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# Deuteron-Deuteron Collision at 160 MeV

by  
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# Outline

- Introduction
- Experimental tools
- 4N System – a step forward
- **Data analysis for d+d @ 160 MeV**
  - Raw-analysis & Event selection
  - Kinematics and BINA acceptance
- Results of QFS in  $dd \rightarrow dpn$  : Comparison with first theories
- Summary

- ✓ **1935: Yukawa** presented a Theory
- ✓ **1947: Powell** proved the theory by experiments
  
- Today , many different Theoretical models are available to exactly describe the nuclear force between **any two nucleons**.

# Introduction

## Nuclear Force

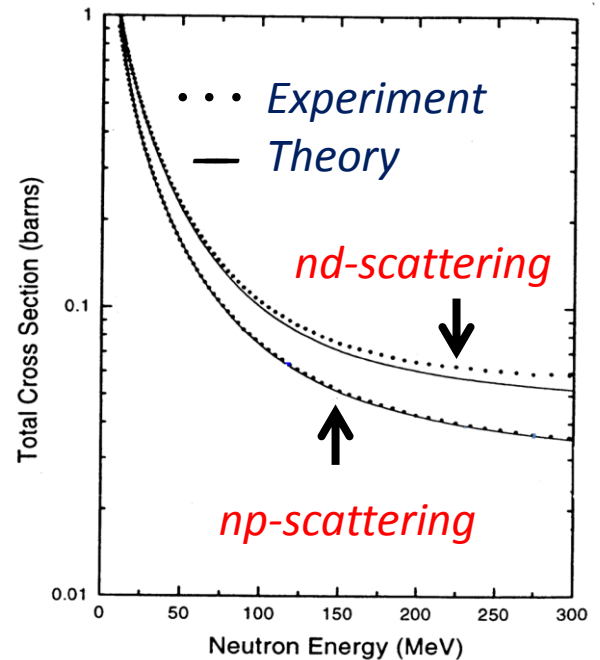
- ✓ **1935: Yukawa** presented a Theory
- ✓ **1947: Powell** proved the theory by experiments
- Today , many different Theoretical models are available to exactly describe the nuclear force between **any two nucleons**.

*...but FAILS to describe Interaction between more than two nucleons!*

- even for the simplest Atomic Nucleus  
e.g.  $^3\text{H}$  and  $^3\text{He}$

Model	[MeV]
Nijm I	7.72
Nijm II	7.62
AV18	7.62
Reid-93	7.63
<b>Exp.</b>	<b><u>8.48</u></b>

Binding  
Energy  
of  
Triton



High precision data from Los Alamos  
W. P. Abfalterer et al., PRL 81, 57 (1998)

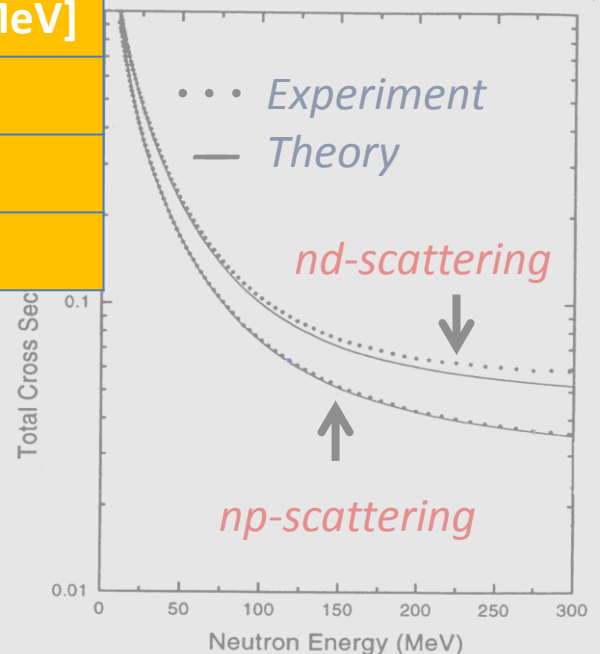
# Introduction

## Adding Thee Nuclear Force (3NF) helps

- ✓ 1935: Yukawa presented a Theory
- ✓ 1947: Powell proved the theory by experiments
- Today, many different Theoretical models are available to exactly describe the nuclear force between **any two nucleons**.

...but FAILS to describe  
more than two nucleons

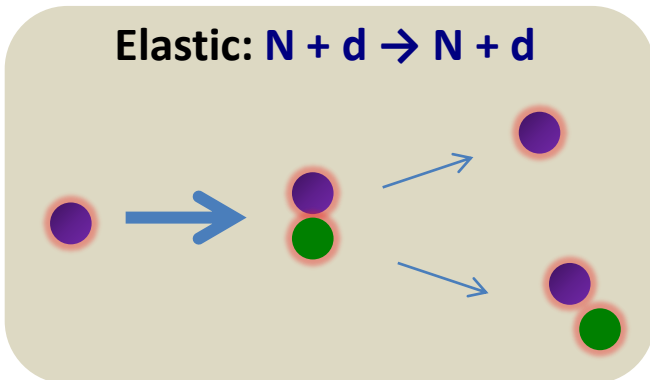
Model	${}^3\text{H}$ [MeV]	${}^4\text{He}$ [MeV]
2NF	7.62	24.2
2NF +3NF	8.47	28.3
<b>Experiment</b>	<b><u>8.48</u></b>	<b><u>28.4</u></b>



High precision data from Los Alamos  
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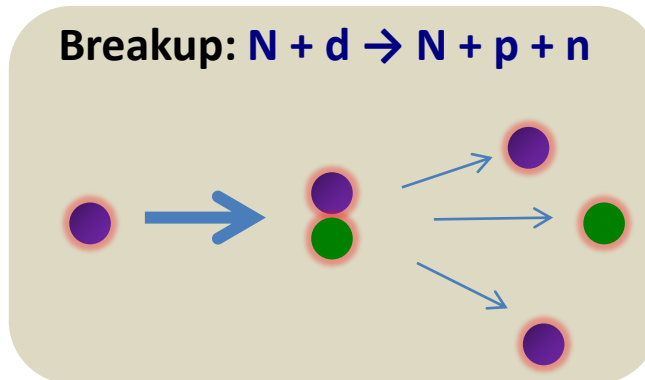
## Nucleon - Deuteron Scattering (Relatively Simplest but not simple):

