

Ultra-Relativistic Heavy-Ion Collisions and Quark-Gluon Plasma

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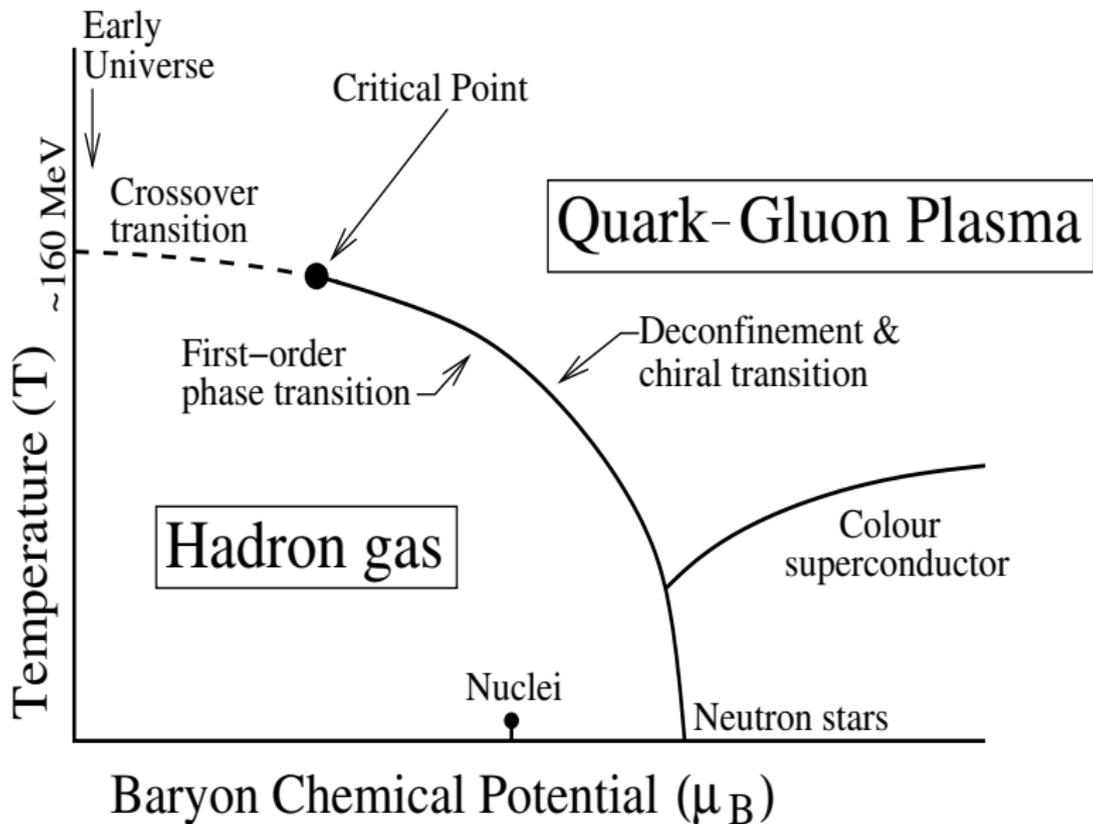
- Overview of this Field
- Recent Advances — Experimental, Theoretical
- Take-Home Message / Open Questions

Fundamental Questions

This field addresses some **fundamental questions** regarding QCD:

- Nature of equilibration processes in QCD
- Collectivity (especially in small systems) as an **emergent phenomenon** in QCD
- How to experimentally probe the physical degrees of freedom relevant in the QCD transition region

QCD Phase Diagram (schematic)



THE BIG IDEA IS TO MAP OUT THE QCD
PHASE DIAGRAM **QUALITATIVELY** and
QUANTITATIVELY, and also STUDY QCD
NON-EQLBM (TRANSPORT) PROPERTIES.

RELATIVISTIC HEAVY-ION COLLISIONS IS
THE ONLY AVAILABLE LABORATORY TOOL.

Various Stages

- Collision of two Lorentz-contracted nuclei (or two CGC plates)
- Deposition of kinetic energy & formation of a fireball (or Glasma)
- Liberation of partons from the strong chromofields (or Decoherence)
- Approx. local thermalization of partons: Formation of QGP
- Hydrodynamic expansion, cooling, dilution. QCD EoS.
- Particlization — Kinetic theory
- Chemical freezeout: inelastic processes stop
- Kinetic freezeout: elastic scatterings stop. Free streaming.
- Detection of particles — Extraction of QGP properties

Wealth of Data

- **Initial-State Variables:** beam energy, beam species, centrality of collision
- **Final-State Variables:** particle species, transverse momentum, rapidity or pseudo-rapidity
- **Observables (differential or integrated):** charged particle multiplicity, p_T spectra, anisotropic transverse flows for $n = 1 - 6$, strangeness enhancement, J/ψ suppression, Υ suppression, BE correlations, jet quenching, 2-,3- and multi-particle correlations, γ and ll spectra, ...

