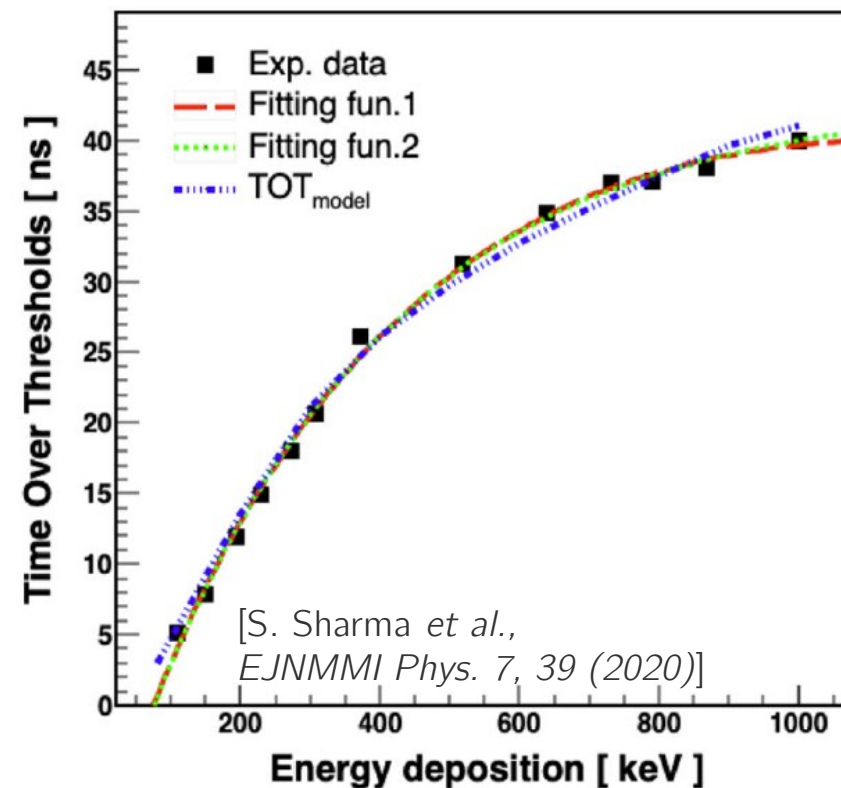
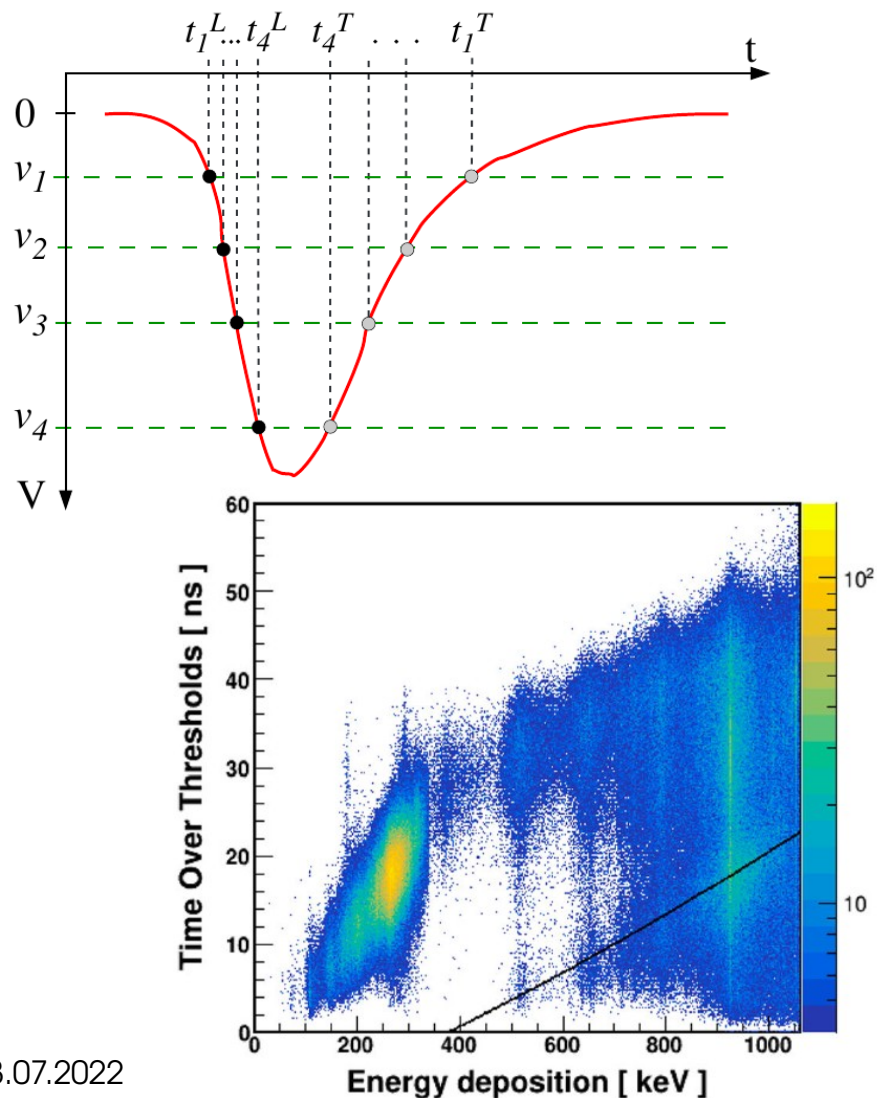