Elastic:  $N + d \rightarrow N + d$



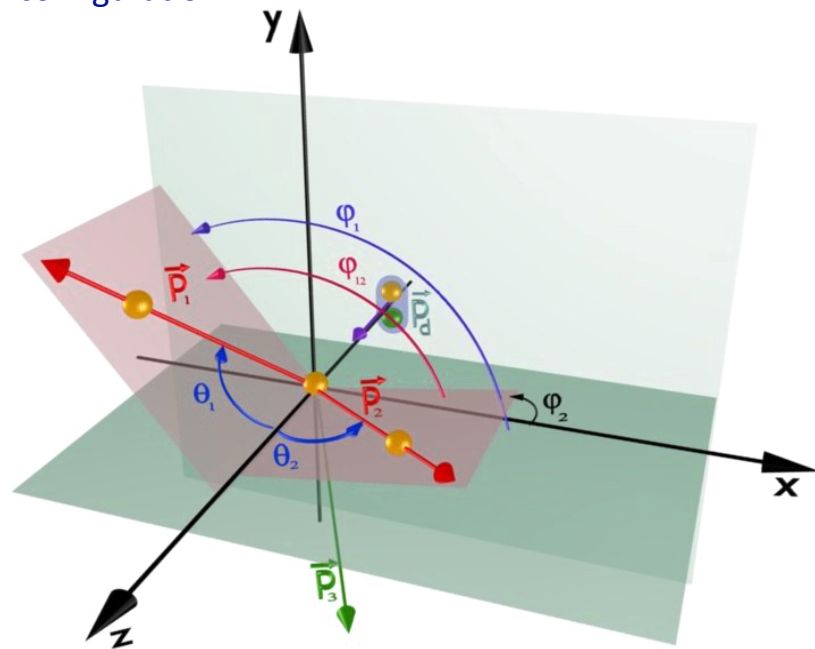
➤ Well-defined kinematic relations

Breakup:  $N + d \rightarrow N + p + n$

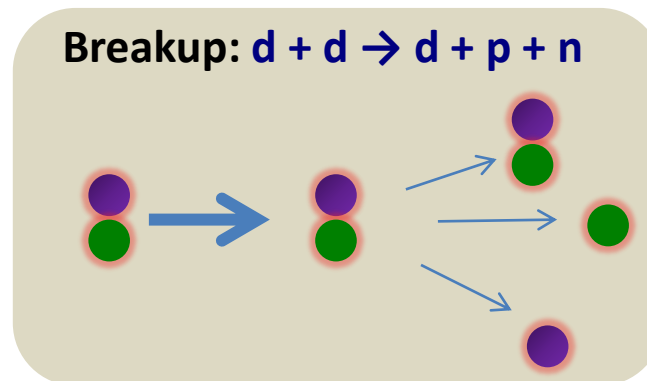


➤ rich phase-space: a large amount of kinematical configuration.

**deuteron-nucleon breakup**  
reaction is well suited to  
study 3N interactions



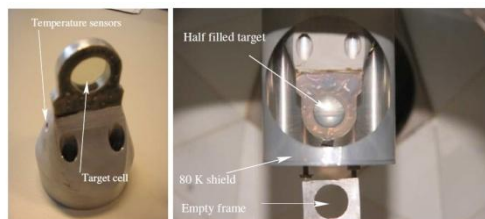
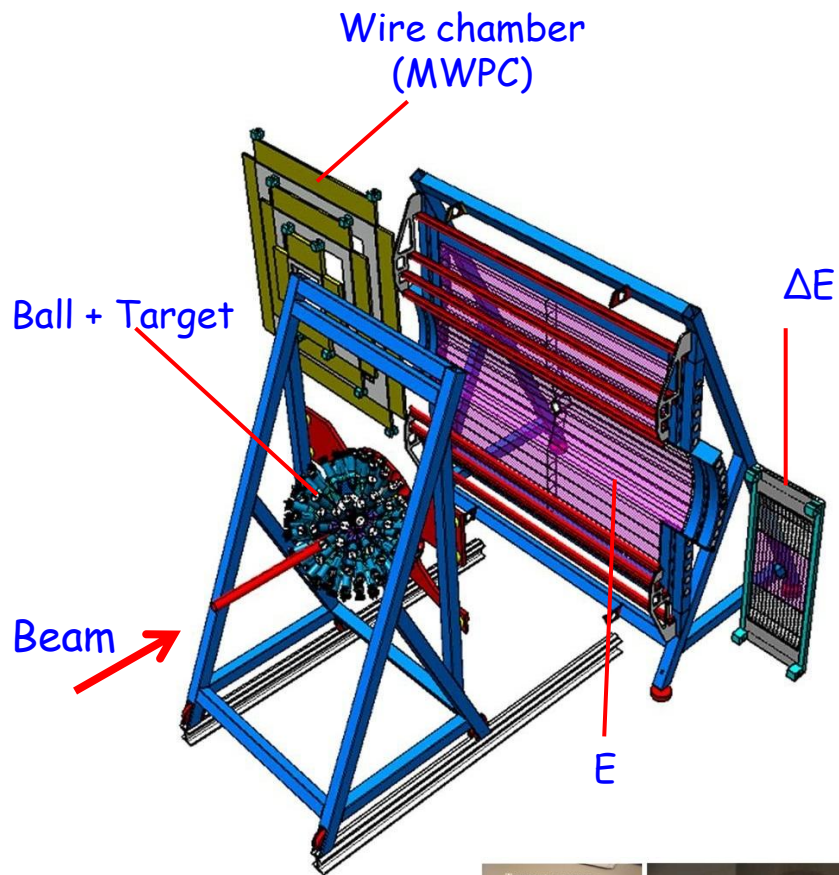
## 4N System - a step forward