Any model has to agree with this body of data

Standard Model of URHICs

- **Initial state:** Glauber model / Colour-Glass Condensate-based model
- **Pre-equilibrium evolution:** AMPT or classical Yang-Mills eqs
- **Intermediate evolution:** Rel. 2nd-order hydro \oplus lattice QCD EoS
- **End evolution:** Rel. Boltzmann dynamics leading to a freeze-out
- **Final state:** Detailed measurements (single-particle inclusive, two- & multi-particle correlations, etc.) are available.

Aim: To achieve a quantitative understanding of the thermodynamic and transport properties of QGP, e.g., its EoS, transport coeffs, etc.

Major hurdle

Event-by-event fluctuations
(not just in the initial state)

Sources of Event-by-Event Fluctuations

- **Initial-state fl.:** Quantum fl. in the distributions of N 's in $\Psi_{nucleus}$. In addition, fl. in the colour charge distributions inside a N . Hence, e-by-e fl. in $\epsilon_i(x, y)$ and $\mathbf{v}_i(x, y)$ at nucleonic and sub-nucleonic scales.
- **Hydrodynamic fl.:** Due to finite particle no. in a given coarse-grained fluid cell. Local thermal noise or fl. in $\epsilon(x, y)$ and $\mathbf{v}(x, y)$. Deterministic vs stochastic hydrodynamics.
- **Fl. induced by hard processes:** Jet prod. is a random process. Hard partons propagating in the medium impart energy to the medium in a random manner.
- **Freezeout fl.:** Finite particle no. effects during and after the freezeout (or particlization of the fluid).

Hence every event is different!