Time-Over-Threshold as a measure of deposited γ energy

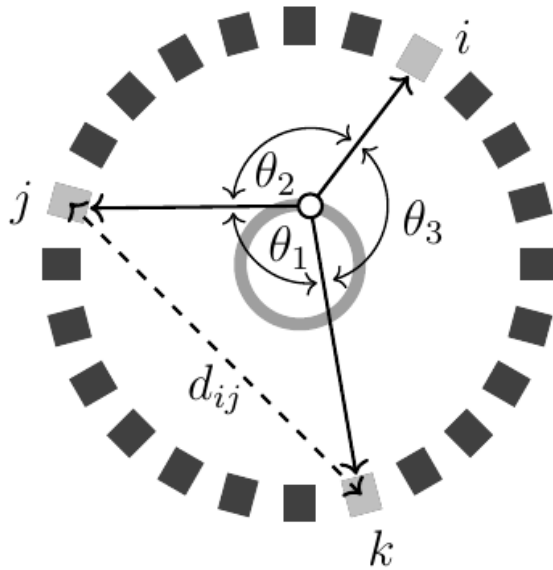
Using total Time Over Threshold (TOT) of PMT signals from a scintillator strip



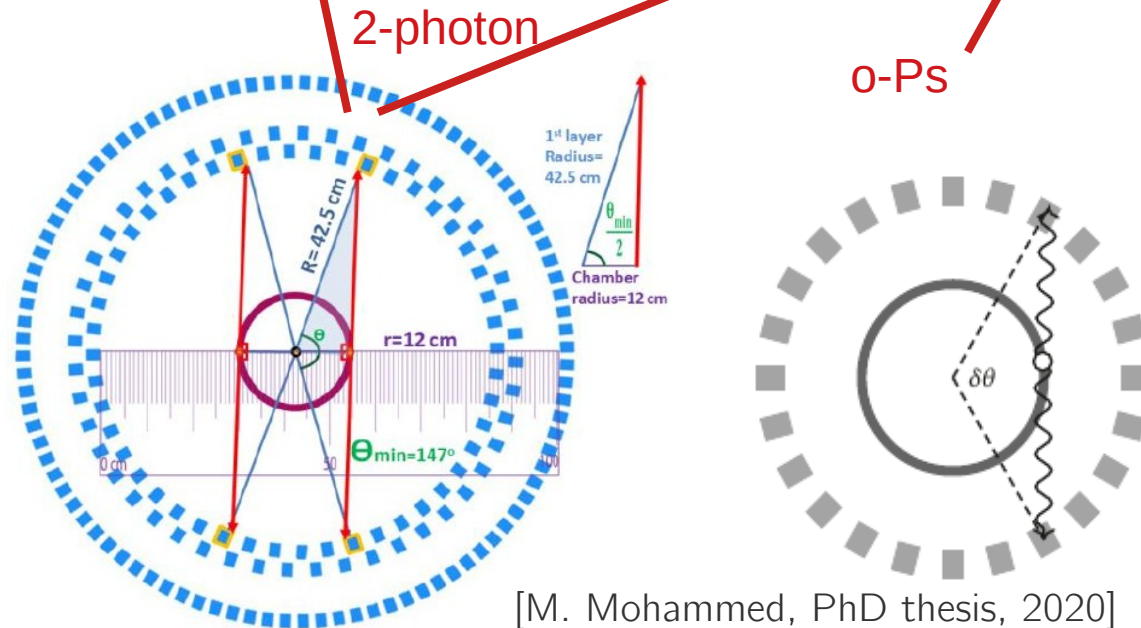
