

# $3\gamma$ tomography with J-PET

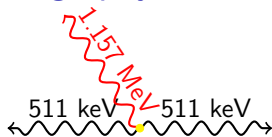
Daria Kisielewska  
on behalf of the J-PET Collaboration

2<sup>nd</sup> Jagiellonian Symposium of Fundamental and Applied Subatomic Physics

8 June 2017  
Kraków



## $3\gamma$ tomography

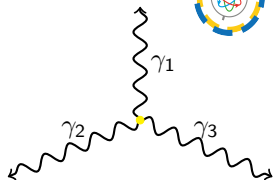


### $e^+e^-$ annihilation with additional photon from $\beta^+$ emitter deexcitation

- 2 annihilation photons are created back-to-back
- deexcitation photon momentum is independent
- the additional photon is used to increase imaging resolution



# J-PET



### Ortho-positronium tomography with $o\text{-Ps} \rightarrow 3\gamma$ annihilation

- momenta of three photons created in  $o\text{-Ps}$  decay are co-planar
- ortho-positronium ( $o\text{-Ps}$ ) lifetime in tissue strongly depends on inter-cellular spaces' size
- morphological imaging possible through determination of  $o\text{-Ps}$  lifetime<sup>1</sup>

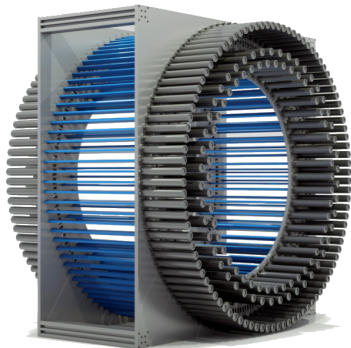
Material	No Ps formed <sup>2</sup>	Water <sup>2</sup>	IC3100 <sup>3</sup>	XAD-4 <sup>3</sup>
$f_{3\gamma} = \sigma_{3\gamma}/\sigma_{2\gamma}$	0.27%	0.52%	16.9%	28.9 %

<sup>1</sup> A. Gajos, E. Czerwiński, D. Kamińska, P. Moskal, patent PCT/PL2015/050038

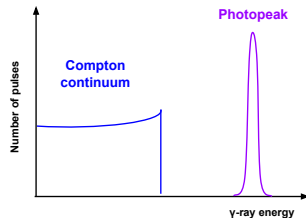
<sup>2</sup> K. Merkurio *et al.*, Phys. Med. Biol. **51**, N323 (2006)

<sup>3</sup> B. Jasińska *et al.*, Acta Phys. Polon. B **47**, 453 (2016)

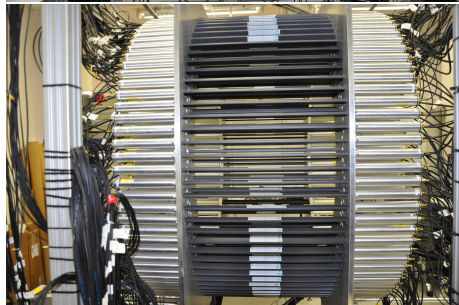
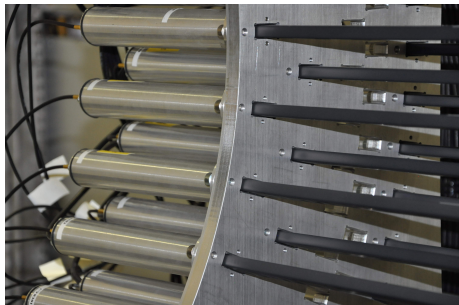
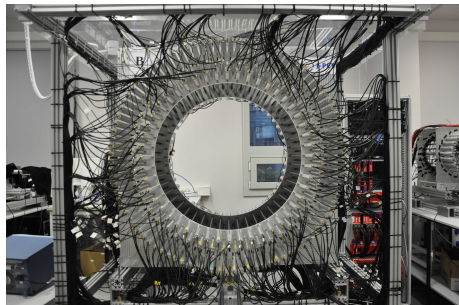
# J-PET detector



For a details see a talk by  
Sz. Niedźwiecki at Applied  
physics: Medical  
Applications, Monday

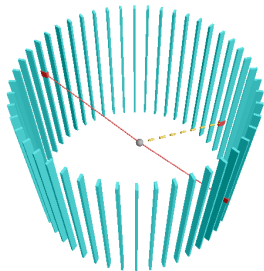


J-PET	Standard PET
Polymers	Crystals
Low granularity	High granularity
Low efficiency	High efficiency
High acceptance	Low acceptance
Compton scattering	Photoeffect
Time domain	Energy domain
Digital electronics	Analog electronics

