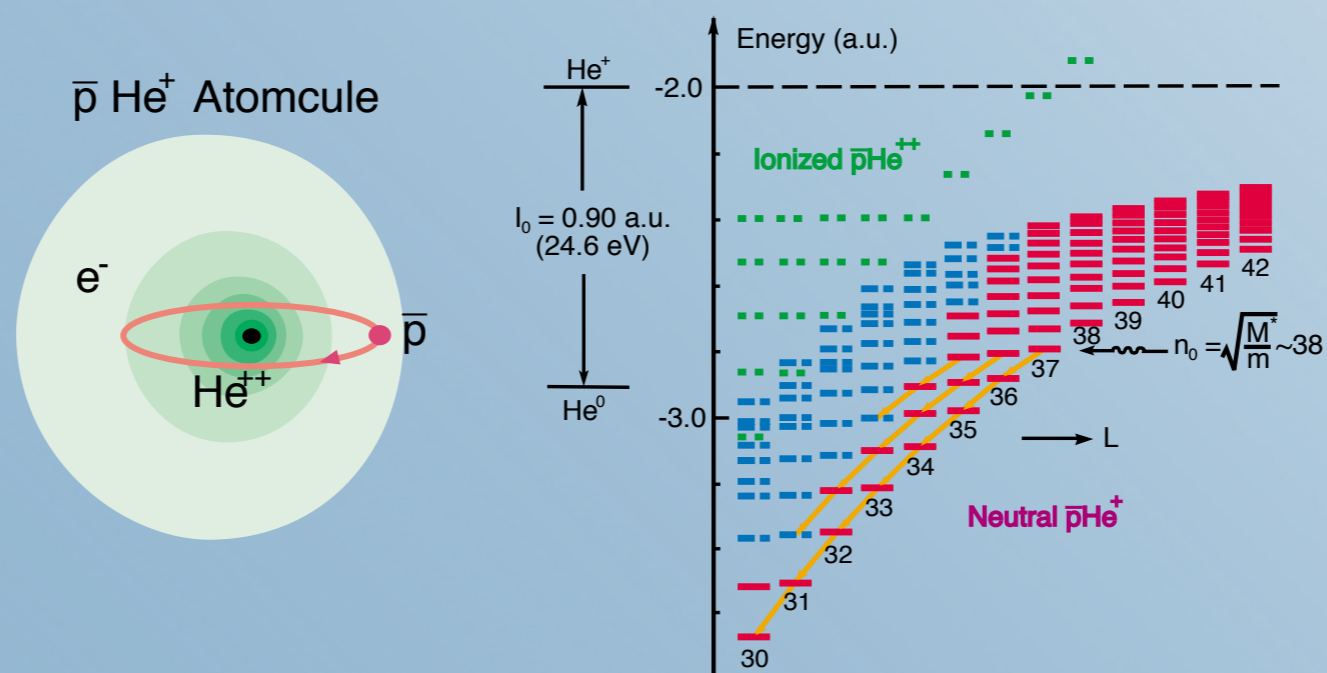




Physics of ASACUSA

the spectroscopy of antiprotonic helium



Ryugo Hayano  THE UNIVERSITY OF TOKYO

7-Oct-97

CERN/SPSC 97-19

CERN/SPSC P-307



ATOMIC SPECTROSCOPY AND COLLISIONS USING SLOW ANTIPROTONS

ASACUSA Collaboration

\bar{p} He spectroscopy: outline

What is it?

What is it good for?

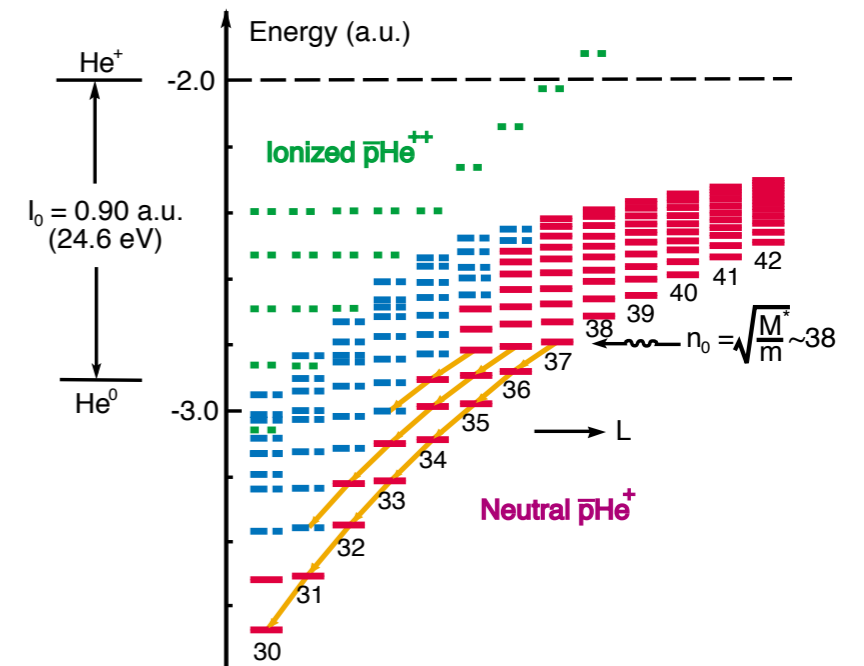
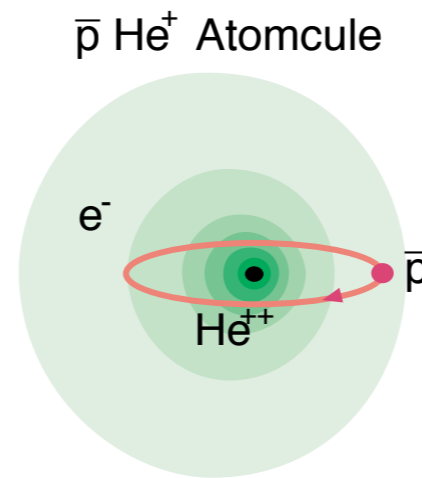
Laser spectroscopy principles