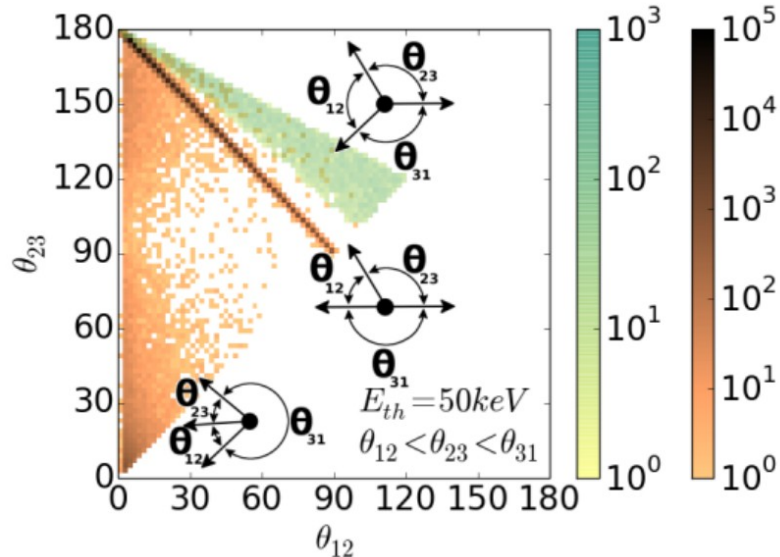
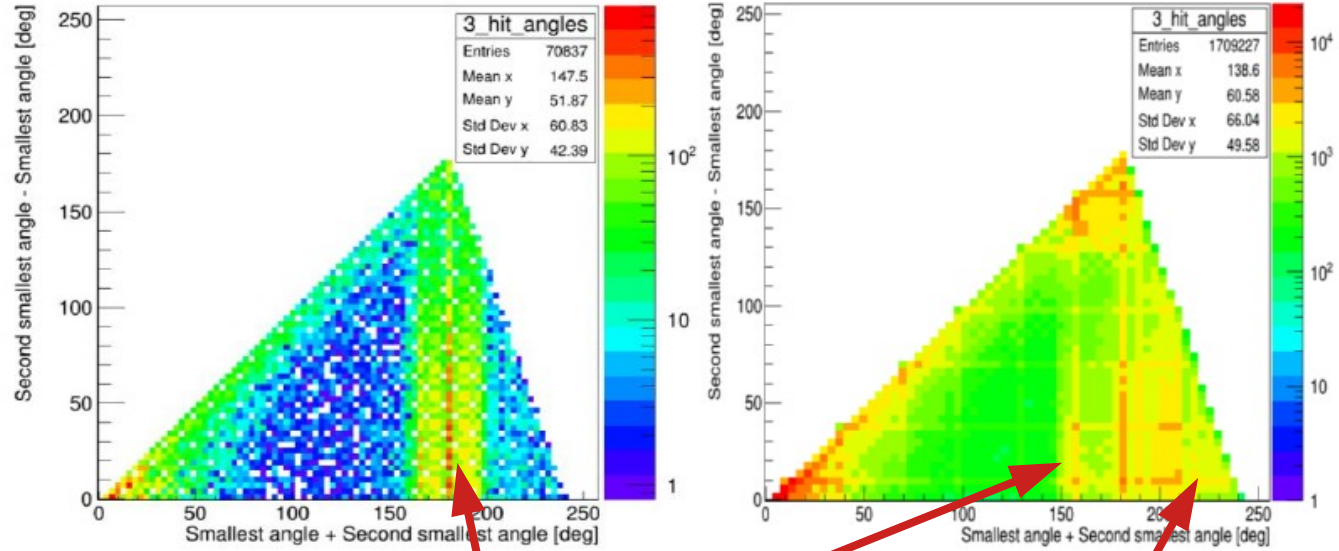
The relation between TOT and energy deposited by a photon in Compton scattering is under an extensive study right now.