Initial-State Fluctuations

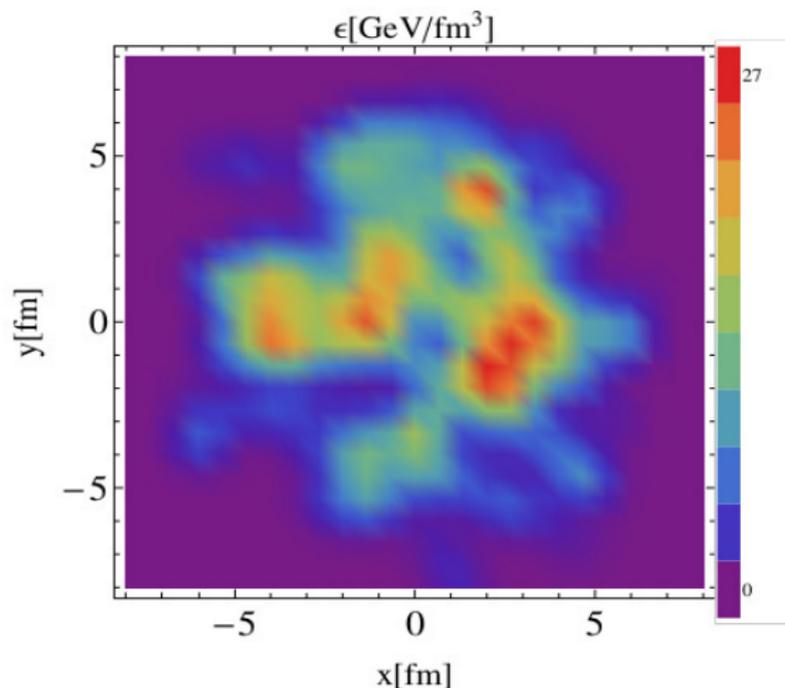


Fig. from
Ollitrault &
Gardim,
1210.8345

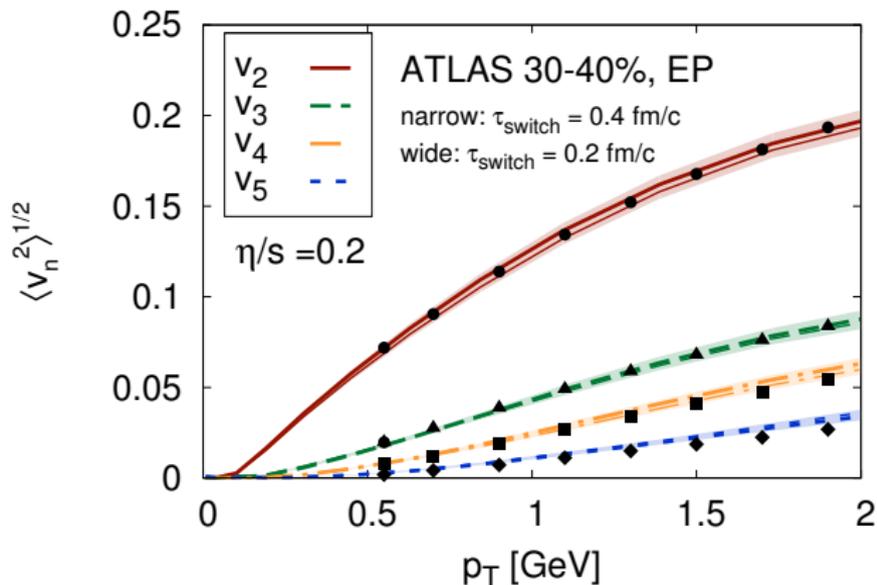
Initial energy density in the transverse plane at $z = 0$ in a simulated random **central** Pb-Pb collision at 2.76 TeV.

Final-state flow pattern is the collective hydrodynamic response to the **initial** conditions fluctuating event by event.

HYDRO[†] PLAYS A **CENTRAL ROLE** IN
UNDERSTANDING THE **SOFT** SECTOR OF
RELATIVISTIC HEAVY-ION COLLISIONS.

[†] Relativistic, dissipative, causal (second-order)
hydrodynamics

Some Successes of Hydrodynamics Picture ...



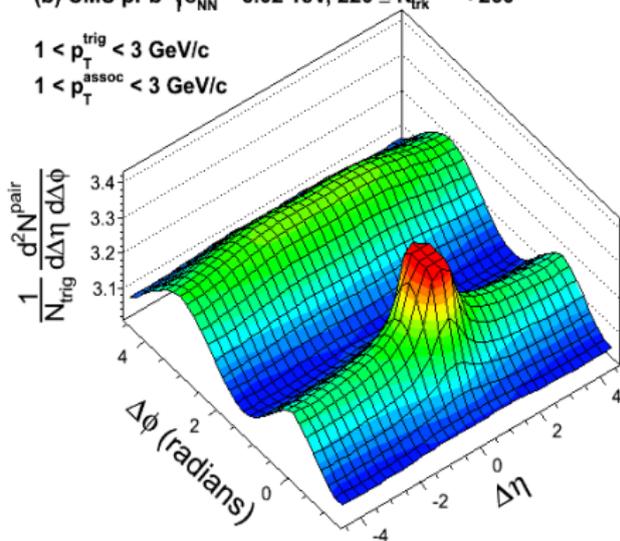
Basic idea: $v_n(\text{perfect fluid}) > v_n(\text{viscous fluid})$
IF one has a good control on $v_n(\text{perfect fluid})$, one can adjust η/s to fit the data on v_n , and thus **extract η/s**