Theory

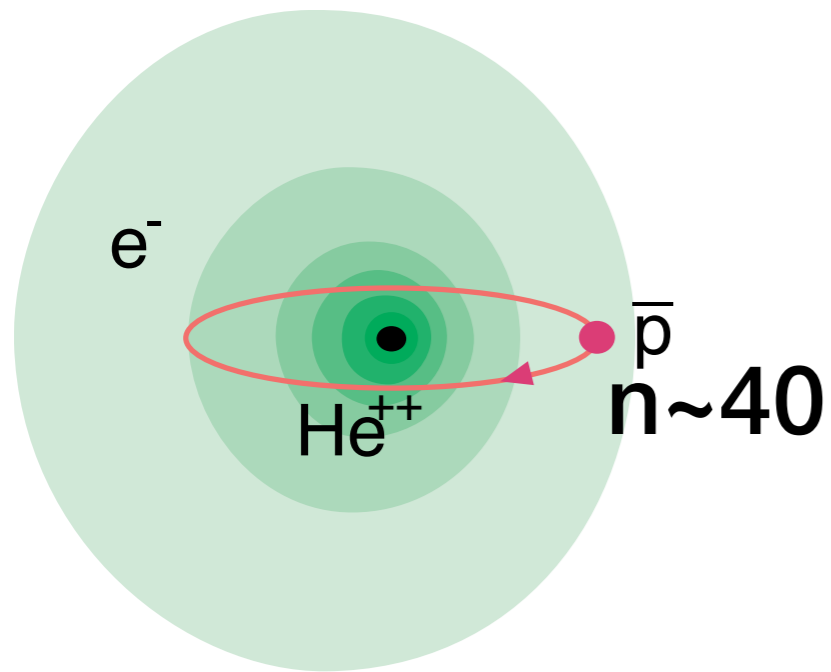
How to reach high precision?

Present status

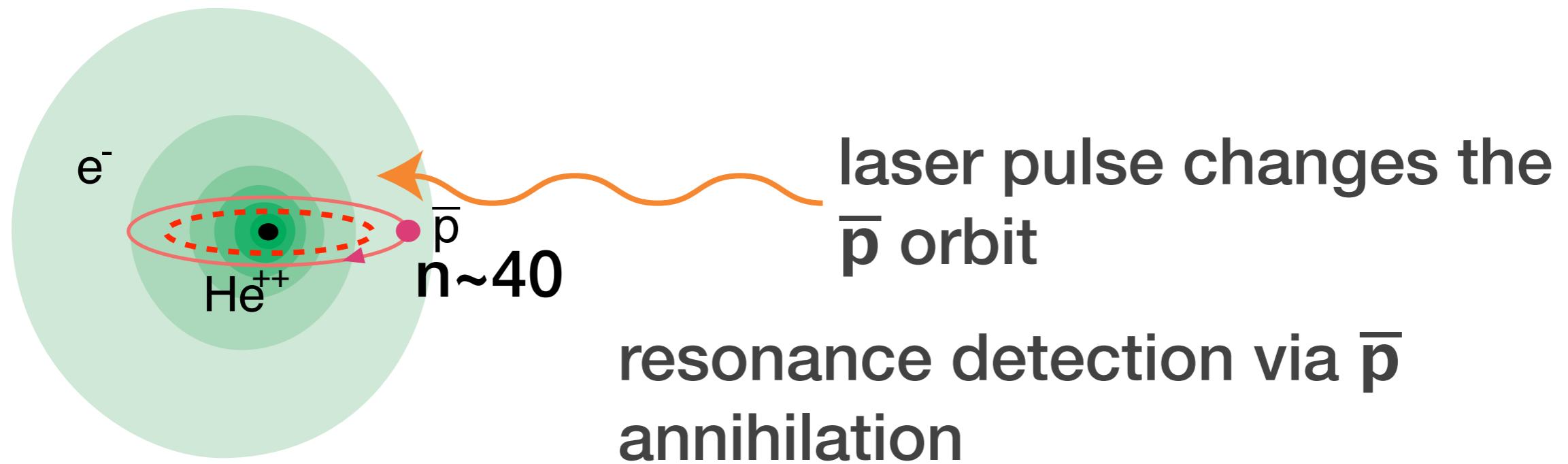
What to expect with ELENA?



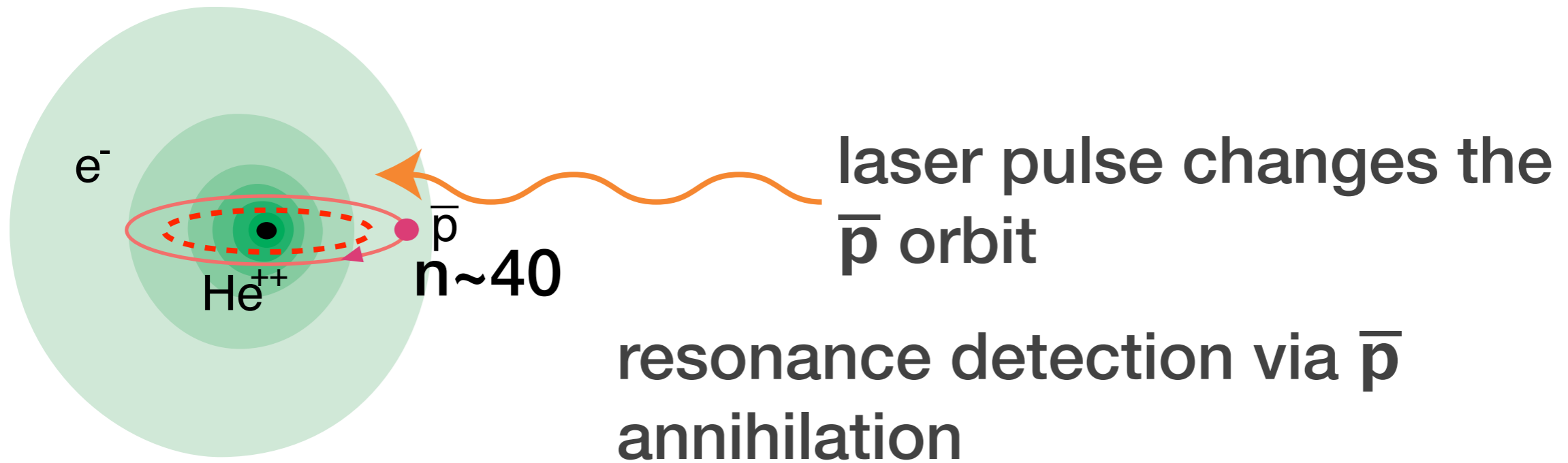
$\bar{p}\text{He}$ spectroscopy $\rightarrow m_{\bar{p}}/m_e$