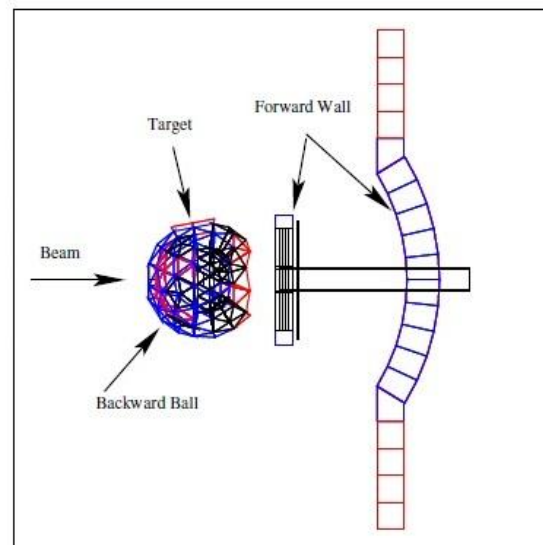
➤ rich phase-space: a large amount of kinematical config.

In the same manner, we investigate  $dd \rightarrow dpn$  breakup

**BINA Detector** Dedicated for few-body studies!  
High-precision data !



**TARGET**





## ***4N System – a step forward***

STATUS: Poor knowledge

### **Theory:**

- > difficult (Technically & computationally)
- > available (not exact) models fail
- > ab-initio calculations for very low energies
- > recent progress by A. Deltuva

### **Experiment:**

- Old data, at low energies
- Most of the data for dd elastic scattering
- Breakup data – very scarce  
(KVI dd breakup data at 130 MeV )

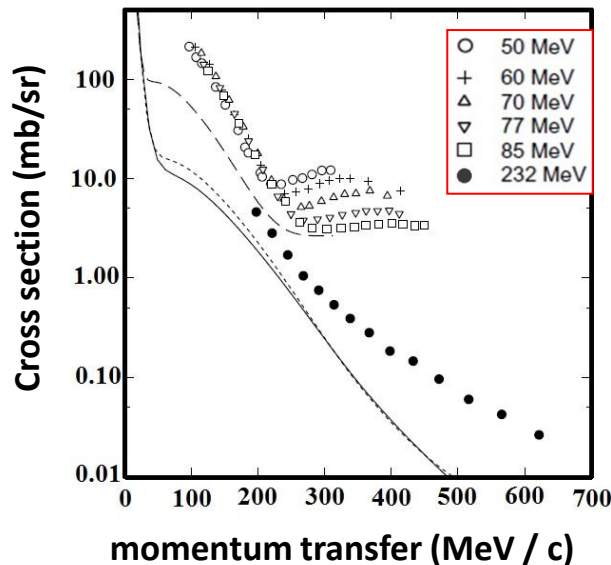
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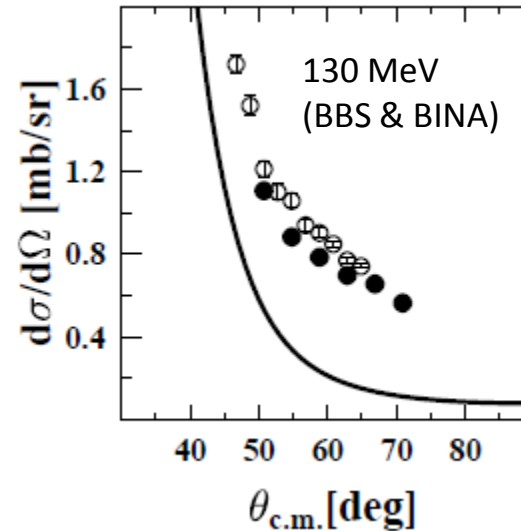
## Experiment:

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(KVI dd breakup data at 130 MeV)

### dd elastic scattering: theory vs experimental data



C. Alderliesten, Phy Rev C, 18(5), 1978  
A. Micherdzinska, Phys Rev C 75, 2007



From KVI, BINA and BBS

calculations by A. C. Fonseca :	---	52 MeV
	.....	191 MeV
	—	232 MeV

Approximation used in Alt-Grassberger-Sandhas (AGS) equation for 4N  
**CD-Bonn +  $\Delta$  potential.**

### **Theory:**

- > difficult (Technically & computationally)
- > available (not exact) models fail
- > ab-initio calculations for very low energies
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### **Experiment:**

- Old data, at low energies
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(KVI dd breakup data at 130 MeV )

Situation of 4N-study today  
SIMILAR TO  
situation of 3N-study 2 decades ago

- Experiment performed at KVI with BINA in April 2011.  
beam: **deuteron**,  
energy: **160 MeV**,  
target: **Liquid Deuterium**

## d+d - EVEN MORE COMPLICATED SYSTEM

$d + d \rightarrow d + d$  ... elastic scattering

$d + d \rightarrow d + p + n$  ... three-body breakup

$d + d \rightarrow p + p + n + n$  ... four-body breakup

$d + d \rightarrow d + p (+ n_{\text{spectator}})$  ... QFS

$d + d \rightarrow p + p (+ 2n_{\text{spectator}})$  ... double QFS

$d + d \rightarrow {}^3\text{H} + p$  ... neutron transfer

$d + d \rightarrow {}^3\text{He} + n$  ... proton transfer

Quasi free scattering:

