

Onset of η -nuclear binding scenarios

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η nuclear quasibound states

E. Friedman, A. Gal, J. Mareš, PLB 725 (2013) 334

A. Cieplý plus FGM, NPA 925 (2014) 126

Review: A. Gal et al., Acta Phys. Polon. B 45 (2014) 673

Onset of η nuclear binding

N. Barnea, E. Friedman, A. Gal, PLB 747 (2015) 345

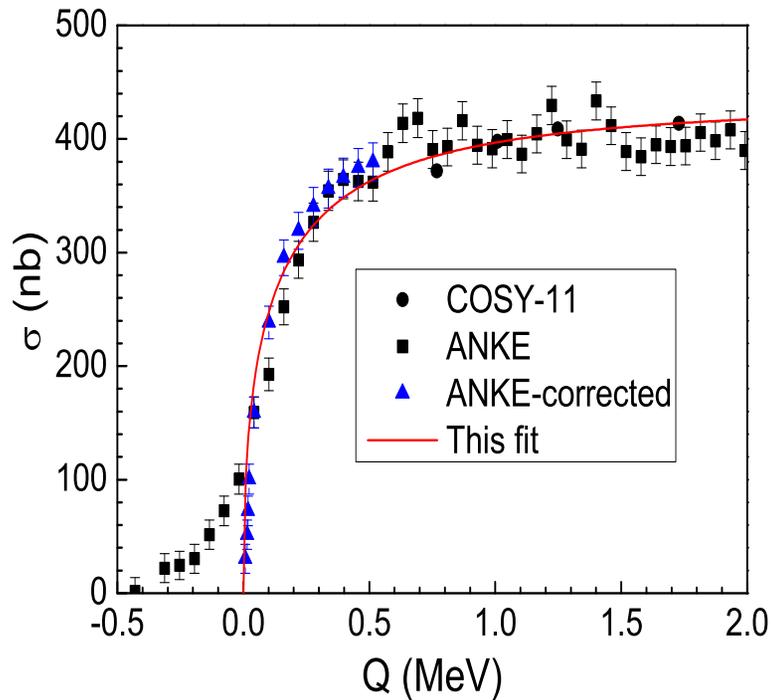
B. Bazak plus BFG, PLB (2017), arXiv:1703.02861

N. Barnea, E. Friedman, A. Gal, to be submitted

Background & Motivation

- The ηN s-wave interaction below $N^*(1535)$ is attractive in a $\pi N - \eta N$ model [Bhalelao–Liu (1985)]. Bound states of $\eta(548)$ in $A \geq 12$ nuclei could exist [Haider–Liu (1986)].
- Chiral $N^*(1535)$ meson-nucleon coupled channel models were introduced by Kaiser, Weise et al (1995-1997) and subsequently by Oset et al (2002). These & other models have been used to calculate η -nuclear quasibound states.
- Exp. searches for such states with proton, pion or photon induced η production reactions are inconclusive. Re the onset of binding, Krusche & Wilkin (2015) state:
“The most straightforward (but not unique) interpretation of the data is that the η d system is unbound, the $\eta^4\text{He}$ is bound, but that the $\eta^3\text{He}$ case is ambiguous.”

Hints from $\eta^3\text{He}$ production



Fitted $dp \rightarrow \eta^3\text{He}$ x-sections below 2 MeV vs. experiment. Remarkable energy dependence, suggesting a nearby S-matrix pole could be in action.

Deduced $a(\eta^3\text{He})$ excludes a quasibound state pole.

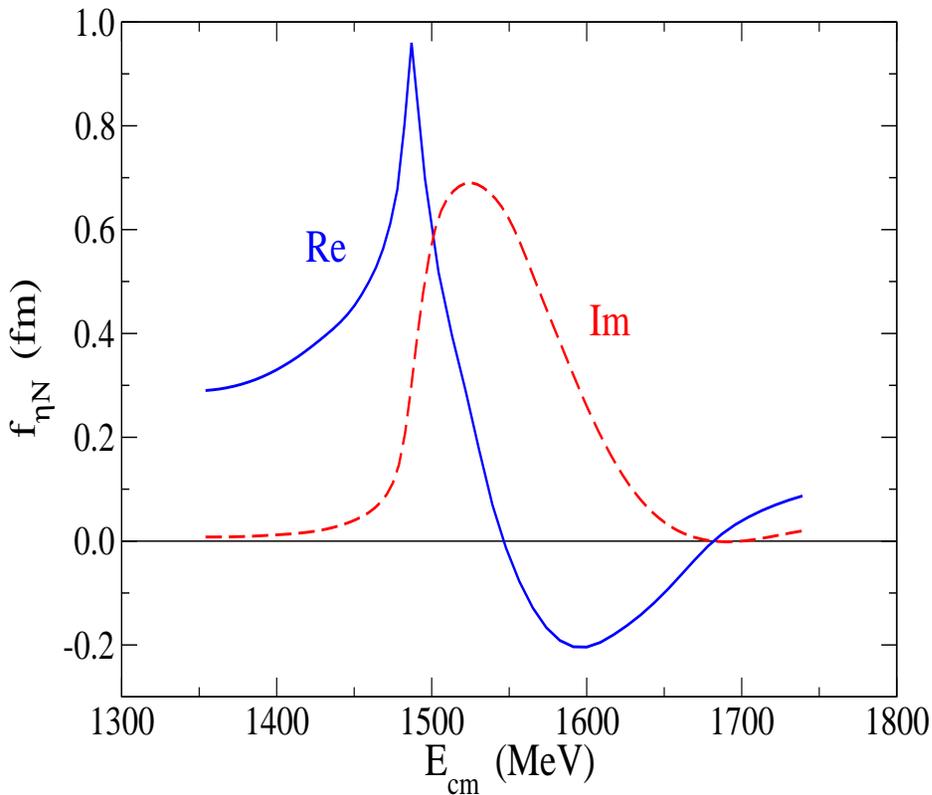
Xie-Liang-Oset-Moskal-Skurzok-Wilkin, PRC 95 (2017) 015202

$$a(\eta^3\text{He}) = [-(2.23 \pm 1.29) + i(4.89 \pm 0.57)] \text{ fm}$$

- Would $\eta^4\text{He}$ be bound? Fix & Kolesnikov (arXiv:1703.06591) argue: **NO**, since the denser ^4He medium leads to a stronger subthreshold suppression.