\bar{p} He spectroscopy $\rightarrow m_{\bar{p}}/m_e$



\bar{p} He spectroscopy $\rightarrow m_{\bar{p}}/m_e$



Frequency

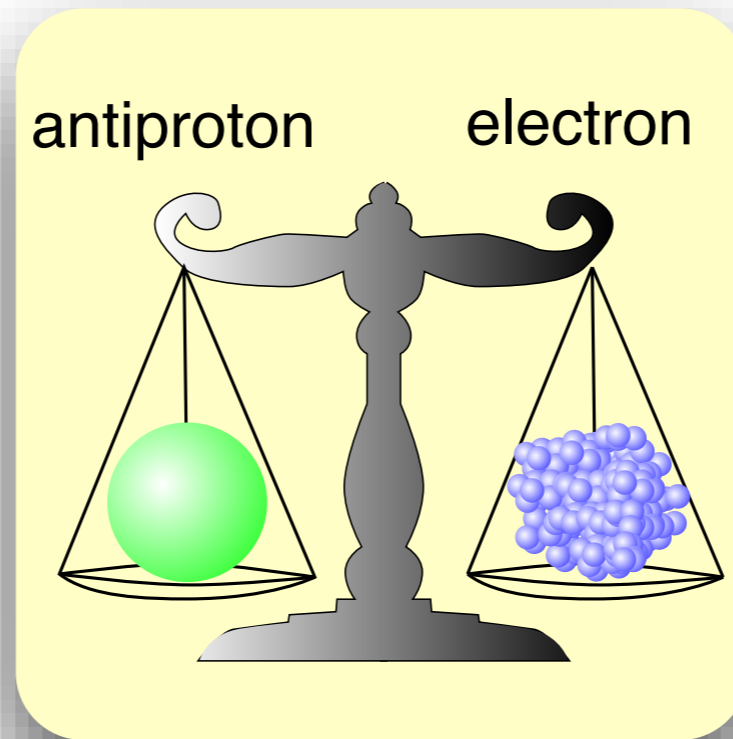
$$\nu_{n,l \rightarrow n',l'} = R c \frac{m_{\bar{p}}^*}{m_e} Z_{\text{eff}}^2 \left(\frac{1}{n'^2} - \frac{1}{n^2} \right) + QED$$