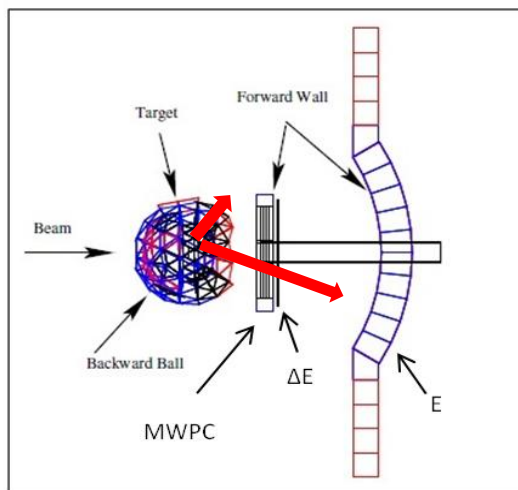
$dd \rightarrow dp$  (neutron spectator)

Two possibilities

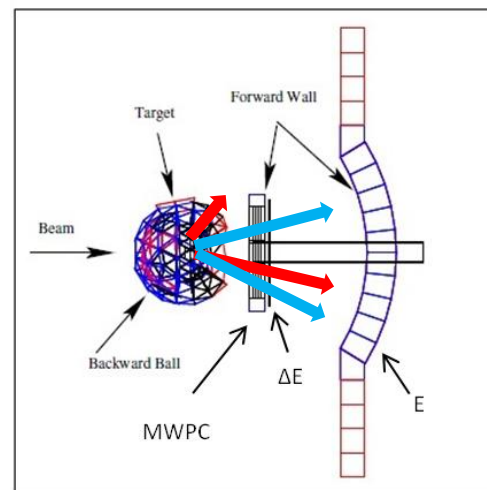
**pd** (half of beam energy)

**dp** (full beam energy)

## dd elastic scattering

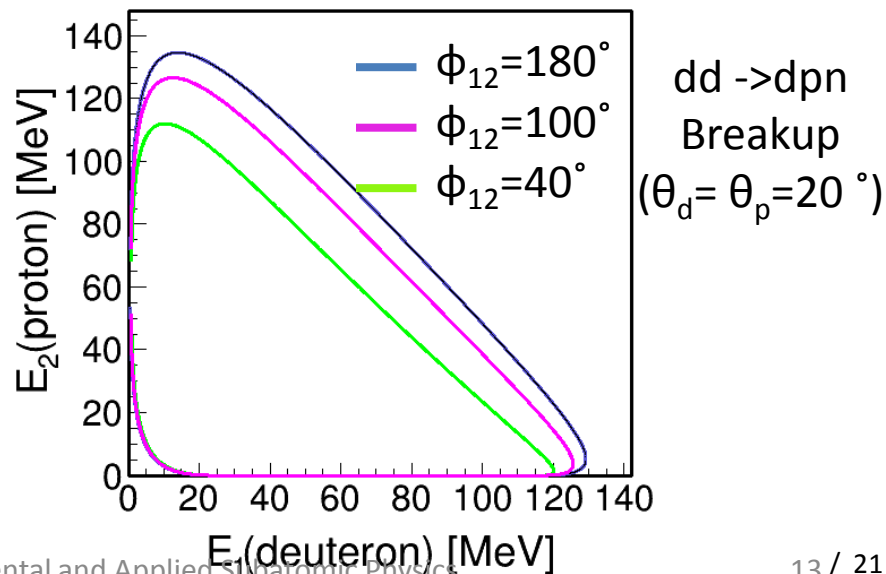
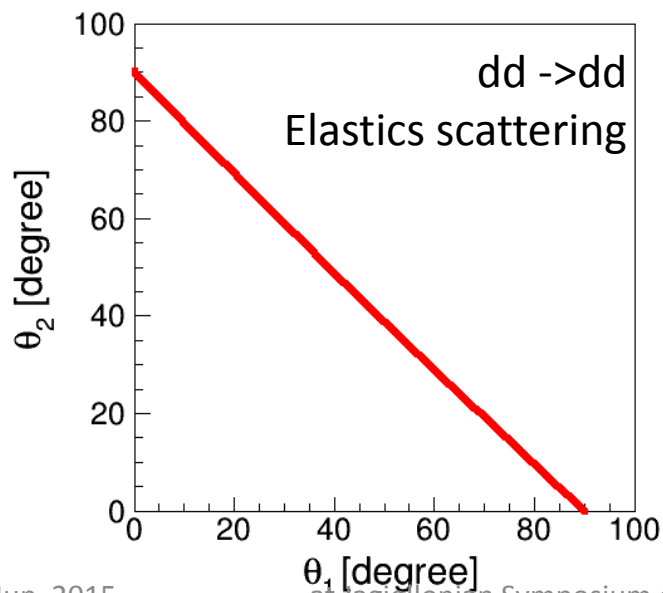