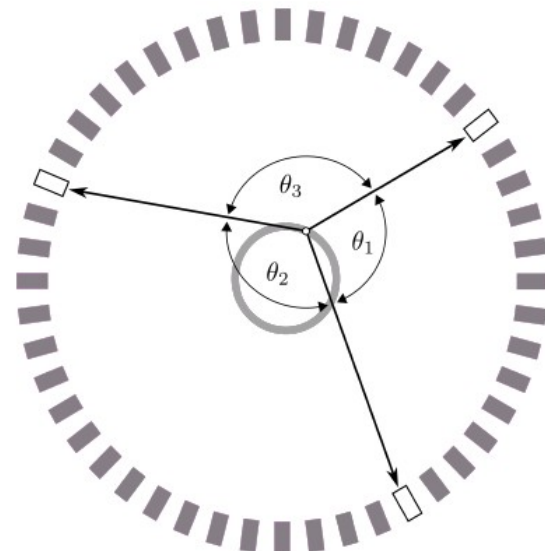
Angular topology of the 3γ events



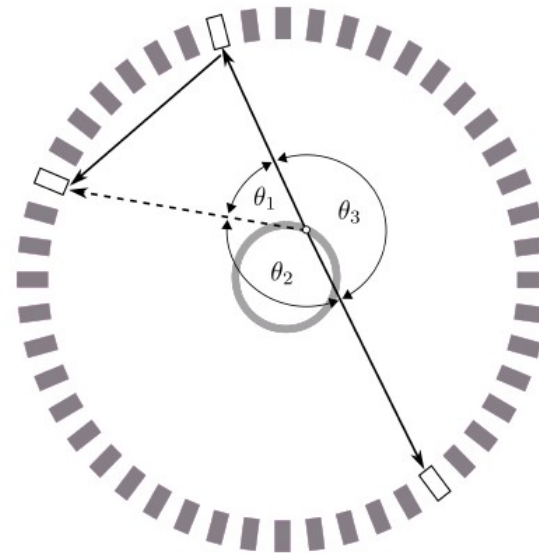
Angles defined in the transverse plane only



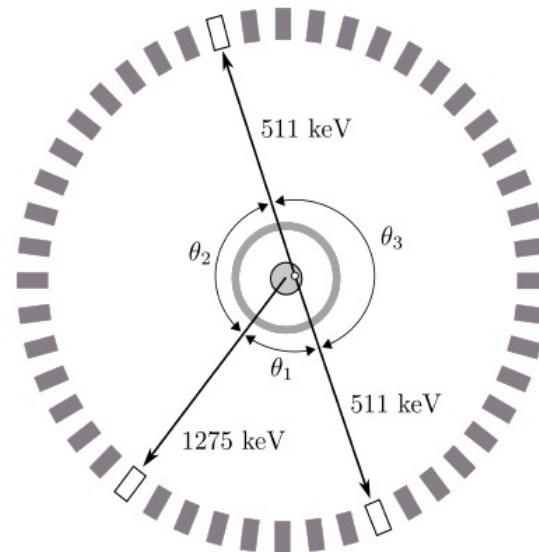
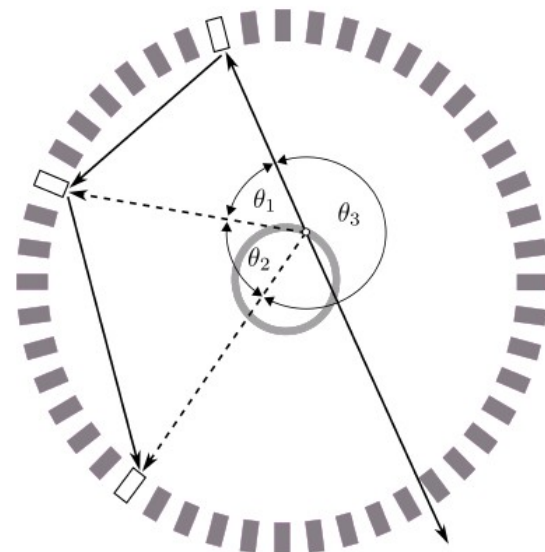
Signal & background events