η nuclear quasibound states

$f_{\eta N}(\sqrt{s})$ from K -matrix & $N^*(1535)$ chiral models



$a_{\eta N}$ (fm) model dependence

a	M1	M2	GW	GR	CS
Re	0.22	0.38	0.96	0.26	0.67
Im	0.24	0.20	0.26	0.24	0.20

Mai et al. PRD 86 (2012) 094033

Green-Wycech PRC 71 (2005) 014001

Garcia-Recio et al. PLB 550 (2002) 47

Cieply-Smejkal, NPA 919 (2013) 46

- Re $a_{\eta N}$ varies from 0.2 to 1.0 fm, **Im $a_{\eta N}$: 0.2–0.3 fm.**
- M1, M2, GW free-space models; GR, CS in-medium.
- **Strong subthreshold fall-off in both Re $f_{\eta N}$ and Im $f_{\eta N}$.**
- In-medium: E dependence, Pauli blocking, self energies.

Self-consistency in mesic-atom & nuclear calculations

Cieplý-Friedman-Gal-Gazda-Mareš, PLB 702 (2011) 402

$$s = (\sqrt{s_{\text{th}}} - B_\eta - B_N)^2 - (\vec{p}_\eta + \vec{p}_N)^2 < s_{\text{th}}$$

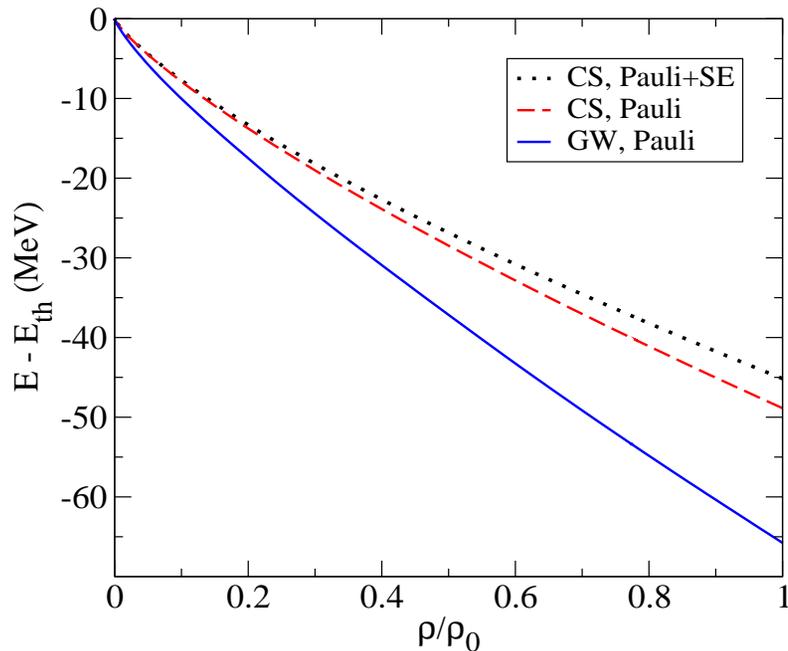
$$\sqrt{s_{\eta N}} \rightarrow E_{\text{th}} - B_N - B_\eta - \xi_N \frac{p_N^2}{2m_N} - \xi_\eta \frac{p_\eta^2}{2m_\eta}$$

$$\xi_{N(\eta)} = \frac{m_{N(\eta)}}{(m_N + m_\eta)} \quad \frac{p_\eta^2}{2m_\eta} \sim -V_\eta - B_\eta$$

η is not at rest!

$E_{\eta N}$ subthreshold shift vs. nuclear density in $1s_\eta$ ^{40}Ca .

A dominant in-medium effect.



Cieplý-Friedman-Gal-Mareš, NPA 925 (2014) 126

In-medium ηN amplitudes

Friedman-Gal-Mareš, PLB 725 (2013) 334

Cieplý-Friedman-Gal-Mareš, NPA 925 (2014) 126

- KG equation and self-energies:

$$[\nabla^2 + \tilde{\omega}_\eta^2 - m_\eta^2 - \Pi_\eta(\omega_\eta, \rho)] \psi = 0$$

$$\tilde{\omega}_\eta = \omega_\eta - i\Gamma_\eta/2, \quad \omega_\eta = m_\eta - B_\eta$$

$$\Pi_\eta(\omega_\eta, \rho) \equiv 2\omega_\eta V_\eta = -4\pi \frac{\sqrt{s}}{m_N} f_{\eta N}(\sqrt{s}, \rho) \rho$$

- Pauli blocking (Waas-Rho-Weise NPA 617 (1997) 449):

$$f_{\eta N}^{\text{WRW}}(\sqrt{s}, \rho) = \frac{f_{\eta N}(\sqrt{s})}{1 + \xi(\rho)(\sqrt{s}/m_N)f_{\eta N}(\sqrt{s})\rho}, \quad \xi(\rho) = \frac{9\pi}{4p_F^2} I(\kappa)$$