## Breakup channels



**WALL-BALL  
&  
WALL-WALL**

Only possible  
in  
**WALL-BALL**  
coincidences



# Data Analysis

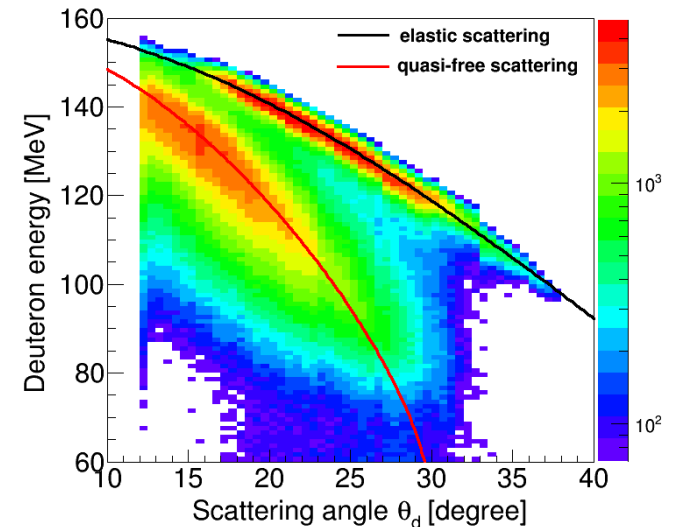
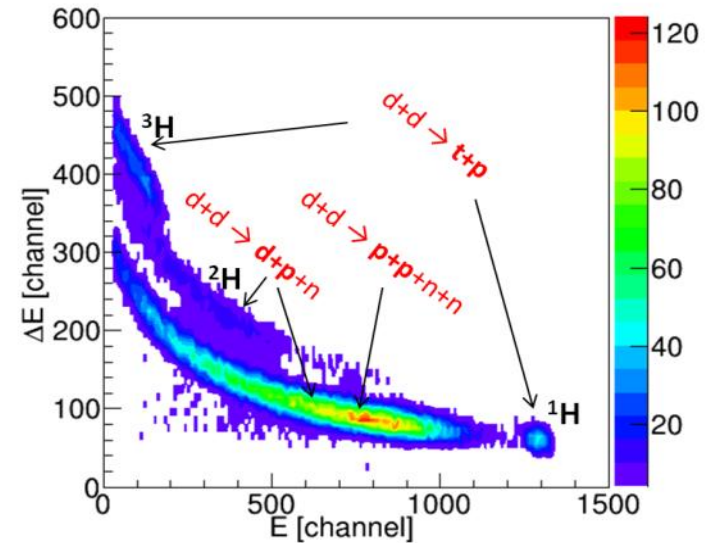
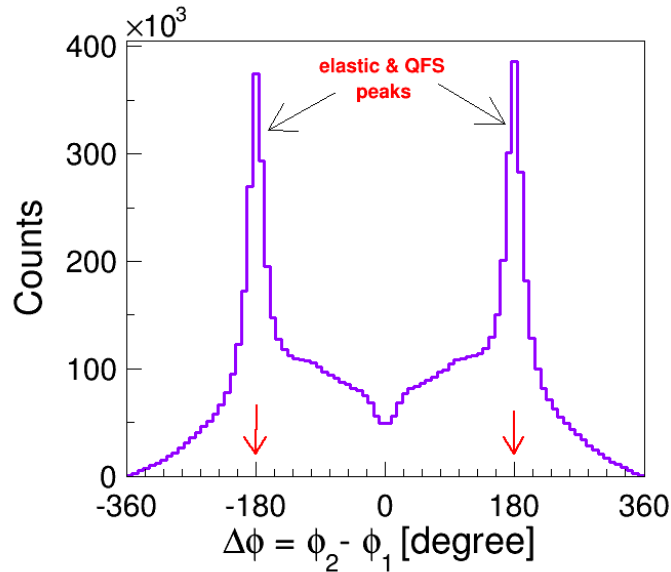
## Steps:

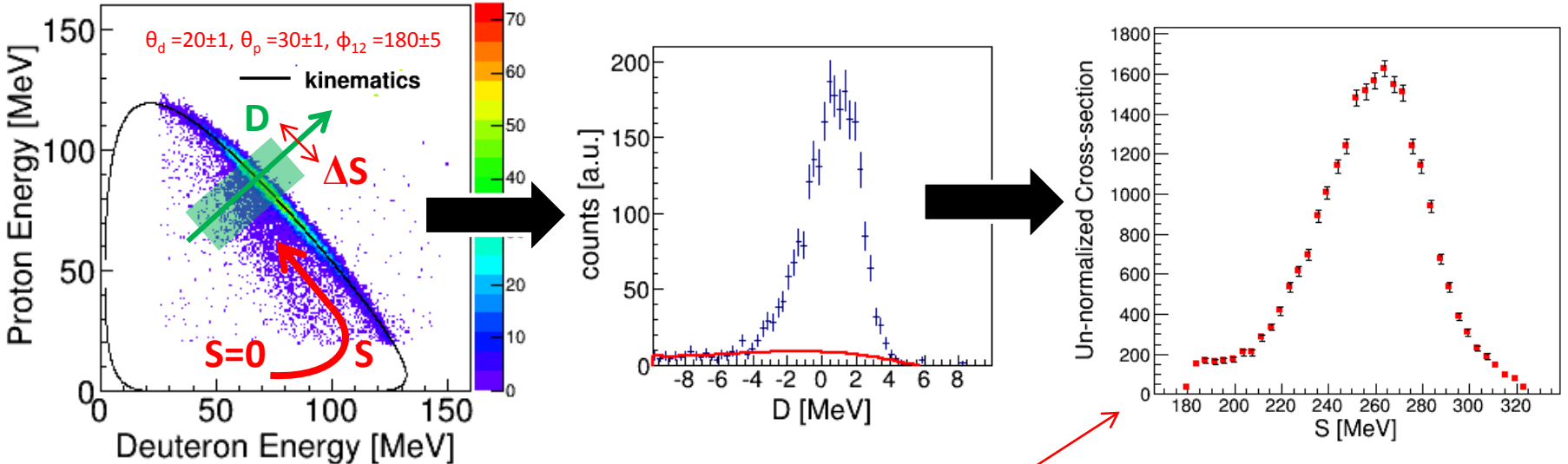
Particle ID  $\rightarrow$  Calibration  $\rightarrow$  Channel discrimination

## basic assumptions:

Coincidence of two charged particles

Co-planarity, i.e.  $\Delta\varphi = \varphi_2 - \varphi_1 = \pm 180^\circ$  (for elastic scattering)