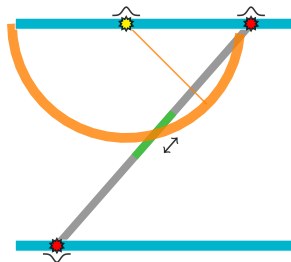
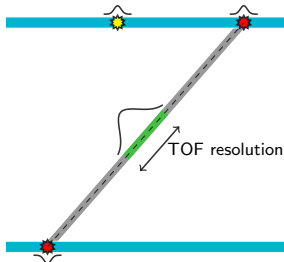
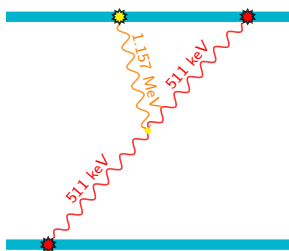




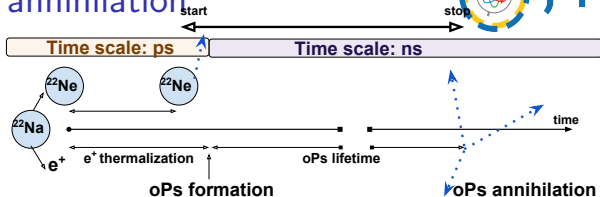
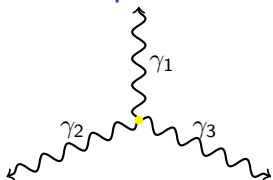
## $3\gamma$ -PET technique with the J-PET detector



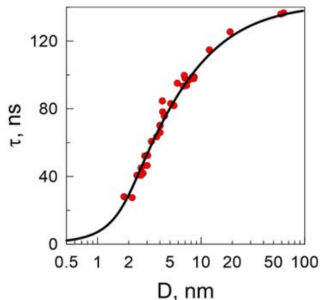
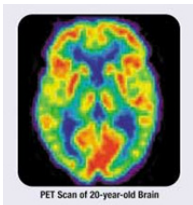
- Large acceptance offered by the J-PET apparatus allows for simultaneous recording of both annihilation photons as well as the deexcitation photon
- PET imaging resolution strongly depends on TOF resolution along the line of response (LOR)
- Information on the deexcitation photon can be used to improve resolution along LOR



# Ortho-positronium annihilation



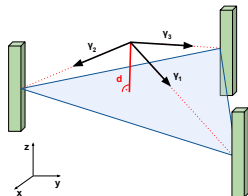
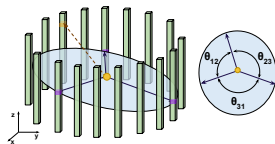
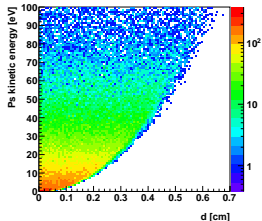
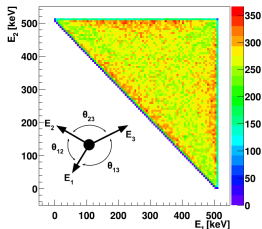
- Ortho-positronium (o-Ps) lifetime in tissue strongly depends on inter-cellular spaces' size
- The detection of  $3\gamma$  annihilation photons carries information about the environment with which the positron interacts
- Morphological imaging possible through determination of o-Ps lifetime



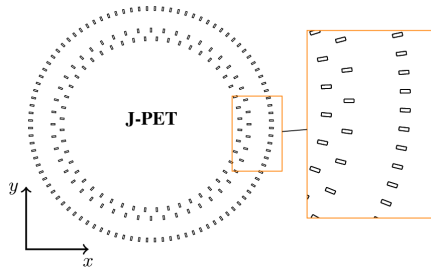
Comparison between o-Ps lifetime ( $\tau$ ) and a diameter of free volume ( $D$ ). Solid line and red points shows theoretical prediction and experimental data, respectively. Figure is adapted from *R. Zaleski, Nukleonika* **60** 795 (2015)

# Simulations

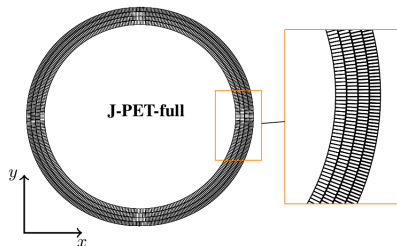
- i) positron emission and thermalisation in the target material,
- ii) angular and energy distributions of gamma quanta originating from ortho-positronium annihilation,
- iii) Compton interactions of emitted gamma quanta in the detector built from plastic scintillators,
- iv) determination of gamma quanta hit-position and hit-time in the detector with experimentally determined resolutions,
- v) multiple scattering and accidental coincidences,
- vi) reconstruction of registered gamma quanta fourmomenta