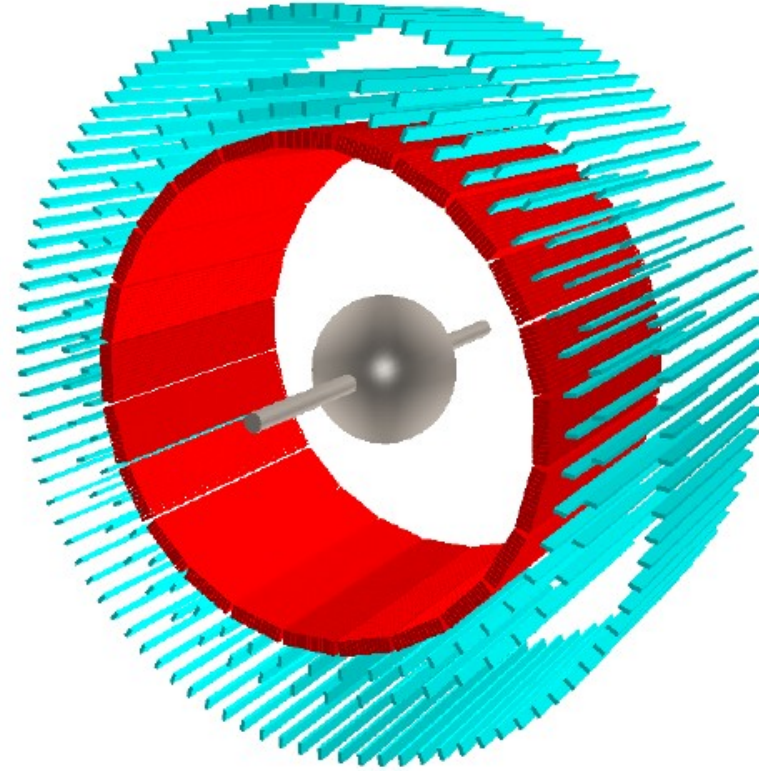
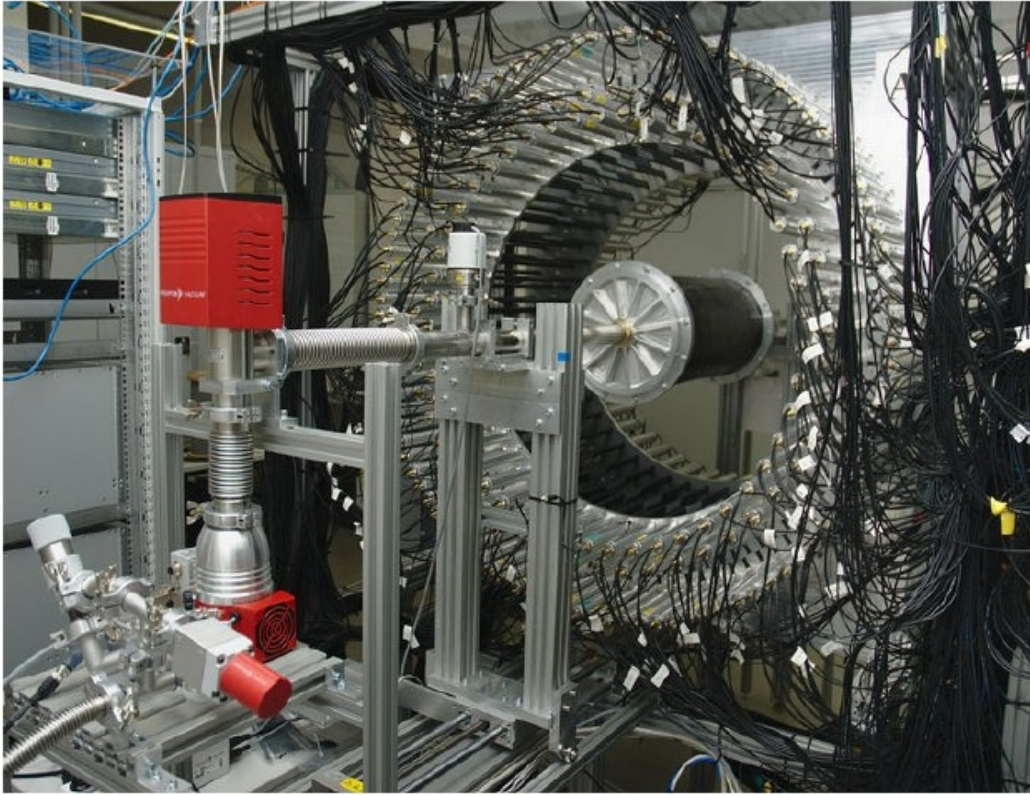
(a) Signal ($o\text{-Ps} \rightarrow 3\gamma$) event.