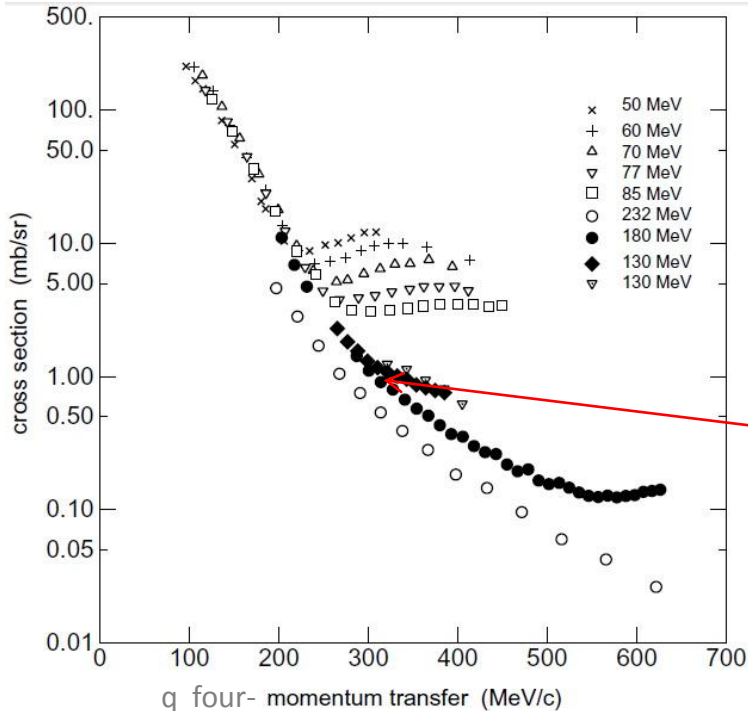


-> Cross section normalised with elastic scattering cross section (of course differential)

$$\frac{d^5\sigma}{d\Omega_1 d\Omega_2 dS}(S, \Omega_1, \Omega_2) = \frac{d\sigma_{el}}{d\Omega_1}(\Omega_1) \cdot \boxed{N_{br}(S, \Omega_1, \Omega_2)} \cdot \frac{\Delta\Omega_1^{el}}{\Delta\Omega_1 \Delta\Omega_2 \Delta S} \cdot \frac{\epsilon^{el}(\Omega_1^{el}) \epsilon^{el}(\Omega_2^{el})}{\epsilon(\Omega_1) \epsilon(\Omega_2)}$$

This quantity is needed  
 counts  
 angles & energy bins  
 detector efficiencies

## Normalisation of dd elastic data



Invariant quantity **four-momentum transfer**,  $q = -t^2$   
Where  $t$ =Mandelstam variable

Simplified for dd elastic scattering as:

$$t = 2p_{1cm}^2 (\cos \theta_{c.m.} - 1)$$

One can extrapolate the 130 MeV and 180 MeV data to extract the 160 MeV.

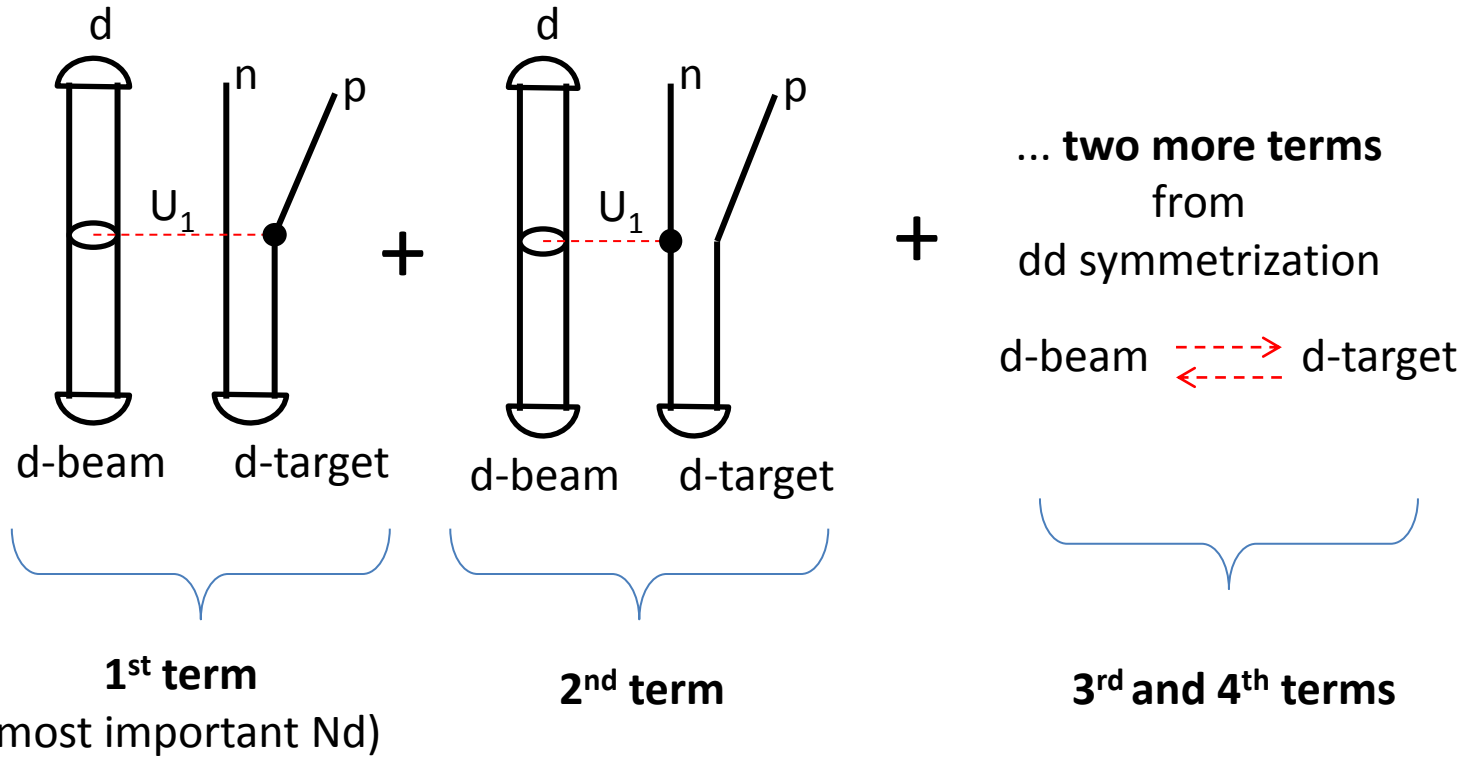
Most reliable is to take a point at **scaling region**