Ridges in pPb and $PbPb$ collisions at LHC

(b) CMS pPb $\sqrt{s_{NN}} = 5.02$ TeV, $220 \leq N_{trk}^{offline} < 260$

$1 < p_T^{trig} < 3$ GeV/c

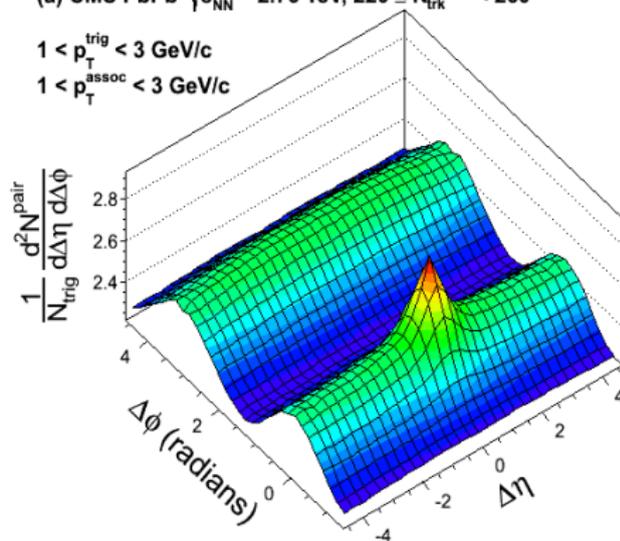
$1 < p_T^{assoc} < 3$ GeV/c



(a) CMS $PbPb$ $\sqrt{s_{NN}} = 2.76$ TeV, $220 \leq N_{trk}^{offline} < 260$

$1 < p_T^{trig} < 3$ GeV/c

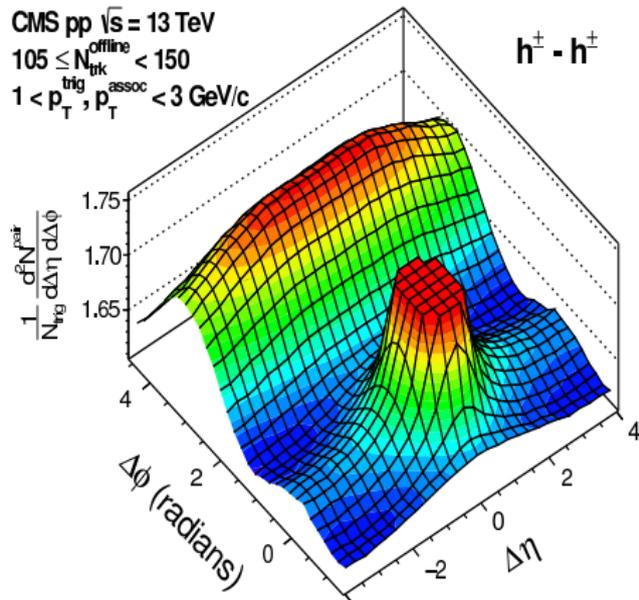
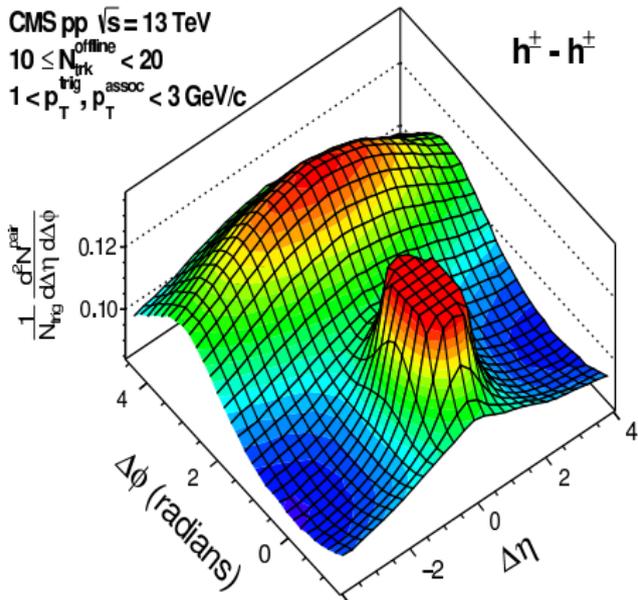
$1 < p_T^{assoc} < 3$ GeV/c



Phys. Lett. B 724 (2013) 213

Ridge in pp collisions

CMS Collab, arXiv:1606.06198



Ridge: One of the key experimental pieces of evidence for the strong collective behaviour comparable to a fluid.

Quark-Gluon Plasma is

the smallest, hottest, densest, and most perfect
fluid ever produced in the laboratory

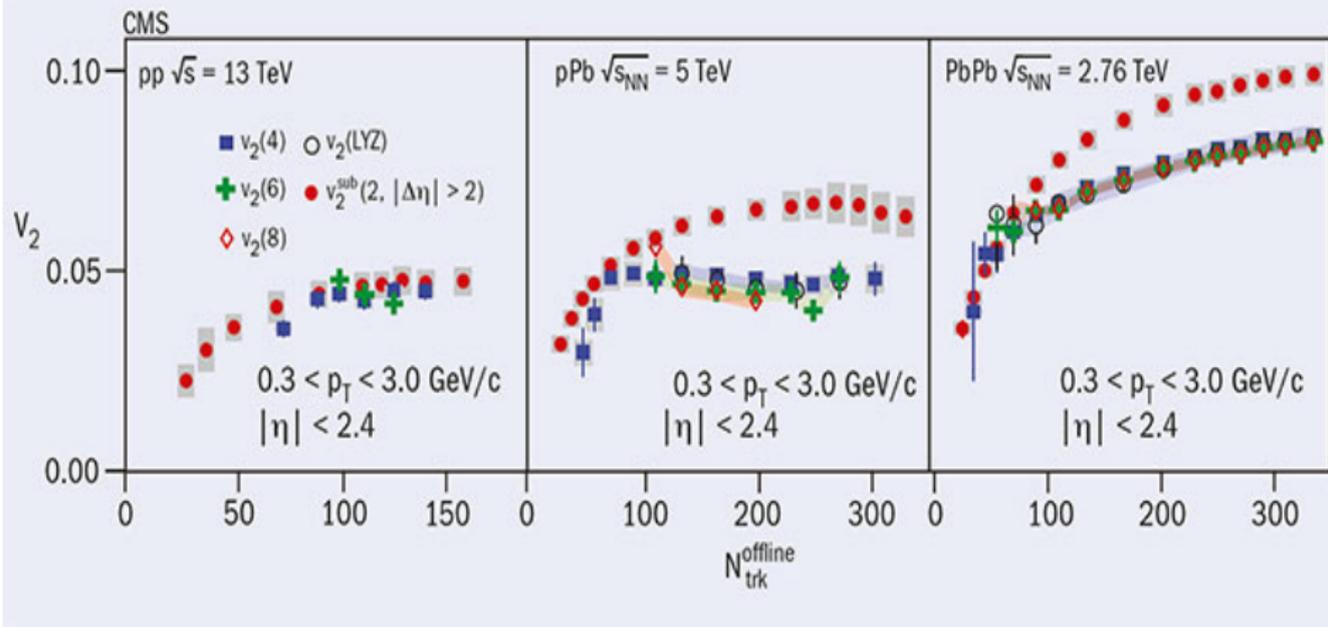
- **Smallest:** $R \sim 10$ fm
- **Hottest:** $T \sim 200$ MeV $\sim 2 \times 10^{12}$ K
(T at the core of the sun $\sim 1.6 \times 10^7$ K)
- **Life-time:** $\sim 3 \times 10^{-23}$ sec
- **Most perfect:** Even more so than liquid helium