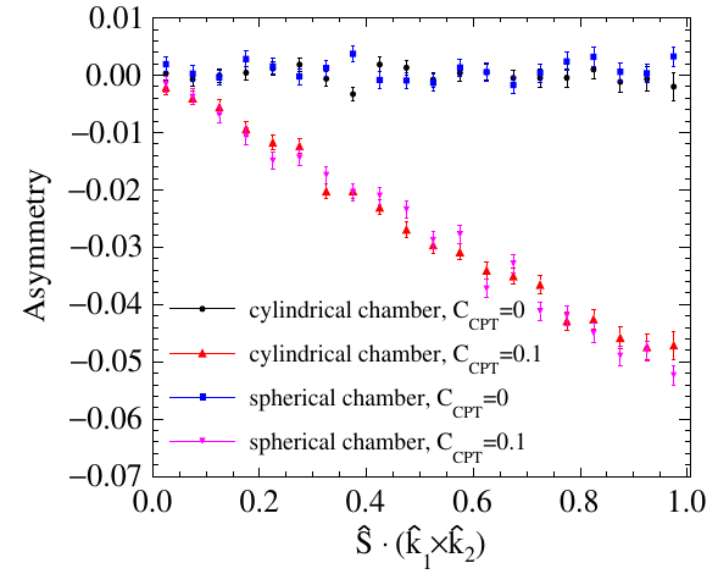
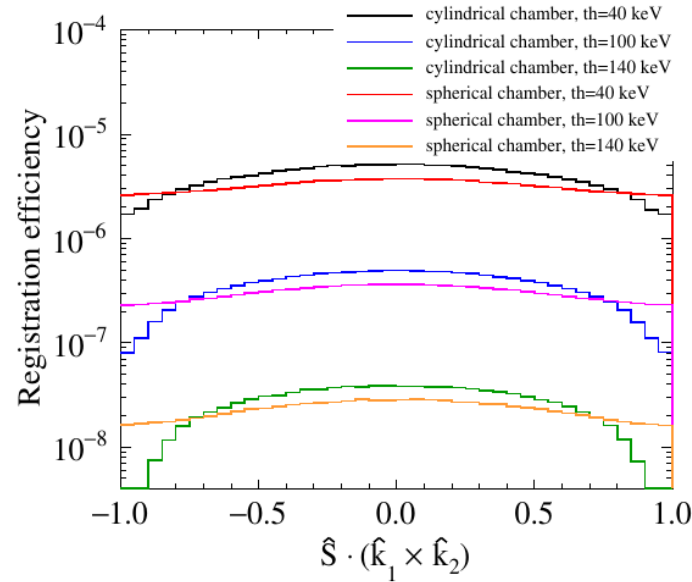
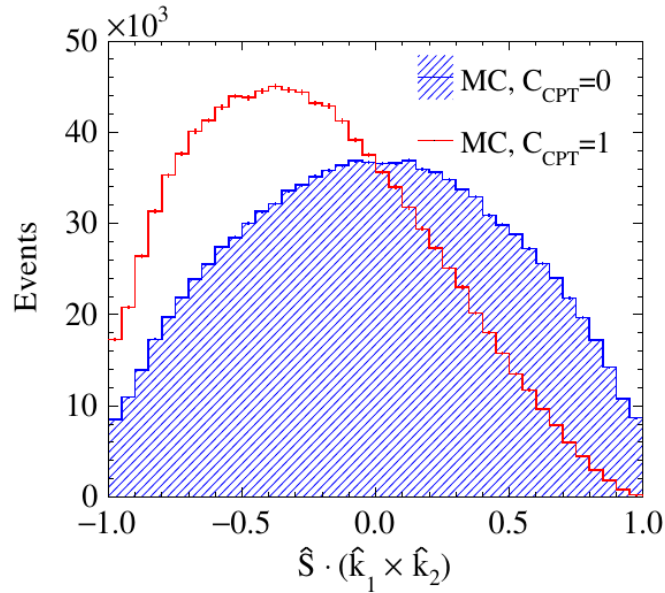
(b) 2γ annihilation with secondary Compton scattering.



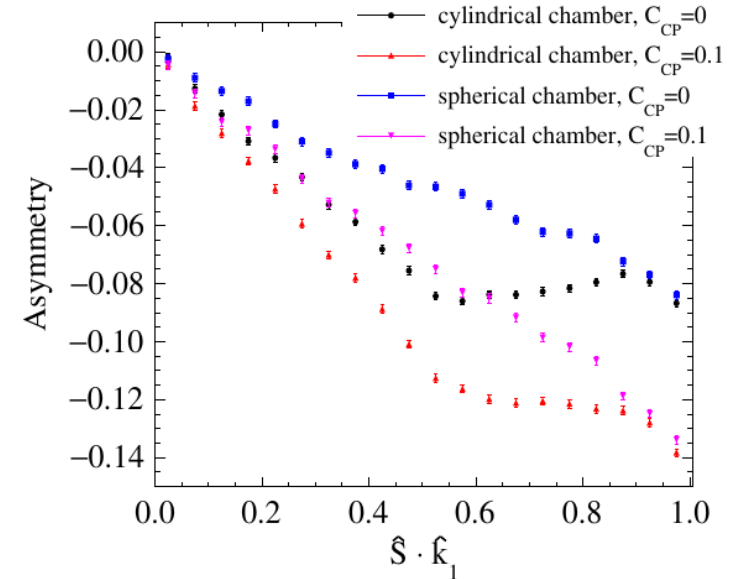
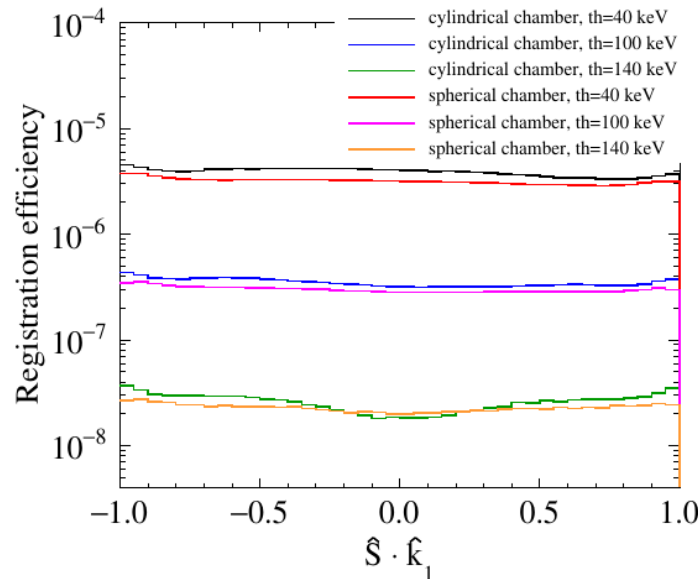
Detector improvements