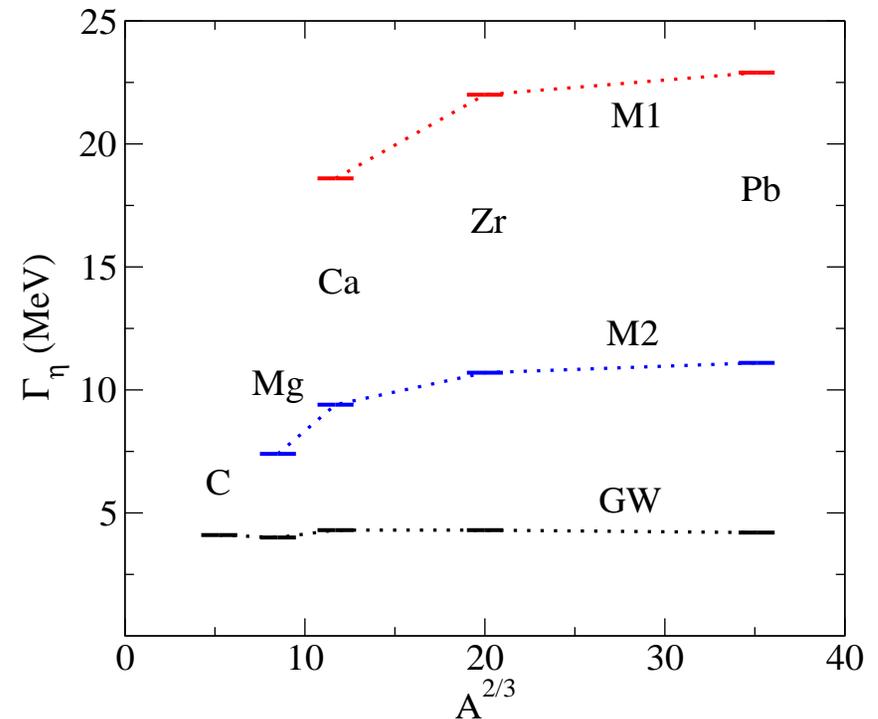
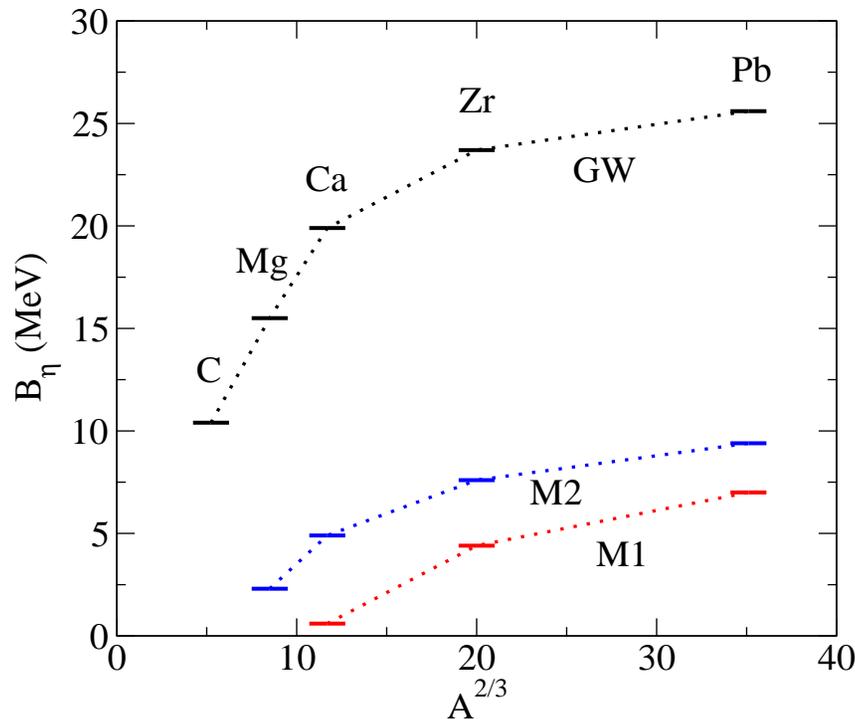
- $N^*(1535) \Rightarrow$ energy dependent $f_{\eta N}(\sqrt{s})$.

$$\text{In medium} \Rightarrow \text{go subthreshold: } \delta\sqrt{s} = \sqrt{s} - \sqrt{s_{\text{th}}}$$

$$\delta\sqrt{s} \approx -B_N \frac{\rho}{\rho} - \xi_N B_\eta \frac{\rho}{\rho_0} - \xi_N T_N \left(\frac{\rho}{\rho}\right)^{2/3} + \xi_\eta \text{Re } V_\eta(\sqrt{s}, \rho)$$