\bar{p} - e mass ratio

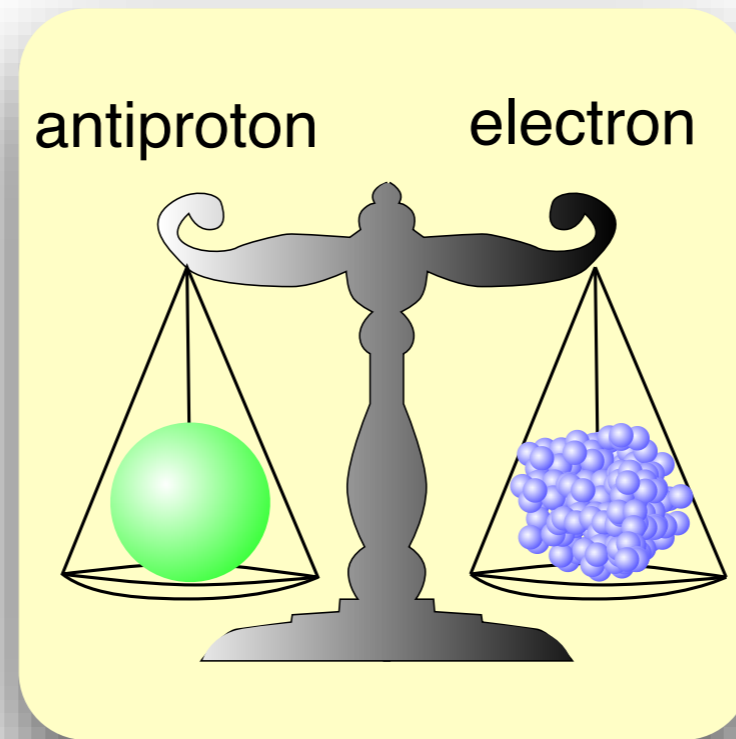
Theory

Korobov

$\bar{p}\text{He}$ can contribute to

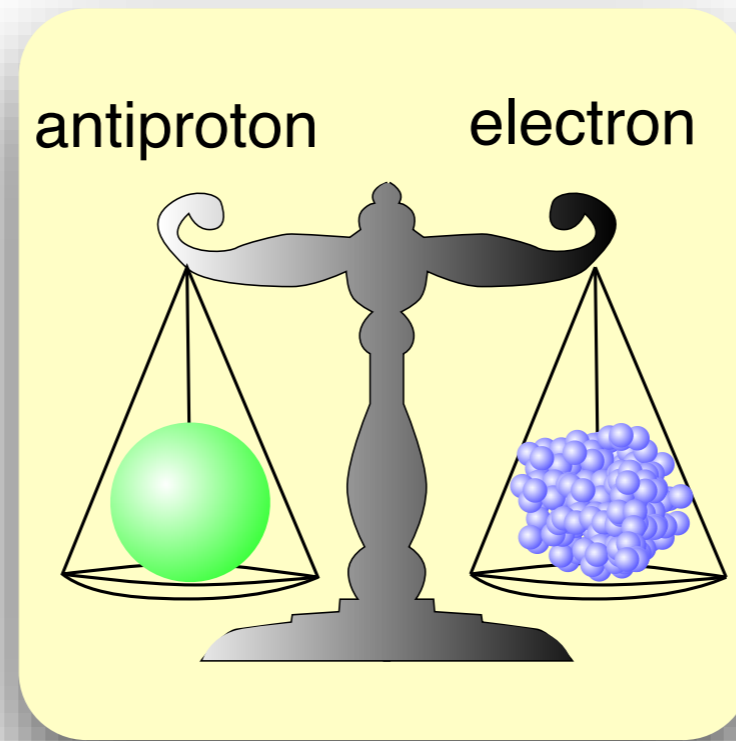


$\bar{p}\text{He}$ can contribute to



↓
CPT test

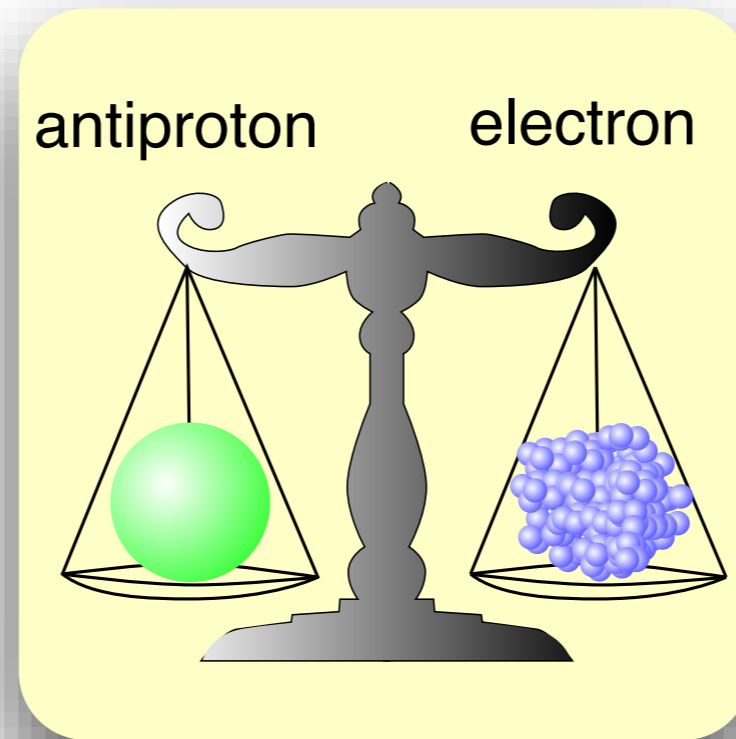
$\bar{p}\text{He}$ can contribute to



↓
CPT test

↓
CPT theorem

$\bar{p}\text{He}$ can contribute to