Some Recent (\sim 5-6 years) Developments

- Collectivity in small systems
- Longitudinal dynamics
- Event-plane correlators
- Stochastic hydrodynamics
- Anisotropic hydrodynamics (Krakow)
- New flow analysis method

Collectivity in **Small** Systems

Elliptic Flow (for charged particles) in pp, pPb, PbPb



CMS Collab, [arXiv:1606.06198](https://arxiv.org/abs/1606.06198)

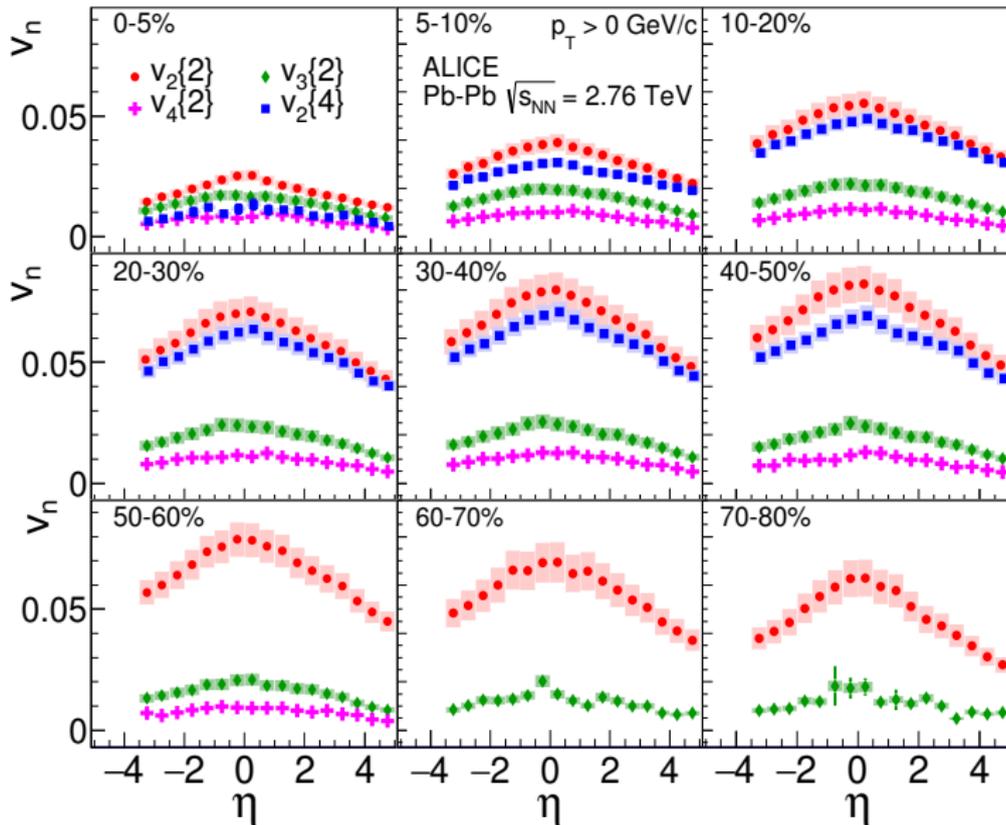
Evidence for **collectivity** in **pp** collisions at the LHC,

First extraction of v_2 in **pp** collisions using multi-particle correlations.