Self-consistency relationship between $\delta\sqrt{s}$ & ρ

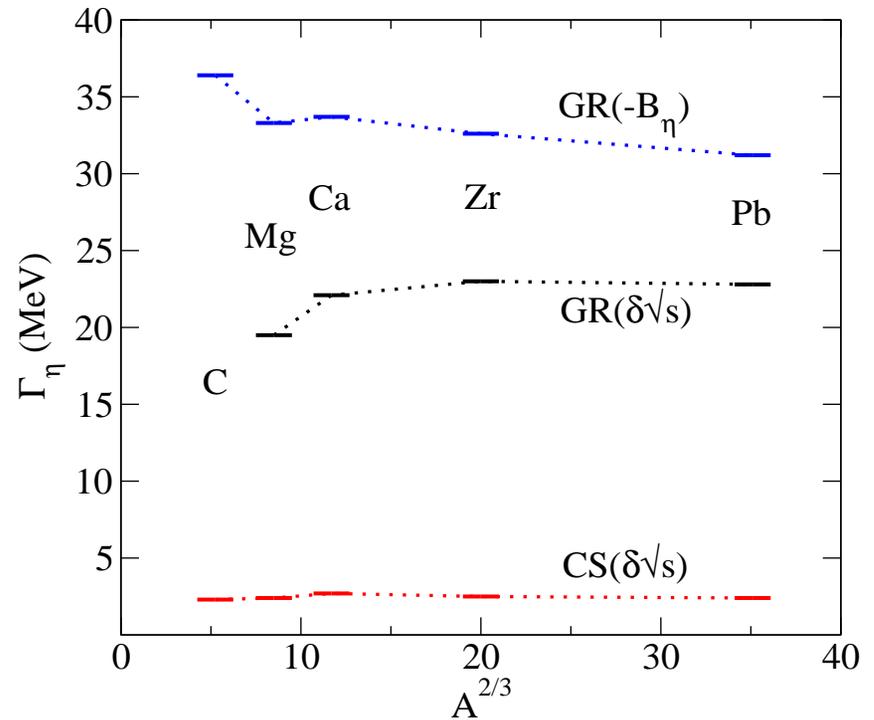
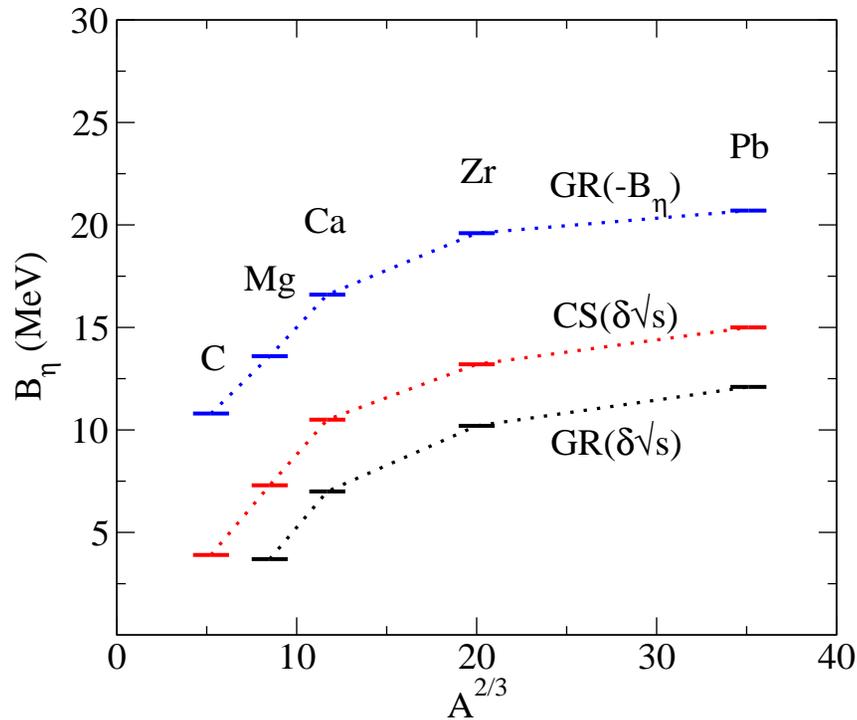
Model dependence I



$1s_\eta$ B & Γ using WRW Pauli-blocked $f_{\eta N}$

- **E dependence treated self consistently.**
- Larger $\text{Re } a_{\eta N} \Rightarrow$ larger B_η .
- Widths are unrelated to $\text{Im } a_{\eta N}$.

Model dependence II

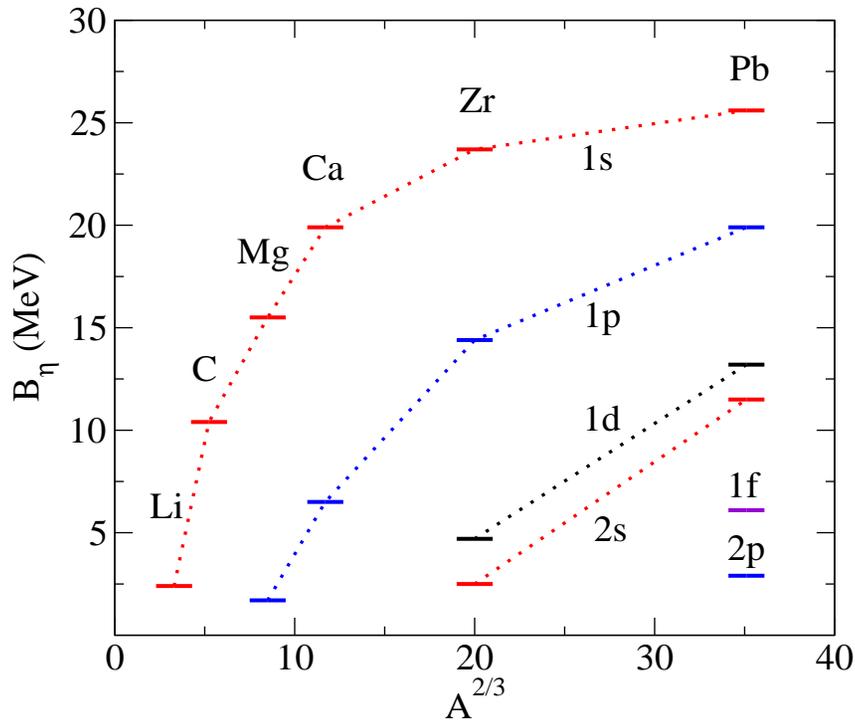


Sensitivity of calc. $B_{1s_{\eta}}$ & $\Gamma_{1s_{\eta}}$ to self-consistency version