Expected sensitivity



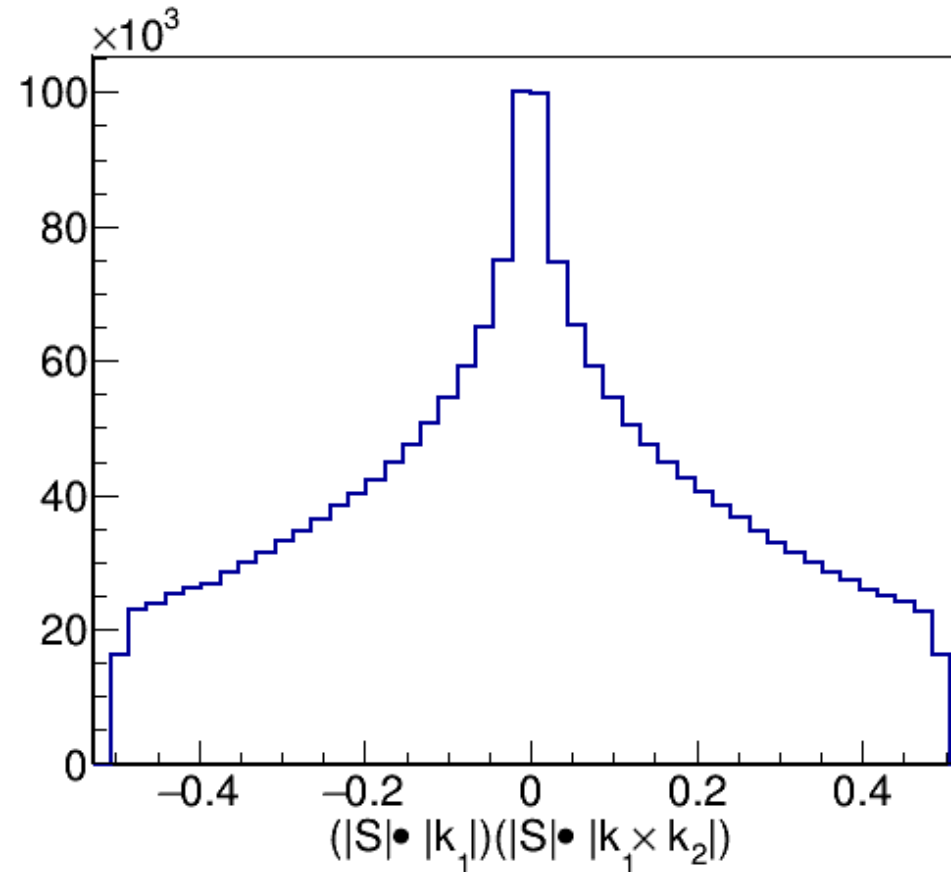
No.	Operator	C	P	T	CP	CPT
1	$\vec{S} \cdot \vec{k}_1$	+	-	+	-	-
2	$\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2)$	+	+	-	+	-
3	$(\vec{S} \cdot \vec{k}_1)(\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2))$	+	-	-	-	+



Control of detector asymmetries

$$(\vec{S} \cdot \vec{k}_1)(\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2))$$

- Insensitive to CPT violation in absence of o- P_s tensor polarization
 - No B field used in the current experiment
- \Rightarrow we expect $\langle 0 \rangle$ unless spurious asymmetries originate from detector/chamber geometry



$$\langle 0 \rangle = (0.99 \ +/- 1.7) \times 10^{-4}$$

o-Ps \rightarrow 3 γ operators involving spin

Presently studied with J-PET:

$$\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2) \quad \text{T \& CPT-violation sensitive}$$