Longitudinal dynamics of the fireball formed in HE collisions:

- Forward-backward rapidity correlations \longrightarrow Mechanism of particle production in HE AA and pA collisions
- Event-plane decorrelation and factorization breakdown for particles of different η were demonstrated recently
- η dependence of v_n \longrightarrow Mechanism underlying collectivity: hydrodynamics or saturation?

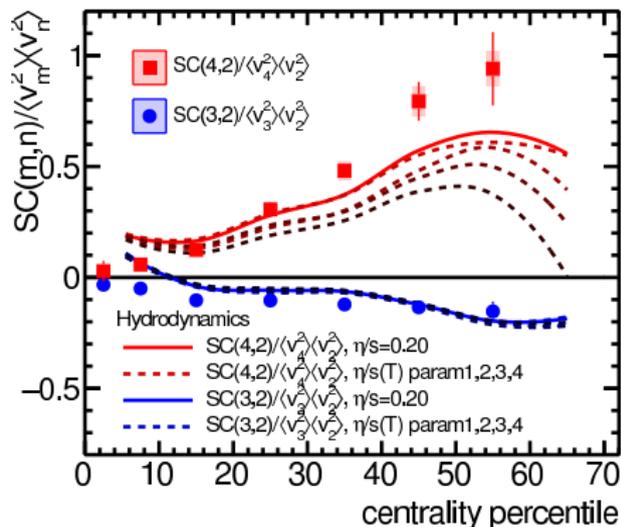
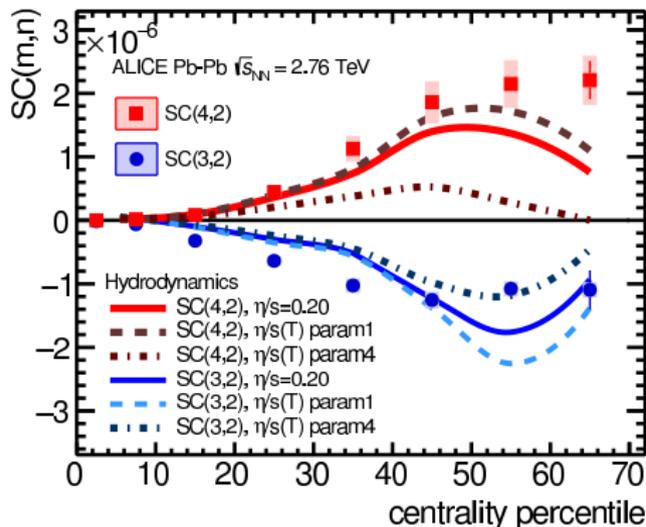
Longitudinal Correlations... ALICE Collab. PLB (2016)



Origin of Longitudinal Correlations

- Fluctuations in multiplicity $dN/d\eta$ e-by-e. Not just statistical but also due to $N_{part}(proj) \neq N_{part}(tgt)$.
- Fluctuations in anisotropic flow $v_n(\eta)$ e-by-e. Not just statistical but also due to $\Psi_n(proj) \neq \Psi_n(tgt)$.
- Symmetry, if any, arises after event averaging.
- $dN/d\eta$ and $v_n(\eta)$ need to be treated **on equal footing**