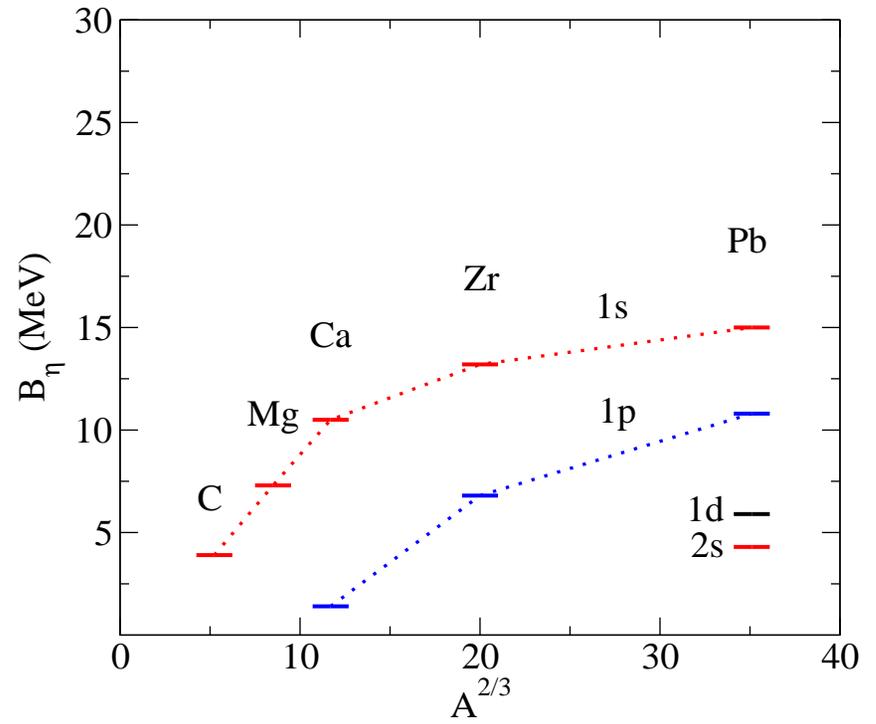
- $\langle \delta\sqrt{s} \rangle$ goes deeper into subthreshold, thereby reducing further $B_{1s_{\eta}}$ & $\Gamma_{1s_{\eta}}$.
- GR's widths are too large to resolve η bound states.

Why $\Gamma_{\eta}(\text{GR}) \gg \Gamma_{\eta}(\text{CS})$ for similar $\text{Im } a_{\eta N}$?

Model predictions for small widths



GW model

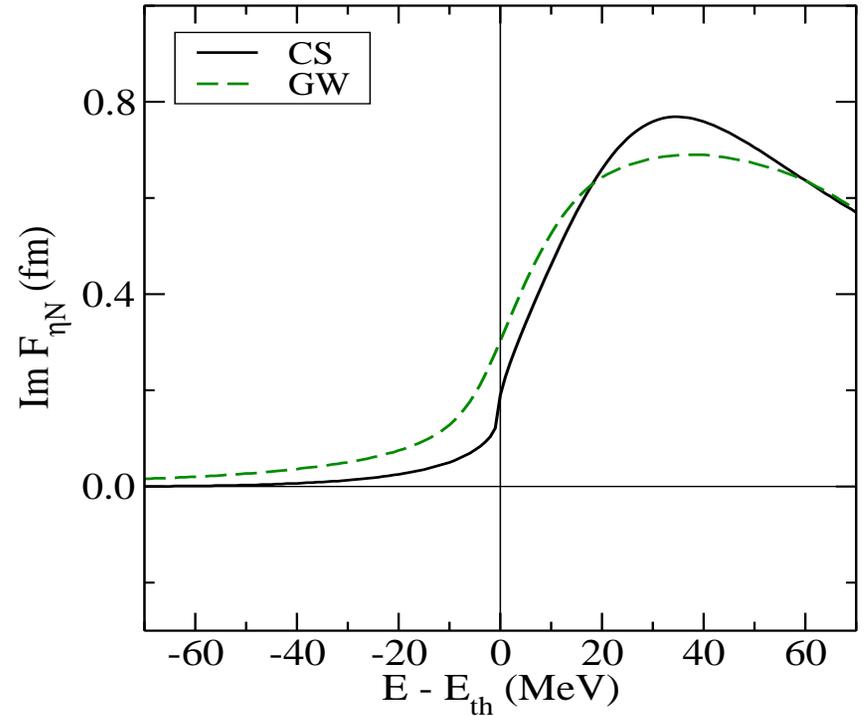
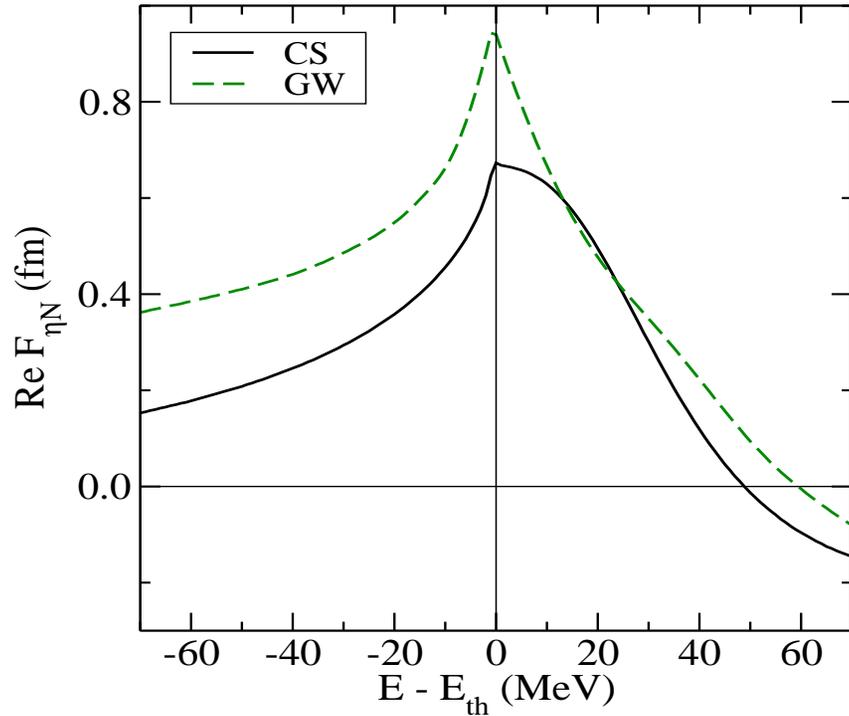


CS model

- Widths of only a few MeV in each of these models.
- What makes the subthreshold values of $\text{Im } f_{\eta N}$ sufficiently small to generate small widths?