Ref: C. D. Bailey, IUCF, PhD Thesis, 2009



# RESULTS

CD Bonn +  $\Delta$  (FIRST calculations by A. Deltuva)



$U_1 = \text{full } Nd \text{ scattering operator}$

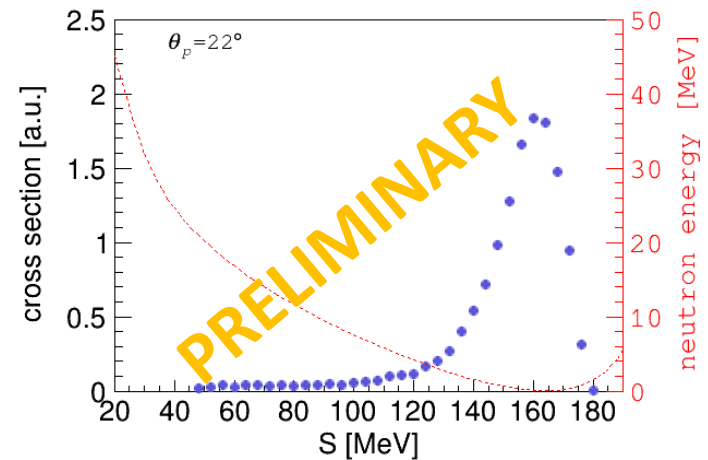
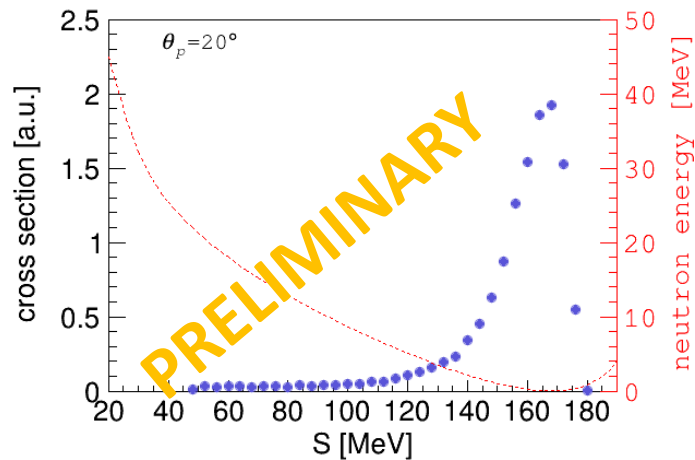
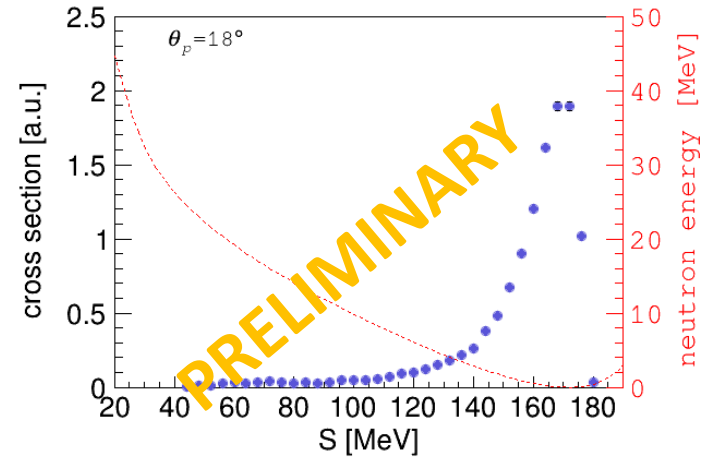
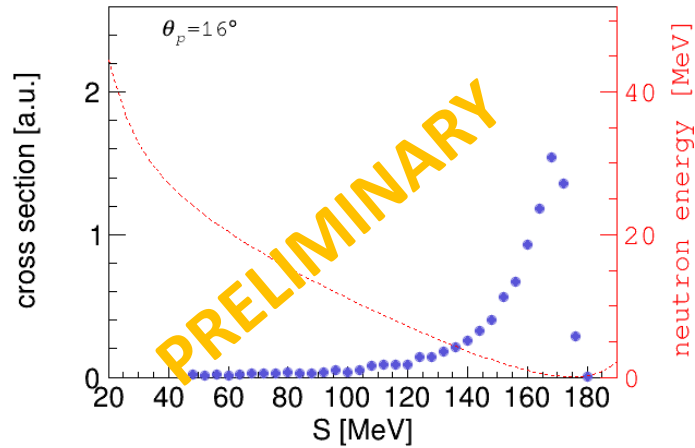
$T_{dpn} = 2(1 - P_{34})U_1 = \text{Breakup operator in } dN \text{ single-scattering approx}$

Breakup amplitude:  $\langle dpn | T_{dpn} | dd \rangle_{\text{symmetrized}}$

$$\theta_d = 26^\circ, \phi_{dp} = 180^\circ$$

scaled with arbitrary factor  
just to compare shape with predictions

Neutron energy  
(when close to 0  
i.e. spectator)