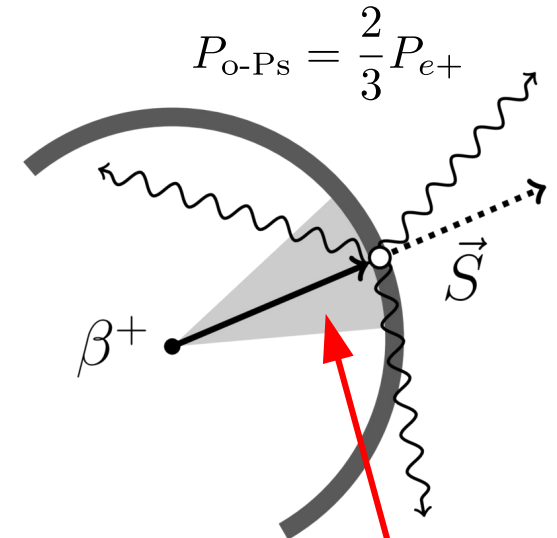
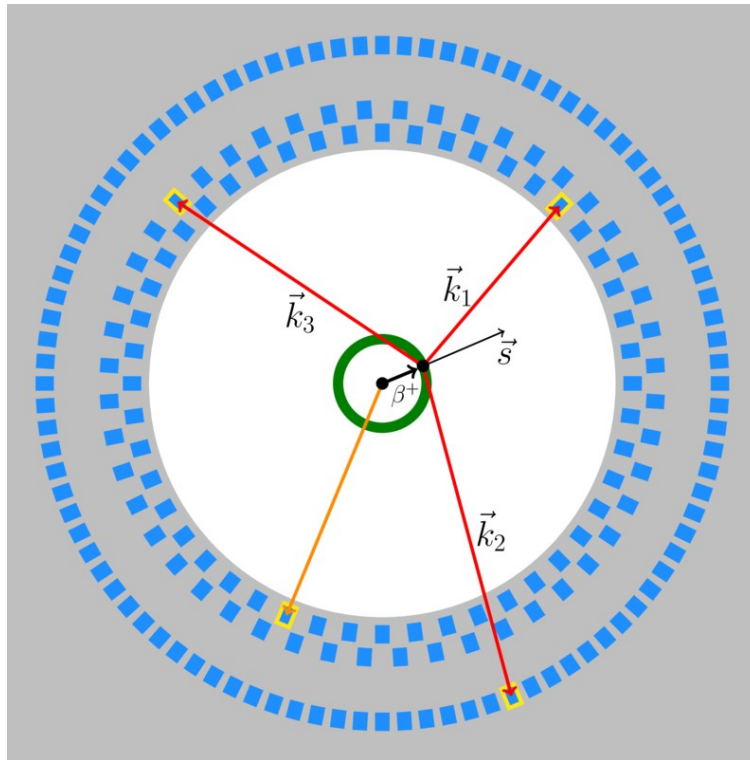
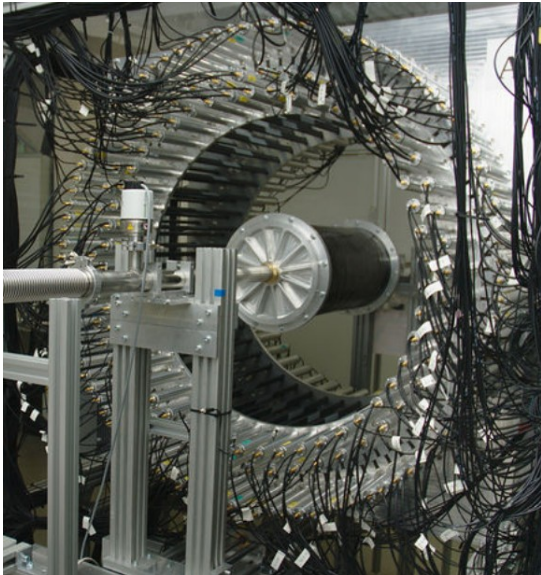
$$\vec{S} \cdot \vec{k}_1 \quad \text{CP-violation sensitive}$$

$$(\vec{S} \cdot \vec{k}_1)(\vec{S} \cdot (\vec{k}_1 \times \vec{k}_2))$$

T & CP-violation sensitive but requires o-Ps tensor polarization \rightarrow not available with the current J-PET approach

Event-by-event spin estimation

Using an extensive-size o-Ps production and annihilation medium



$$P_{e+} \approx \frac{v}{c} \cdot \frac{1}{2} (\cos \alpha + 1)$$

Effective polarization depends on o-Ps \rightarrow 3 γ vertex resolution