Onset of η nuclear binding

ηN model input

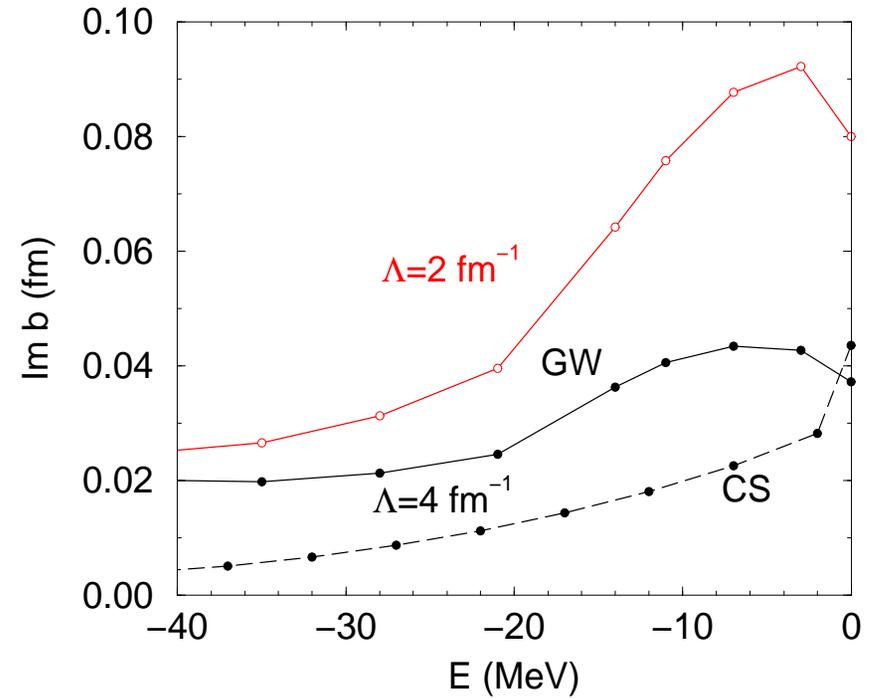
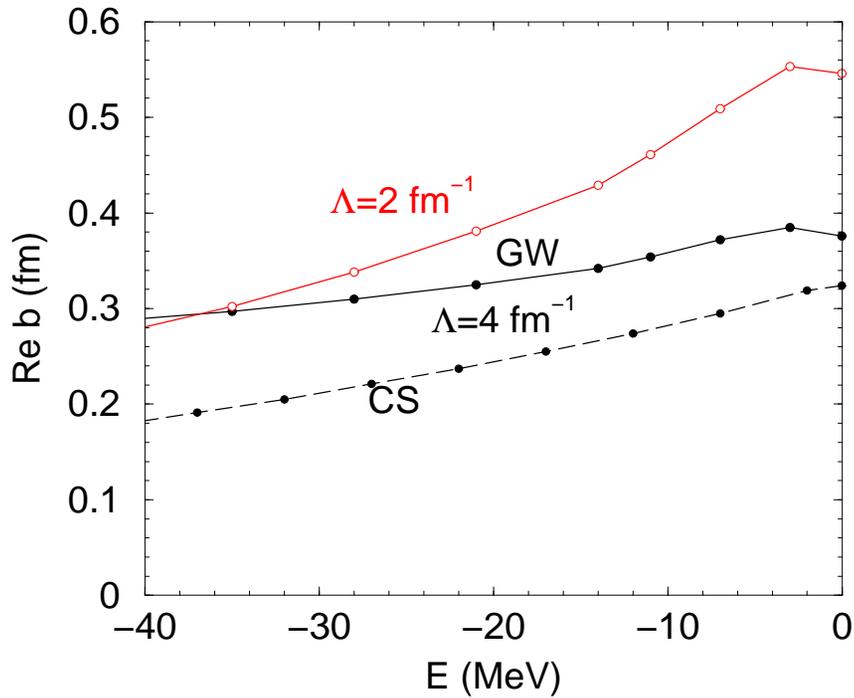


CM s-wave scattering amplitude $F_{\eta N}(E)$ in two meson-baryon coupled-channel $N^*(1535)$ models.

$$\mathbf{a_{\eta N}^{GW} = 0.96 + i0.26 \text{ fm}, \quad a_{\eta N}^{CS} = 0.67 + i0.20 \text{ fm}}$$

- Derive local, energy dependent potentials $v_{\eta N}(E; r)$ that reproduce $F_{\eta N}(E)$ below threshold, for use in solving the ηNN , ηNNN , $\eta NNNN$ few-body Schroedinger equations.

$F_{\eta N}(\mathbf{E}) \Rightarrow v_{\eta N}(\mathbf{E})$ in models GW & CS



Strength $b(E)$ of effective potential $v_{\eta N}(\mathbf{E})$ at $E < 0$

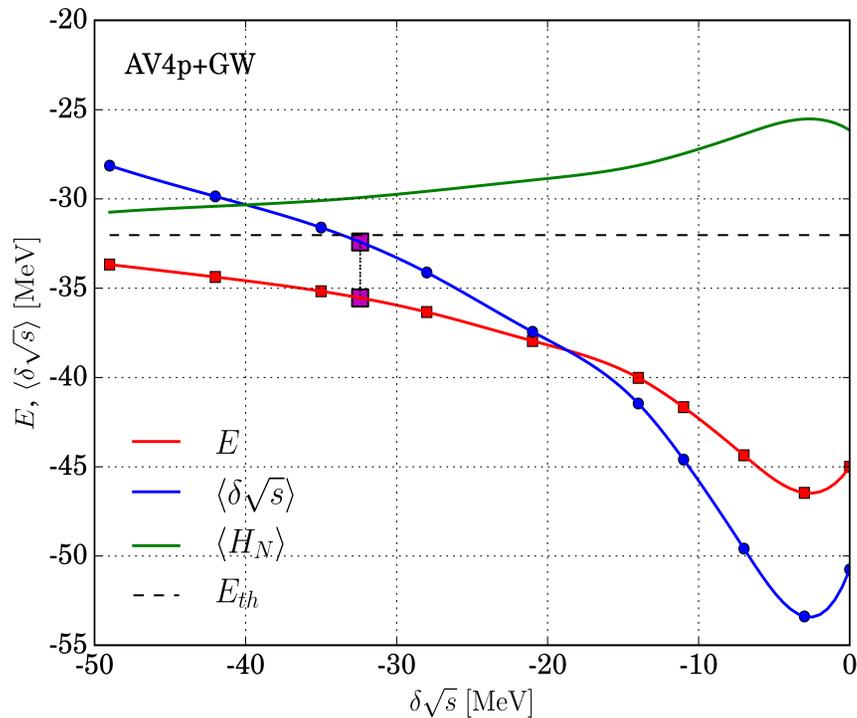
$$v_{\eta N}(\mathbf{E}; \mathbf{r}) = -\frac{4\pi}{2\mu_{\eta N}} b(\mathbf{E}) \left(\frac{\Lambda}{2\sqrt{\pi}} \right)^3 \exp\left(-\frac{\Lambda^2 r^2}{4}\right)$$