# Simulations

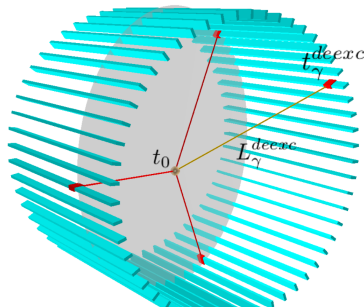


↑ Geometry already build and tested



↑ Simulated geometry

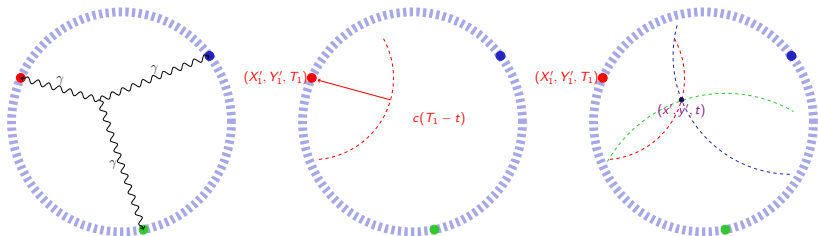
- momenta of the  $3\gamma$  from o-Ps decay are contained within a single plane (in the o-Ps ref. frame)
- 4-th (deexcitation) photon momentum is not correlated with the other three
- o-Ps  $\rightarrow 3\gamma$  decay and deexcitation photon emission differ by distance and time related to free  $e^+$  path and positronium life







# Principle of o-Ps $\rightarrow 3\gamma$ reconstruction



A. Gajos et al. (*J-PET*) NIM **A819**, 54 (2016)

- 1 Find the decay plane containing the 3 hits in the J-PET barrel
- 2 Transform the hit coordinates to a 2D coordinate system in the decay plane  
 $(X_i, Y_i, Z_i, T_i) \rightarrow (X'_i, Y'_i, 0, T'_i)$
- 3 For each of the recorded  $\gamma$  hits define a circle of possible origin points of the incident photon assuming o-Ps decay at time  $t$
- 4 Find the decay point  $(x', y')$  in the decay plane and time  $t$  as an intersection of 3 circles by solving the following equation system:

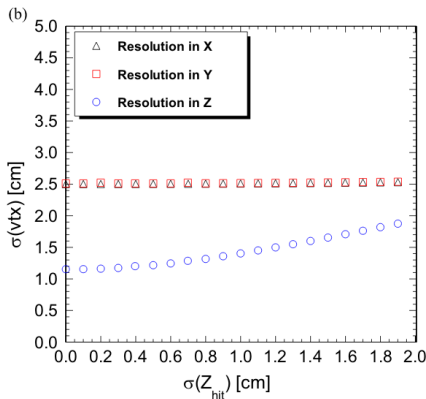
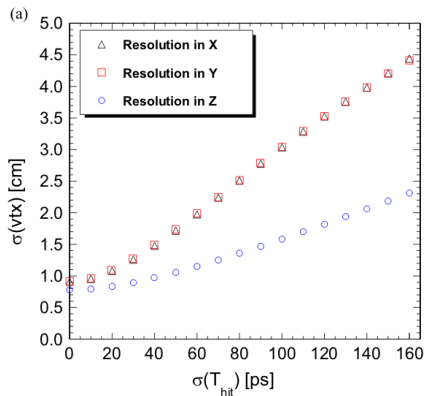
$$(T_i - t)^2 c^2 = (X'_i - x')^2 + (Y'_i - y')^2, \quad i = 1, 2, 3$$

where:  $x', y', t$  - unknowns,  $T_i$  - time of  $i$ -th hit,  $X'_i, Y'_i$  - coordinates of the  $i$ -th hit in the barrel expressed in the decay plane coordinates

- 5 Transform  $(x', y', t)$  of the decay point back to the detector 3D coordinate system

Spatial and time resolution of  $\alpha$ -Ps decay point

The resolution of  $\alpha$ -Ps decay obtained with the presented reconstruction method depends predominantly on the timing resolution of  $\gamma$  hits in scintillator strips.