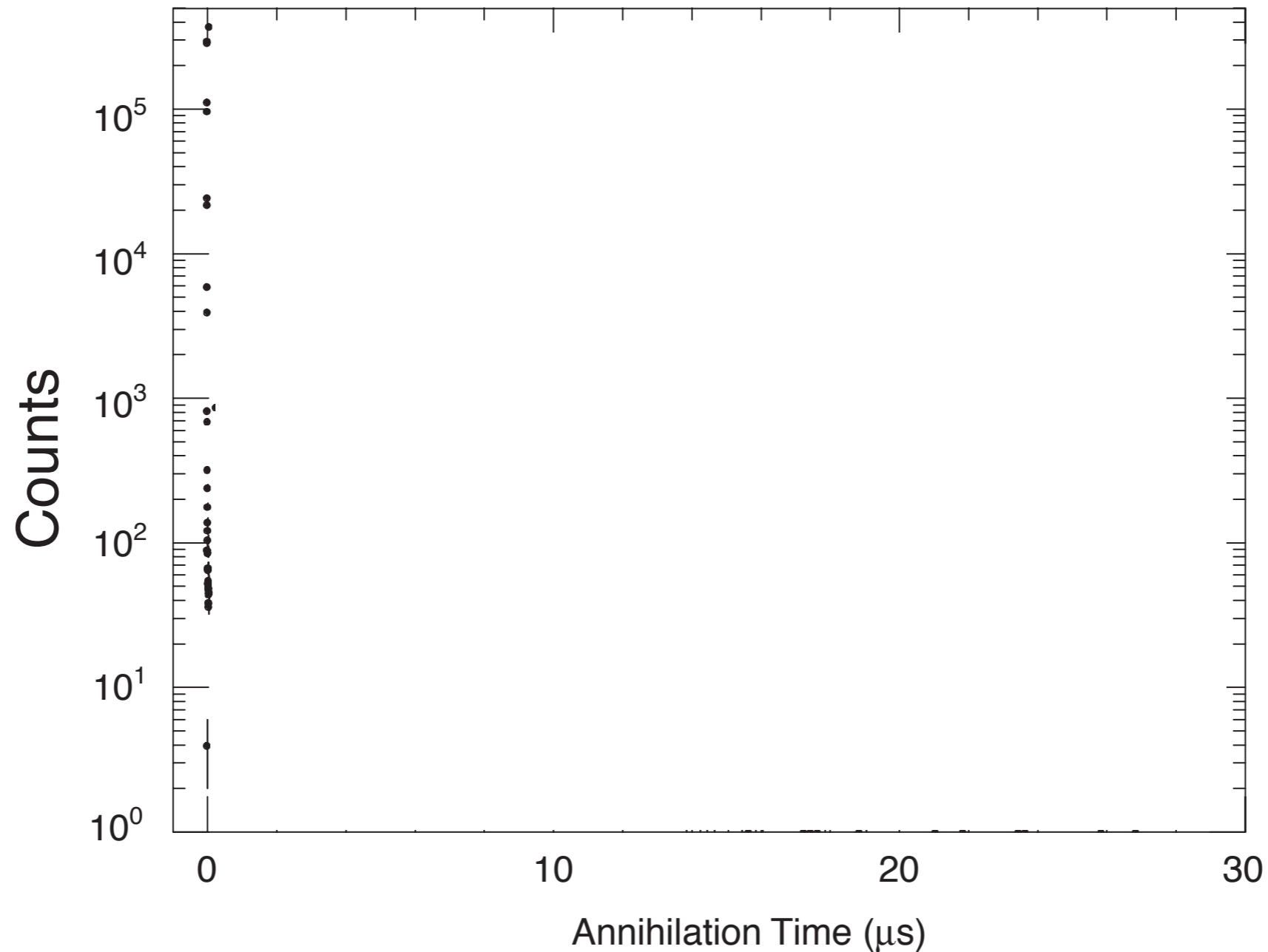


↓
CPT test

↓
CPT theorem

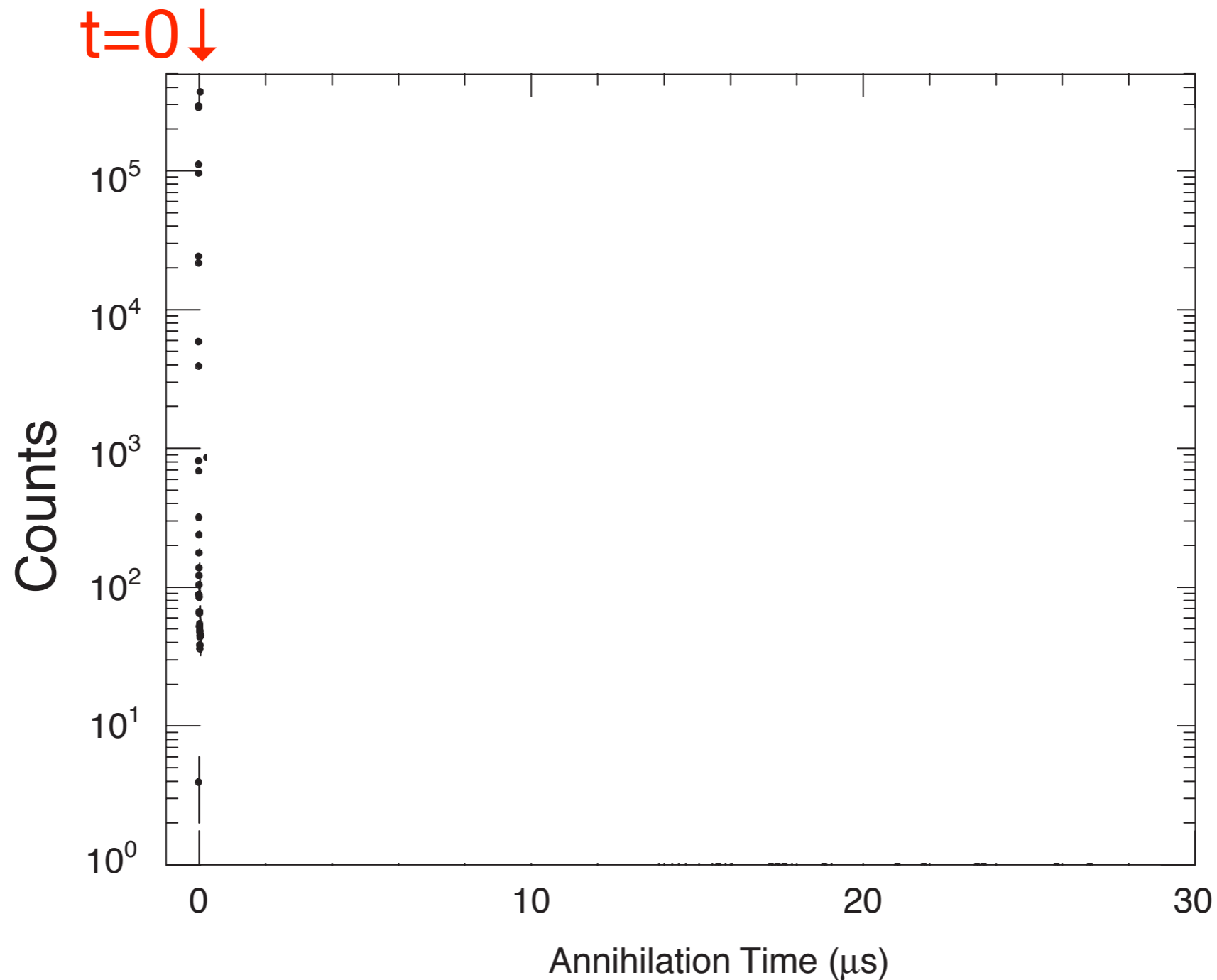
↓
proton-electron mass ratio
(CODATA)

discovery of \bar{p} longevity in helium (at KEK)



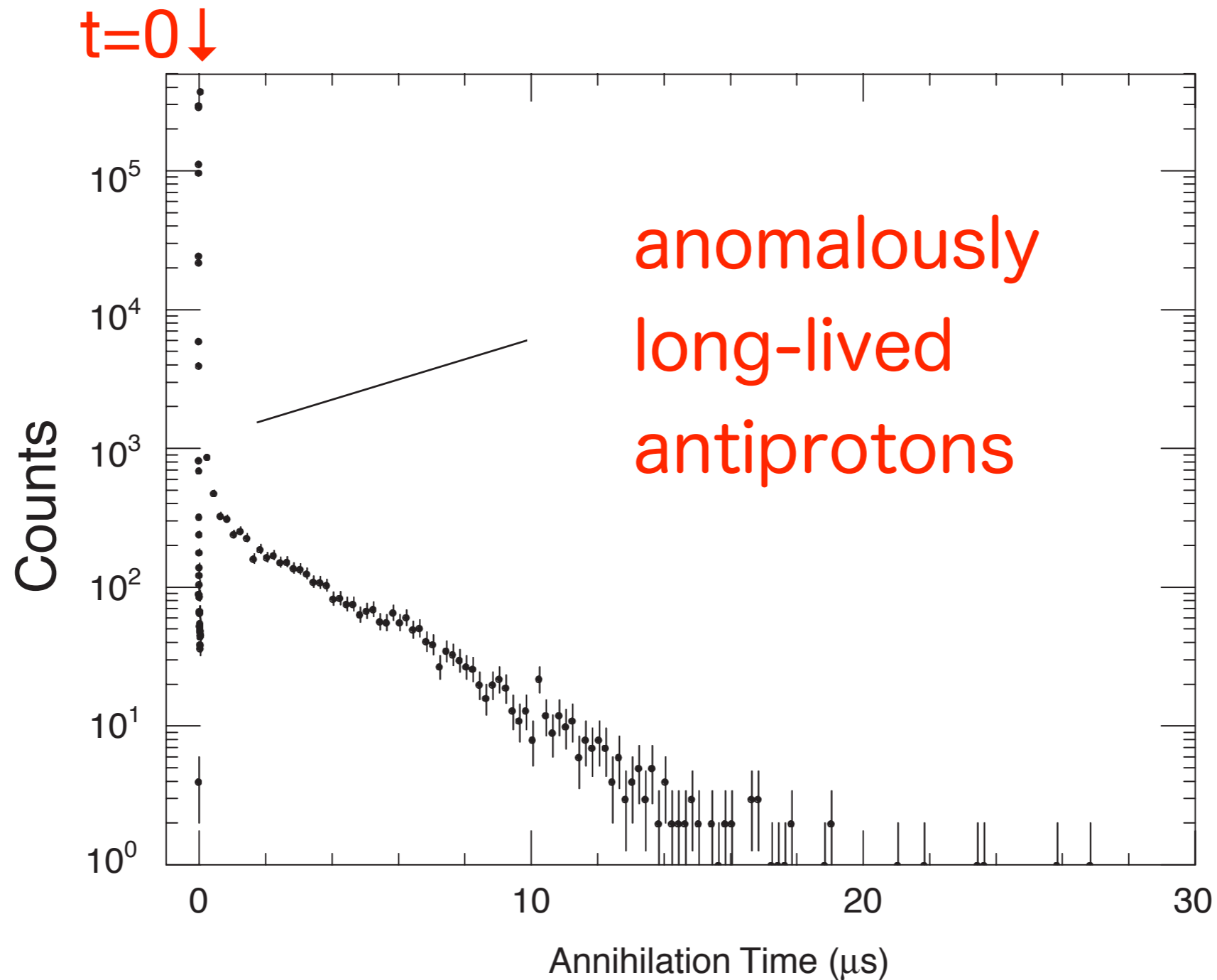
Iwasaki et al., PRL 67 (1991) 1246

discovery of \bar{p} longevity in helium (at KEK)