- Scale Λ is inversely proportional to the range of $v_{\eta N}$.
- In pionless EFT, vector-meson exchange requires $\Lambda \leq 4 \text{ fm}^{-1}$.

Energy dependence in η nuclear few-body systems

- $N^*(1535)$ induces strong energy dependence of the scattering amplitudes $f_{\eta N}(\sqrt{s})$ and the effective input potentials $v_{\eta N}(\sqrt{s})$.
- $s = (\sqrt{s_{\text{th}}} - B_\eta - B_N)^2 - (\vec{p}_\eta + \vec{p}_N)^2 < s_{\text{th}}$
- Expanding nonrelativistically near $\sqrt{s_{\text{th}}}$:
$$\langle \delta\sqrt{s} \rangle = -\frac{B}{A} + \frac{A-1}{A} E_\eta - \xi_N \frac{1}{A} \langle T_N \rangle - \xi_\eta \left(\frac{A-1}{A}\right)^2 \langle T_\eta \rangle,$$
$$\delta\sqrt{s} \equiv \sqrt{s} - \sqrt{s_{\text{th}}}, \quad E_\eta = \langle H - H_N \rangle, \quad \xi_{N(\eta)} \equiv \frac{m_{N(\eta)}}{(m_N + m_\eta)}.$$
- Self-consistency:
output $\langle \sqrt{s} \rangle = \text{input } \sqrt{s}$.

Recent SVM results for $\eta^{3,4}\text{He}$

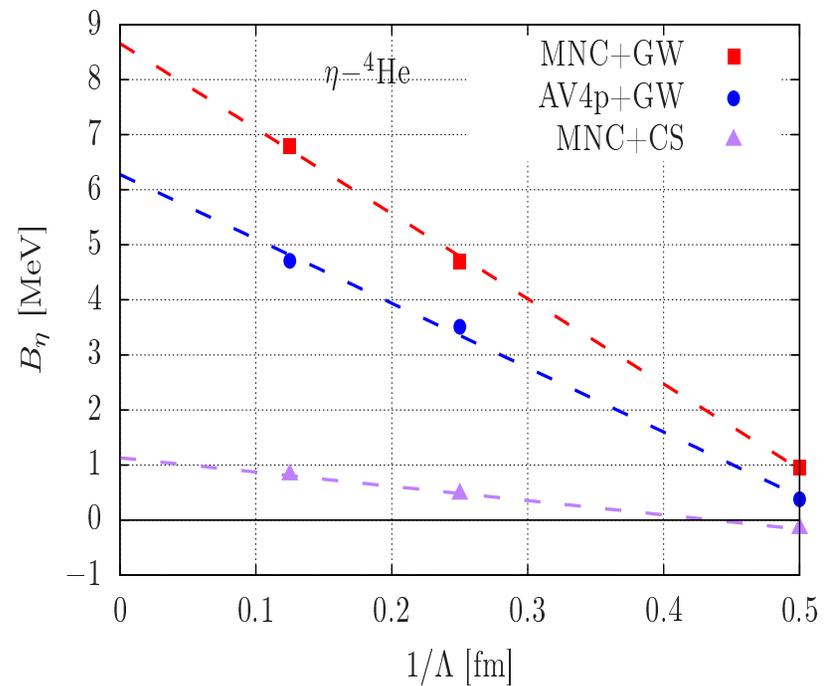
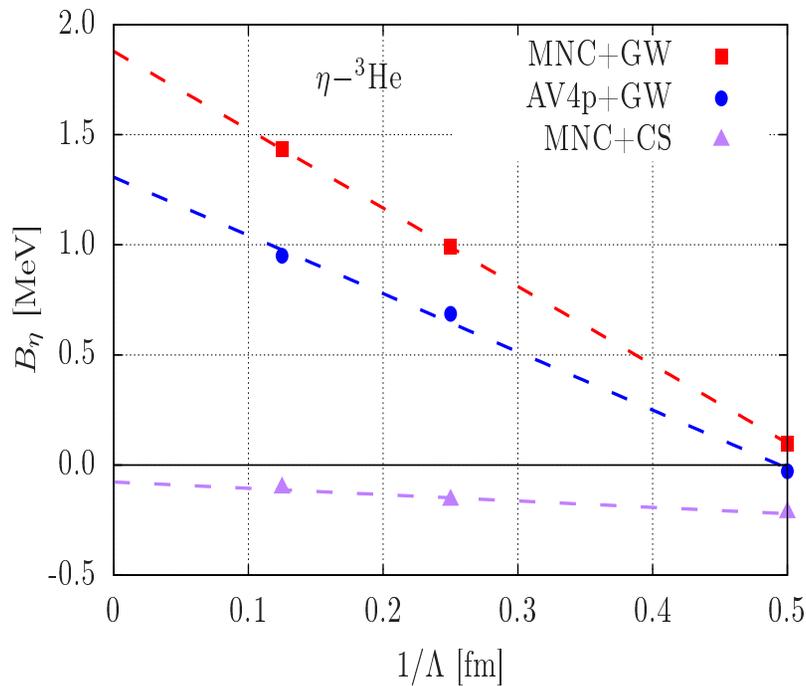


Self consistency plot

$\eta^4\text{He}$ bound-state energy E , $\langle\delta\sqrt{s}\rangle$ & $\langle H_N \rangle$, for AV4' v_{NN} & GW $v_{\eta N}(E)$ with scale $\Lambda=4 \text{ fm}^{-1}$.