Correlations bet. v_2, v_4 and $v_2, v_3 \dots$ Pb-Pb, 2.76 TeV, PRL 2016



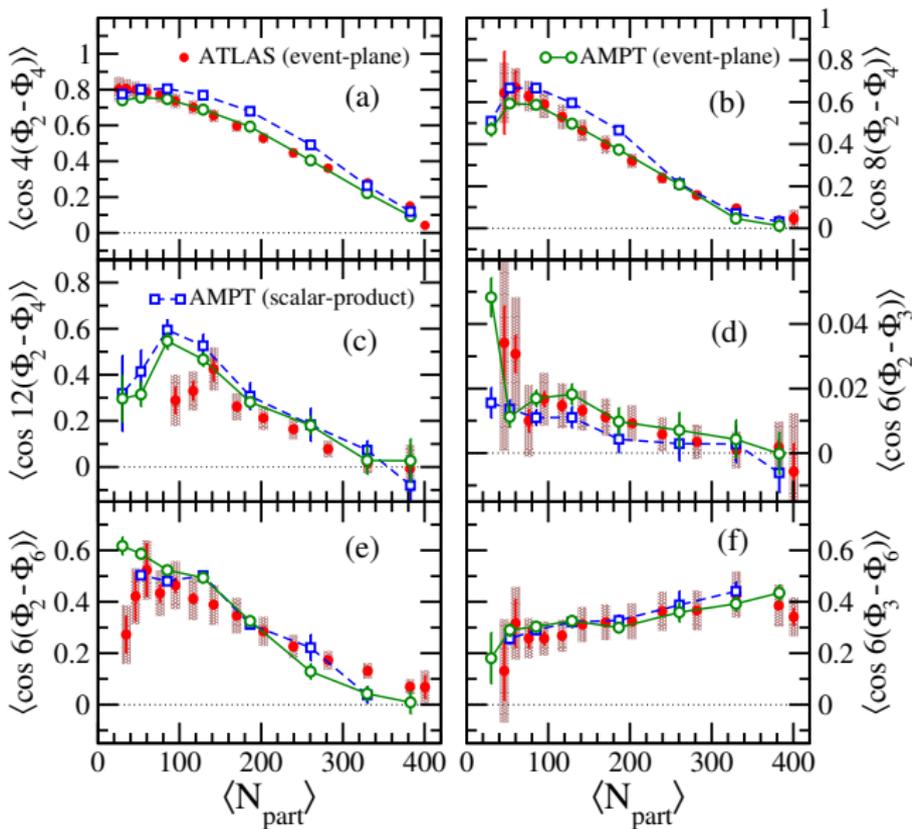
$$SC(m, n) = \langle v_m^2 v_n^2 \rangle - \langle v_m^2 \rangle \langle v_n^2 \rangle$$

Symmetric Cumulants = Standard Candles (old name) = Correlations between the **amplitudes** of anisotropic flow in diff. Fourier harmonics

Event-Plane Correlators

- **Pair** correlations (or the anisotropic flow v_n extracted from them) are by now reasonably well understood.
- Event-plane correlations: correlations among event planes (Ψ_n) corresponding to different harmonics.
- **Represent higher-order correlations, involving at least three particles.**
- They bring in a large number of **new observables** with a promise to provide new, detailed insight into the hydrodynamic response & the initial-state phenomena.
- **They open a new direction in heavy-ion physics.**
- **ATLAS @ LHC (2013):** Two- and three-plane correlators. Predictions exist for four-pl correlators.

Two-Event-Plane Correlators ... Pb-Pb, 2.76 TeV, PRC (2013)