Iwasaki et al., PRL 67 (1991) 1246

discovery of \bar{p} longevity in helium (at KEK)



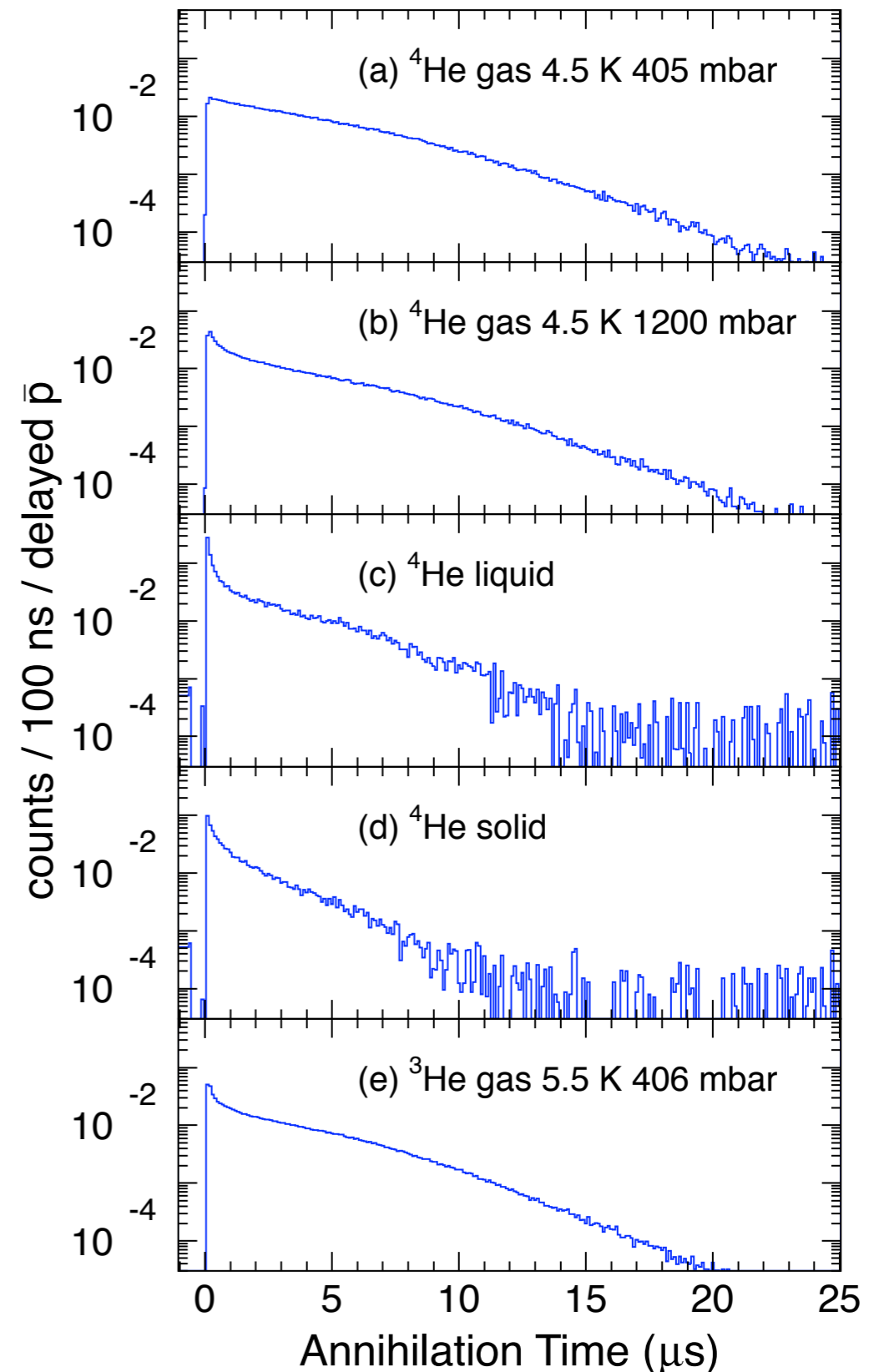
Iwasaki et al., PRL 67 (1991) 1246

\bar{p} He formation probability & lifetime

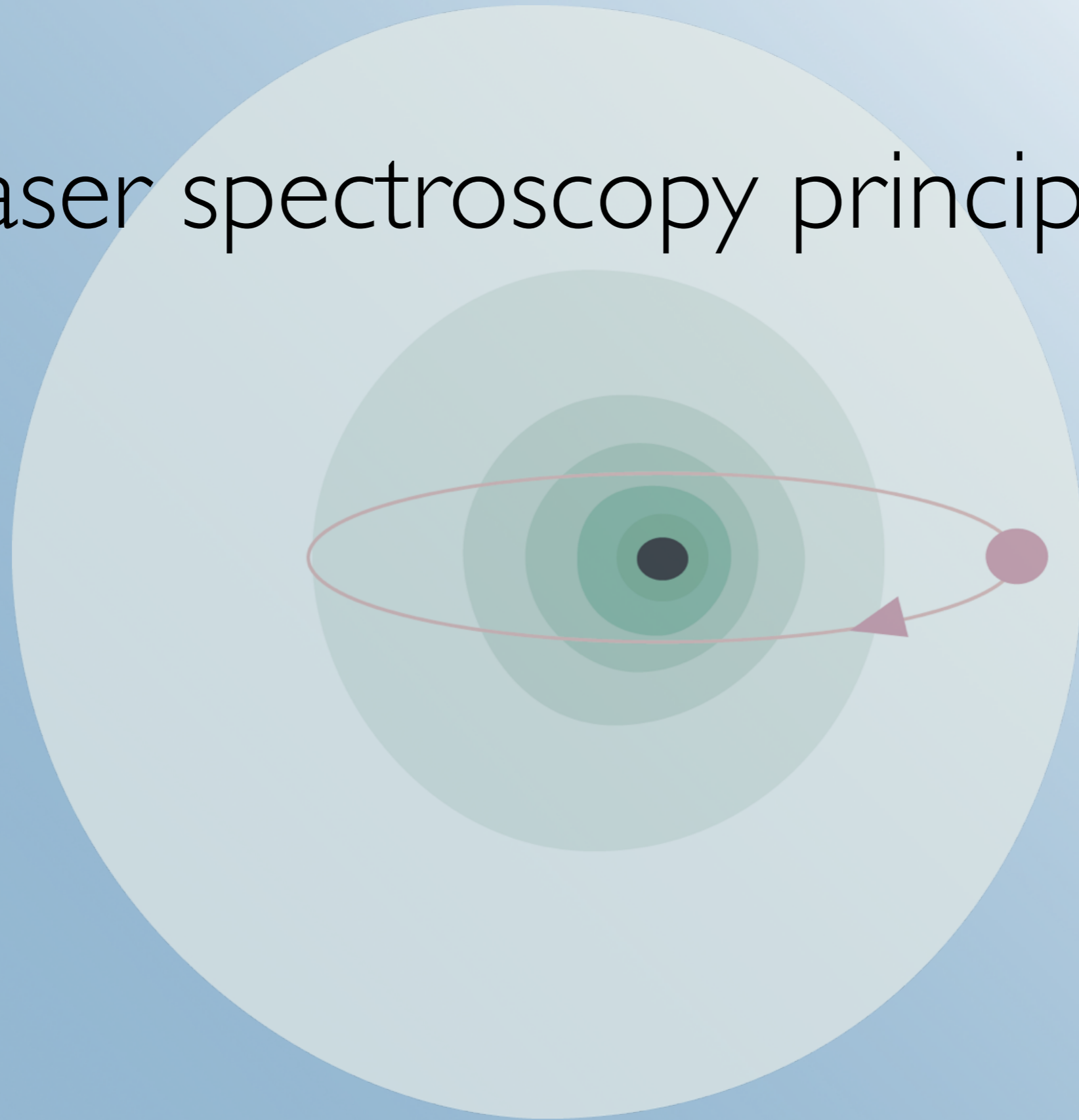
At LEAR -