- **Stochastic Variational Method** calculations with correlated Gaussian trial wavefunctions.
- η d is definitely unbound in both GW and CS (2015).
- $\eta^3\text{He}$ is nearly or just bound in GW & unbound in CS.
- $\eta^4\text{He}$ is bound in GW and just or nearly bound in CS.

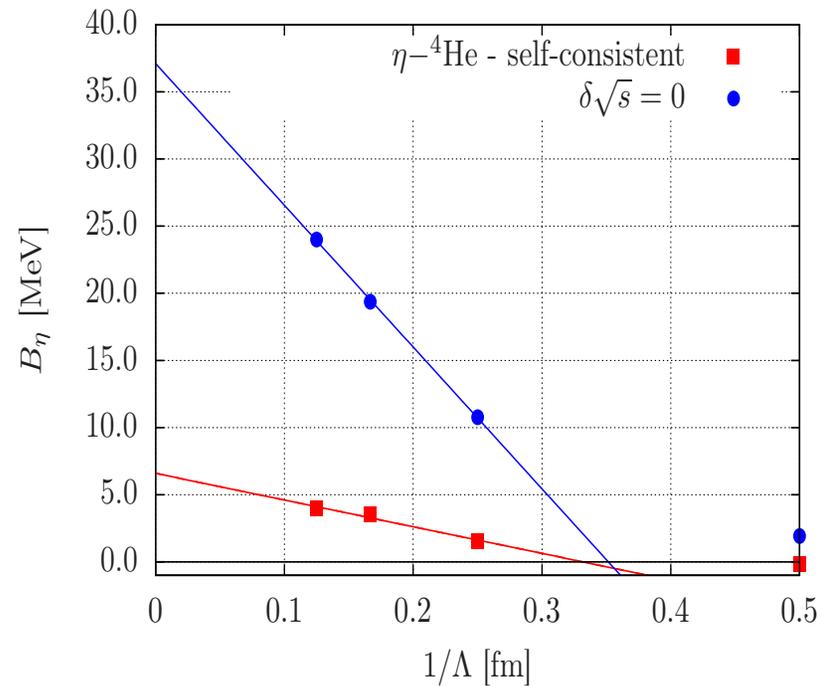
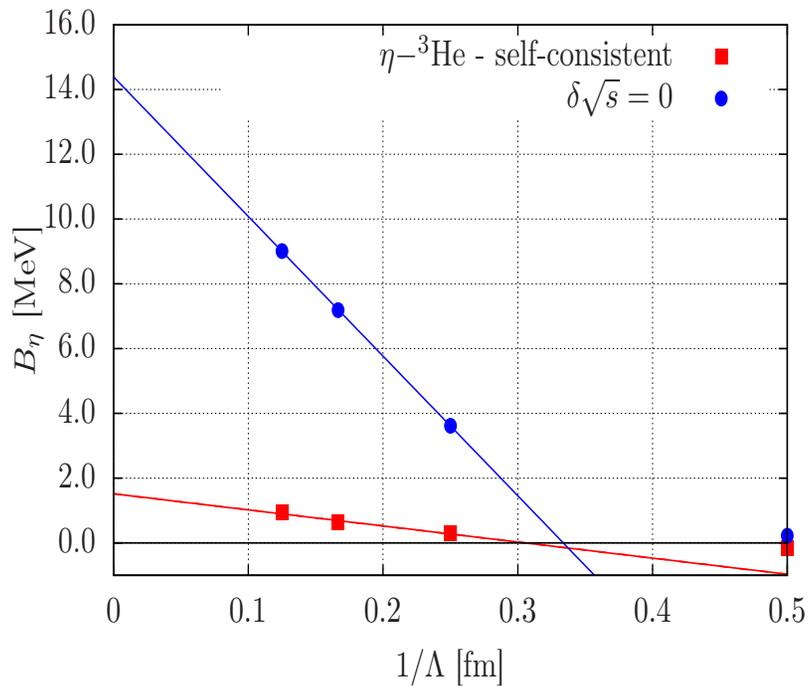
Scale dependence; semi-realistic NN



B_η as a function of $1/\Lambda$

- These bindings will decrease by ≤ 0.3 MeV when Im v is treated nonperturbatively.
- AV4' is more realistic for NN than Minnesota (MNC).
- CS does not bind $\eta^3\text{He}$ & unlikely to bind $\eta^4\text{He}$.

Scale dependence; pionless EFT



B_η as a function of $1/\Lambda$

- Two NN & one NNN contact terms at LO.
Add **one** ηN contact term ($\sim b(E)$).
- No ηNN contact term needed to avert collapse.
- Crucial role of **self consistency** in reducing η binding.

Summary

- Subthreshold behavior of $f_{\eta N}$ is crucial in studies of η -nuclear bound states to decide whether (i) such states exist, (ii) can they be resolved (i.e. widths), and (iii) which nuclear targets and reactions to try.
- The onset of binding $\eta^3\text{He}$ requires a minimal value of $\text{Re } a_{\eta N}$ close to 1 fm, yielding then a few MeV η binding in $\eta^4\text{He}$. The onset of binding $\eta^4\text{He}$ requires a lower value of $\text{Re } a_{\eta N}$, roughly exceeding 0.7 fm.

Thanks to my collaborators N. Barnea, B. Bazak, A. Cieplý, E. Friedman, J. Mareš