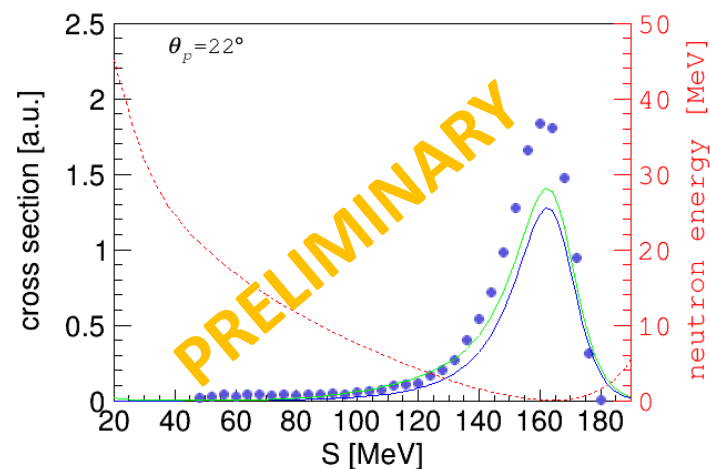
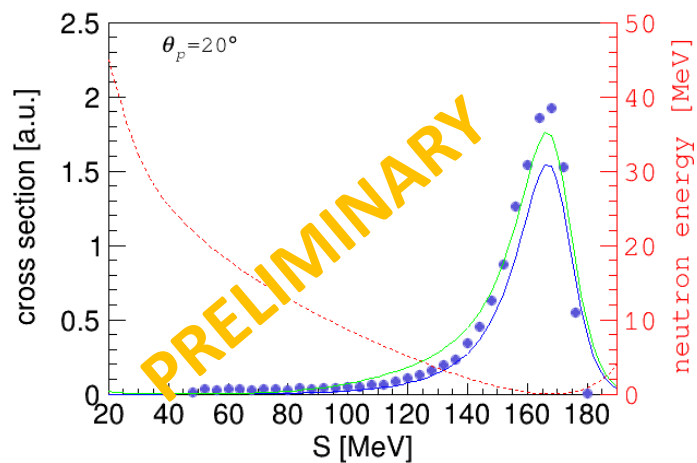
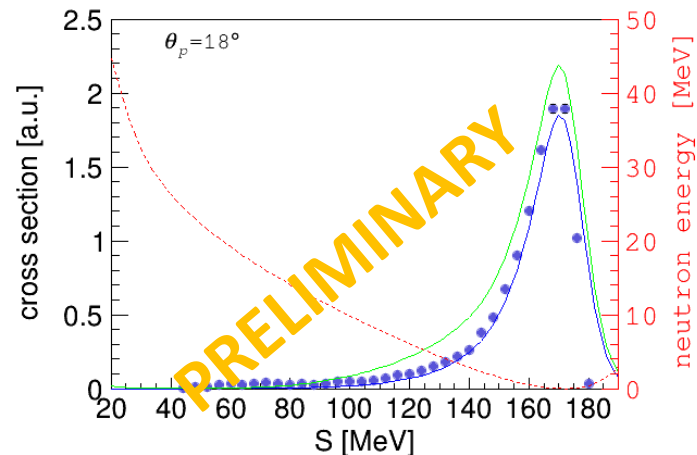
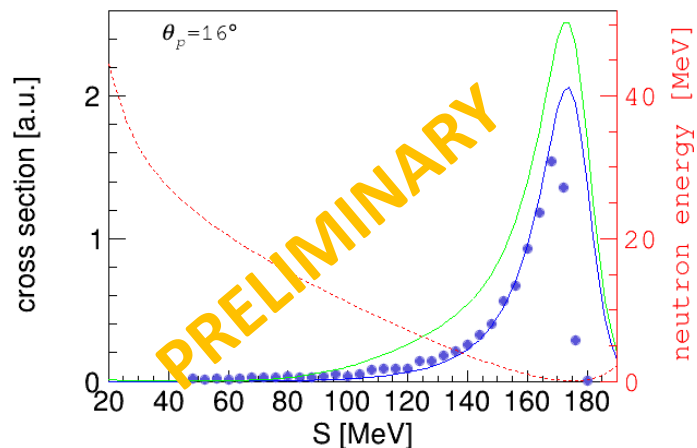


(calculations by A. Deltuva)

$$\theta_d = 26^\circ, \phi_{dp} = 180^\circ$$

- Only first term in  $T_{dpn}$  (i.e. dp elastic scattering)
- all four terms  $T_{dpn}$  taken into account

- - - Neutron energy  
(when close to 0  
i.e. spectator)



- **Detail analysis of systematic effects**
- theoretical progress in 4N is urgently needed, the recent results are very promising
- **3N systems can be further studied with BINA@CCB**
- complementary studies of 4N systems, e.g. in  $p+3\text{He} \rightarrow p+p+d$  reaction, are planned

➤ new set of very precise and numerous experimental data for  $dd$  breakup at 160 MeV :

normalized cross section for the breakup reaction following combinations of angles:

$\theta_1, \theta_2 = 16^\circ - 28^\circ$  (in step of  $2^\circ$ ),  $\phi_{12} = 180^\circ, 160^\circ, 140^\circ$   
(in total about 150 data points)



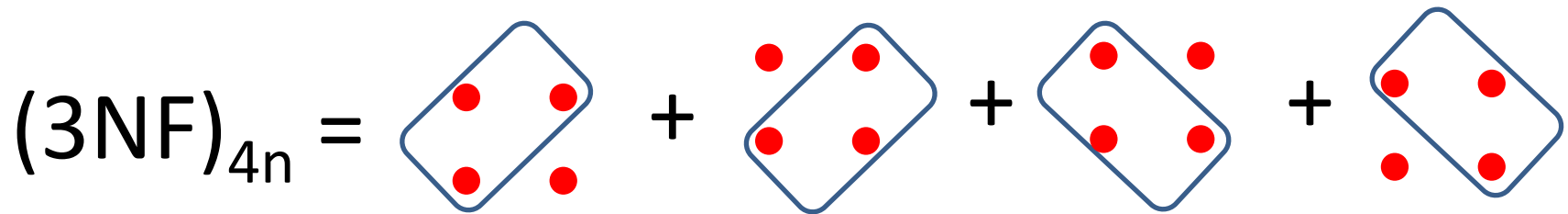
**Thank you for your attention !!!**

## 3NF helps but.....

-> some discrepancies (Ay puzzle, star-anomaly, problems with description of analyzing powers at medium energies)

-> a very subtle & hard to detect.

-> it's expected to be enhanced in 4N system.



$$3NF/2NF \ll 1$$