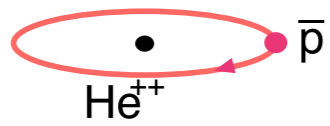
Established \bar{p} longevity in
gas, liquid, solid helium-3
& helium-4

Lifetime $3\sim 4\mu\text{s}$, formation
probability $\sim 3\%$



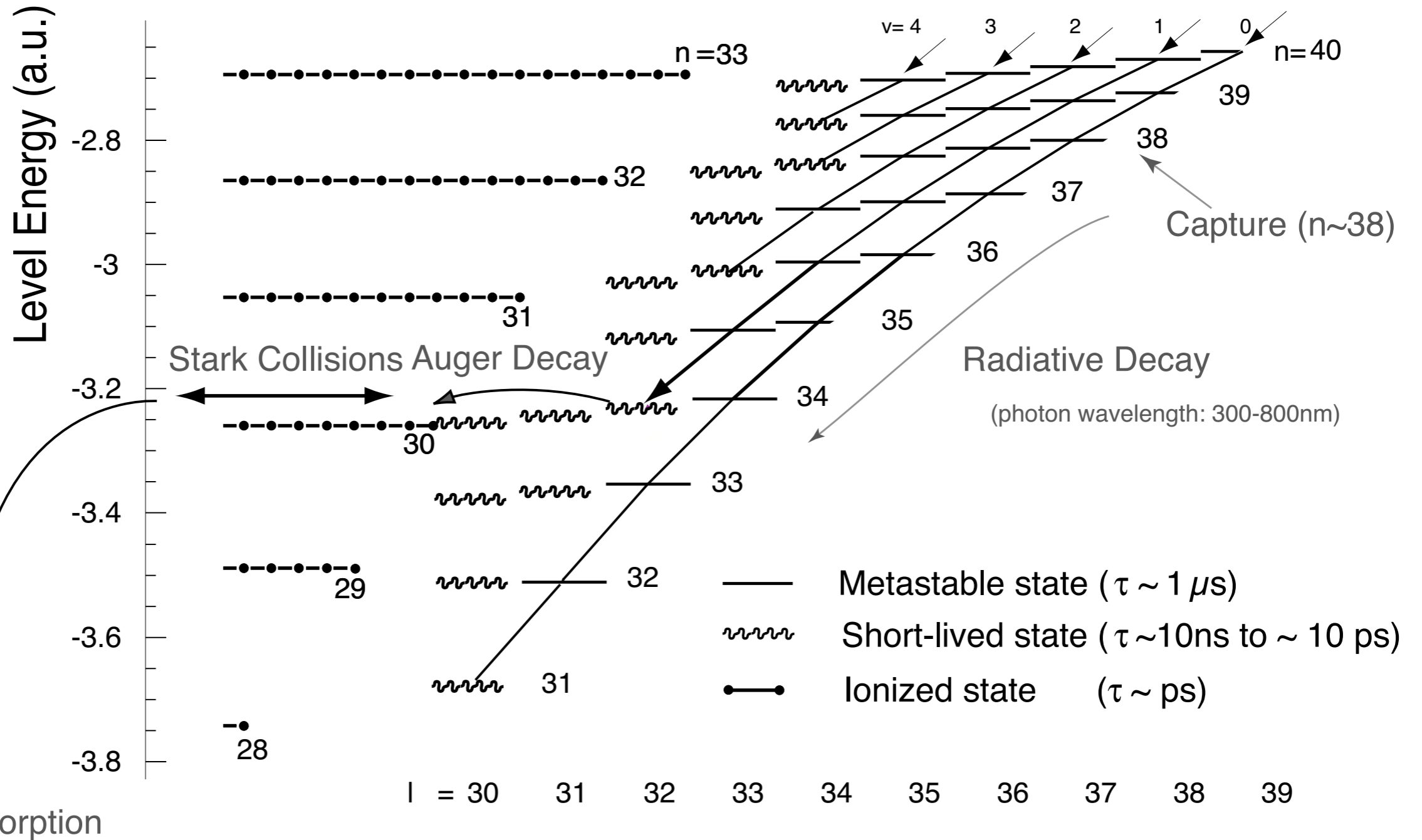
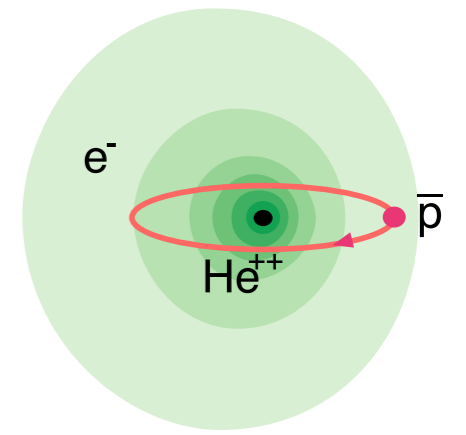
Laser spectroscopy principles