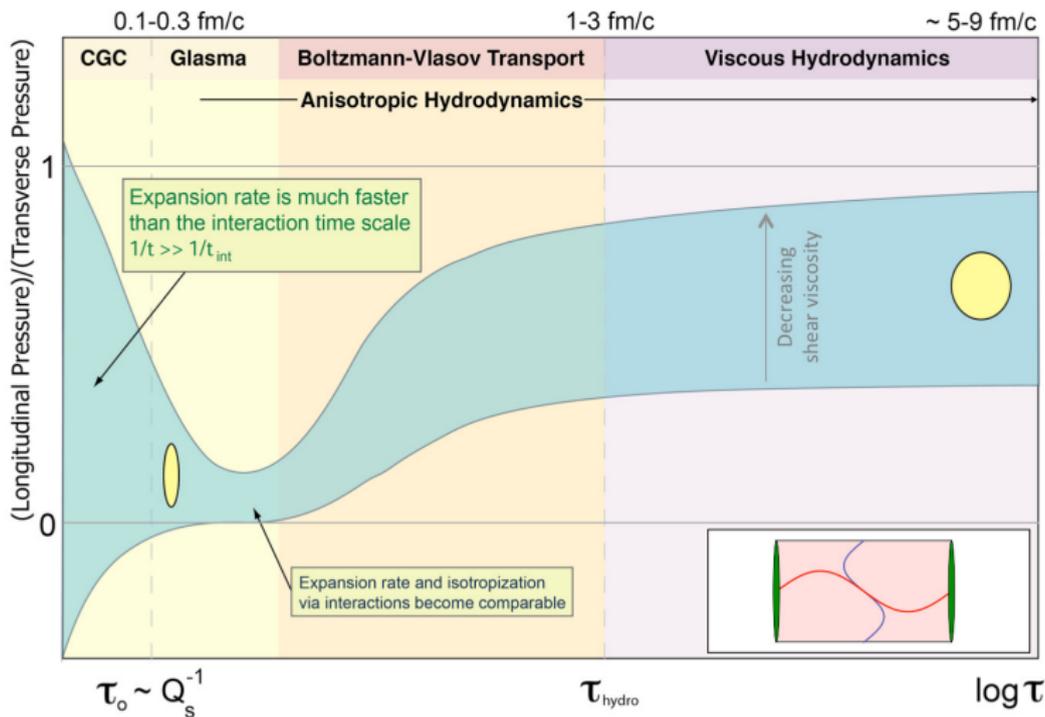


Stochastic Hydrodynamics

- **Hydrodyn. fluct.** is not a new idea, but their relativistic theory is: Kapusta, Müller, Stephanov, PRC 2012.
- **Hydrodyn. fluct.** arise due to finite particle no. fluct. in a given coarse-grained fluid cell. This leads to local thermal noise or fluct. in $\epsilon(x, y)$ and $\mathbf{v}(x, y)$. Effect is **intrinsic** to hydrodyn.
- **Fluctuation-Dissipation Theorem**: Viscosity controls the magnitude of hydro fluct. This provides another handle on η/s .
- $T^{\mu\nu} = T_{perfect}^{\mu\nu} + \Delta T^{\mu\nu} + S^{\mu\nu}$, $J^\mu = J_{perfect}^\mu + \Delta J^\mu + I^\mu$,
 $\partial_\mu T^{\mu\nu} = 0 = \partial_\mu J^\mu$: Stochastic (rather than deterministic) hydro.
- Are there any **observable** effects? Correlations across large $\Delta\eta$?

ANISOTROPIC HYDRODYNAMICS (aHydro)

Evolution of Pressure Anisotropy ... M. Strickland, 1410.5786



Yellow ellipses: shape of the momentum-space distribution with x -axis: longitudinal direction, y -axis: transverse direction.

Anisotropic Hydrodynamics (aHydro)

- Originally **proposed in 2010**: Florkowski and Ryblewski 1007.0130, Martinez and Strickland 1007.0889
- Very early times: sizable **pressure anisotropy** in LRF
- Sizable **momentum-space anisotropy** ($p_L^2 \ll p_T^2$) in parton $f(x, p)$
- Better to **reorganize** hydrodynamic expansion by taking into account large momentum anisotropy at leading order **non-perturbatively**, instead of as a **perturbative** correction to an isotropic $f(x, p)$
- This **extends applicability** of hydrodynamics to situations far from isotropic thermal equilibrium
- **Recent Progress** in aHydro: 1610.10055 and 1611.05056

Principal Component Analysis of Event-by-Event Fluctuations

RSB, Jean-Yves Ollitrault (Saclay), Subrata Pal (TIFR), Derek Teaney (Stony Brook), *PRL* 114 (2015) 152301

A New Flow Analysis Method (contd.)

Analysis of anisotropic flow v_n

- Methods currently in use (**event-plane, cumulants, ..**): devised before the importance of flow fluctuations was recognized
- **New method**: extraction of flow fluct. directly from data on 2-particle correls; uses **all** the information
- Based on Principal Component Analysis (**PCA**) — applied to the 2-particle correlation matrix, $\langle \cos n\Delta\phi \rangle$
- Leading eigenmode \longleftrightarrow usual v_2, v_3
Subleading modes of v_2, v_3 revealed for the 1st time

Other Recent Developments ...

- Critical Point search in RHIC Beam Energy Scan:
Overview [STAR, EPJ Web Conf. 95 \(2015\) 01009](#)
- Rel. Hydrodynamics \rightarrow Rel Magneto-hydrodynamics:
[F. Becattini et al, arXiv:1609.03042](#)
- Multi-dimensional parameter optimization program
that uses sophisticated Bayesian techniques:
[S.A. Bass et al, arXiv:1502.00339, 1605.03954](#)
- Alternative (non-fluid-dynamic) explanations of apparent
collectivity: [Discussion in arXiv:1604.03310](#)
- Heavy ions at the Future Circular Collider (FCC):
[CERN Yellow Report, arXiv:1605.01389](#)

Take-Home Message / Open Questions

- All data so far are consistent with the formation of **Quark-Gluon Plasma**, and we are in the midst of trying to determine its equilibrium and transport properties accurately.
- Data provide a strong support to hydrodynamics as the appropriate **effective theory** for rhics. But the **Standard Model** still incomplete.
- Dichotomy between **strong** and **weak** coupling descriptions of hot QCD matter.
- How does a **weakly-coupled** colour-glass condensate become a **strongly-coupled** fluid?
- Collectivity in **small** systems. Size of the smallest QCD droplet?
- **QCD Phase Diagram** still remains largely unknown. **Critical Point?**
- **LHC**: High luminosity era. **NICA**: Fixed target expt to start in 2017. **CBM@FAIR**: Data taking to start in 2022. **EIC?** So this exciting field is going to remain very active for a decade at least.

THANK YOU