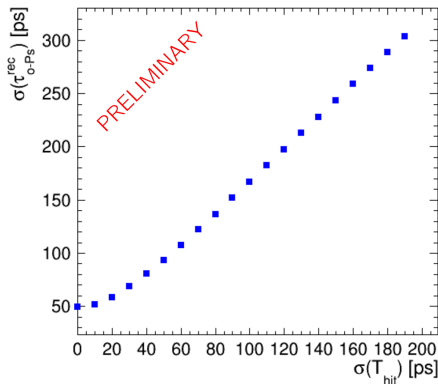
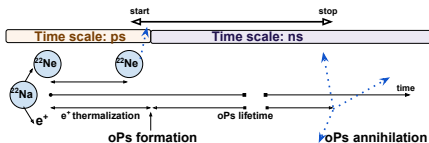
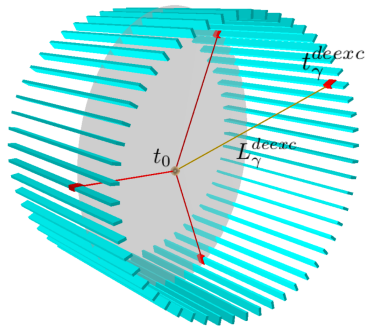


# Ortho-positronium lifetime resolution

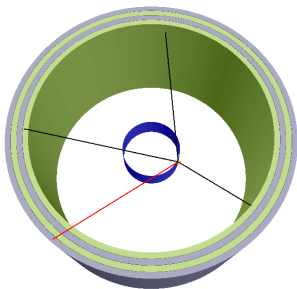
The ortho-positronium lifetime can be estimated as:

$$t_{\text{o-Ps}}^{\text{rec}} = t_0 - \left( t_{\gamma}^{\text{deexc.}} - \frac{L_{\gamma}^{\text{deexc.}}}{c} \right)$$

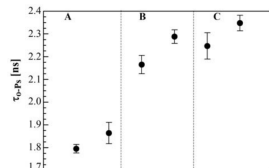
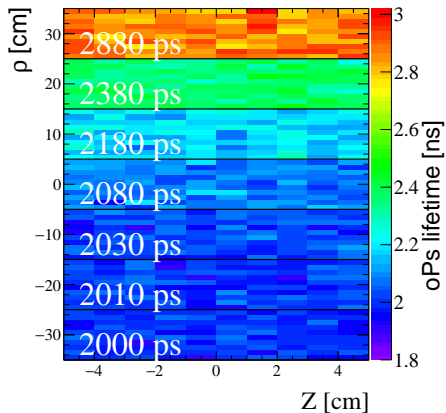
- $t_0$  - reconstructed o-Ps decay time
- $L_{\gamma}^{\text{deexc.}}$  - is calculated using reconstructed o-Ps decay point



# Morphological imaging

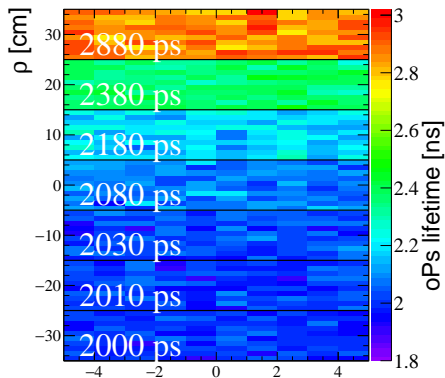
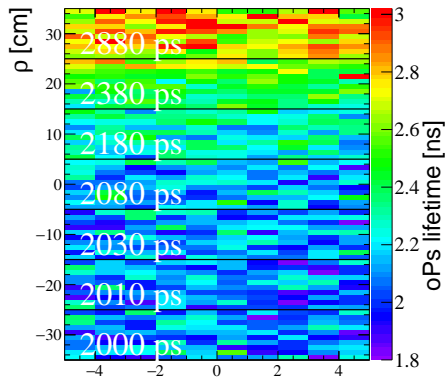


- cylindrically shaped  $\beta^+$  emitter is localized in the center of the detector
- radioactive source is uniformly distributed along the cylinder
- ortho-positronium lifetime changes with the azimuthal angle
- values of oPs lifetime in plasma or hematocrits is within range 1.7-2.4 ns



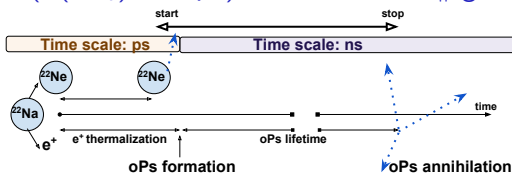


# Morphological imaging



↑ reconstructed ( $\sigma(T_{hit}) = 60ps$ )

↑ generated





## Summary

- The J-PET detector can be used for multi-photon positron emission tomography imaging
- The standard TOF-PET spatial resolution can be improved by using information from de-excitation photon
- A novel imaging technique based on ortho-positronium annihilation into three-photons is based on the fact that the properties of ortho-positronium atom depend strongly on the size of the free volumes between molecules
- The latter technique may be used as an indicator of the stage of development of metabolic disorders

**Thank you for your attention**