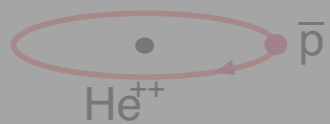


$\bar{p}^4\text{He}^{++}$ ion

$\bar{p}^4\text{He}^+$ atom

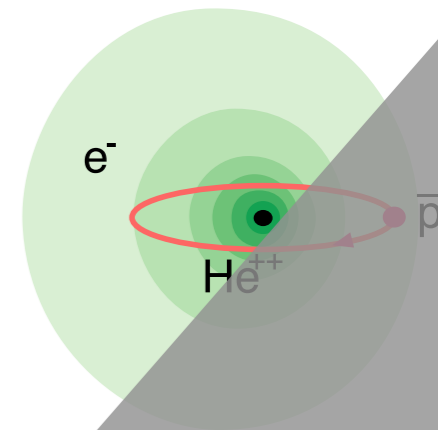


Nuclear Absorption

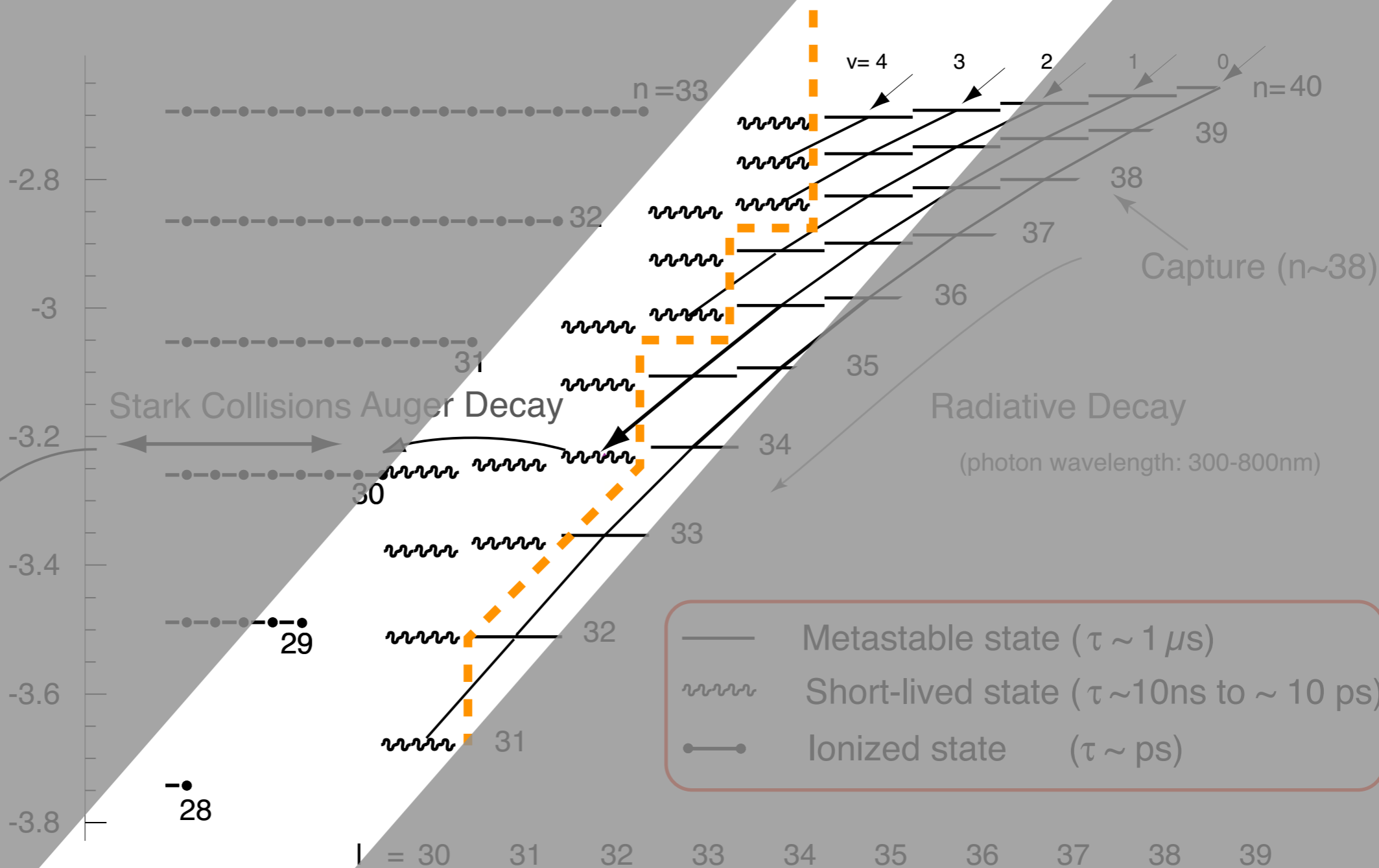


$\bar{p}^4\text{He}^{++}$ ion

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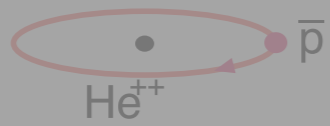


Level Energy (a.u.)



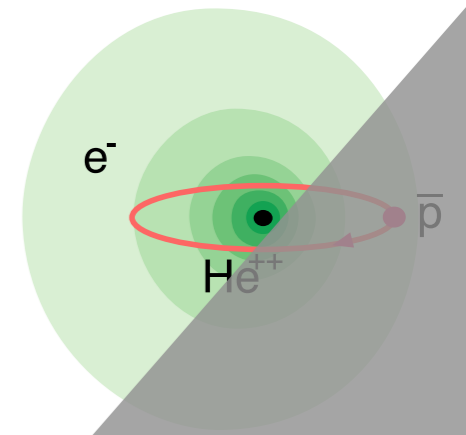
- Metastable state ($\tau \sim 1 \mu\text{s}$)
- ~~~~~ Short-lived state ($\tau \sim 10\text{ns}$ to $\sim 10 \text{ps}$)
- Ionized state ($\tau \sim \text{ps}$)

Nuclear Absorption

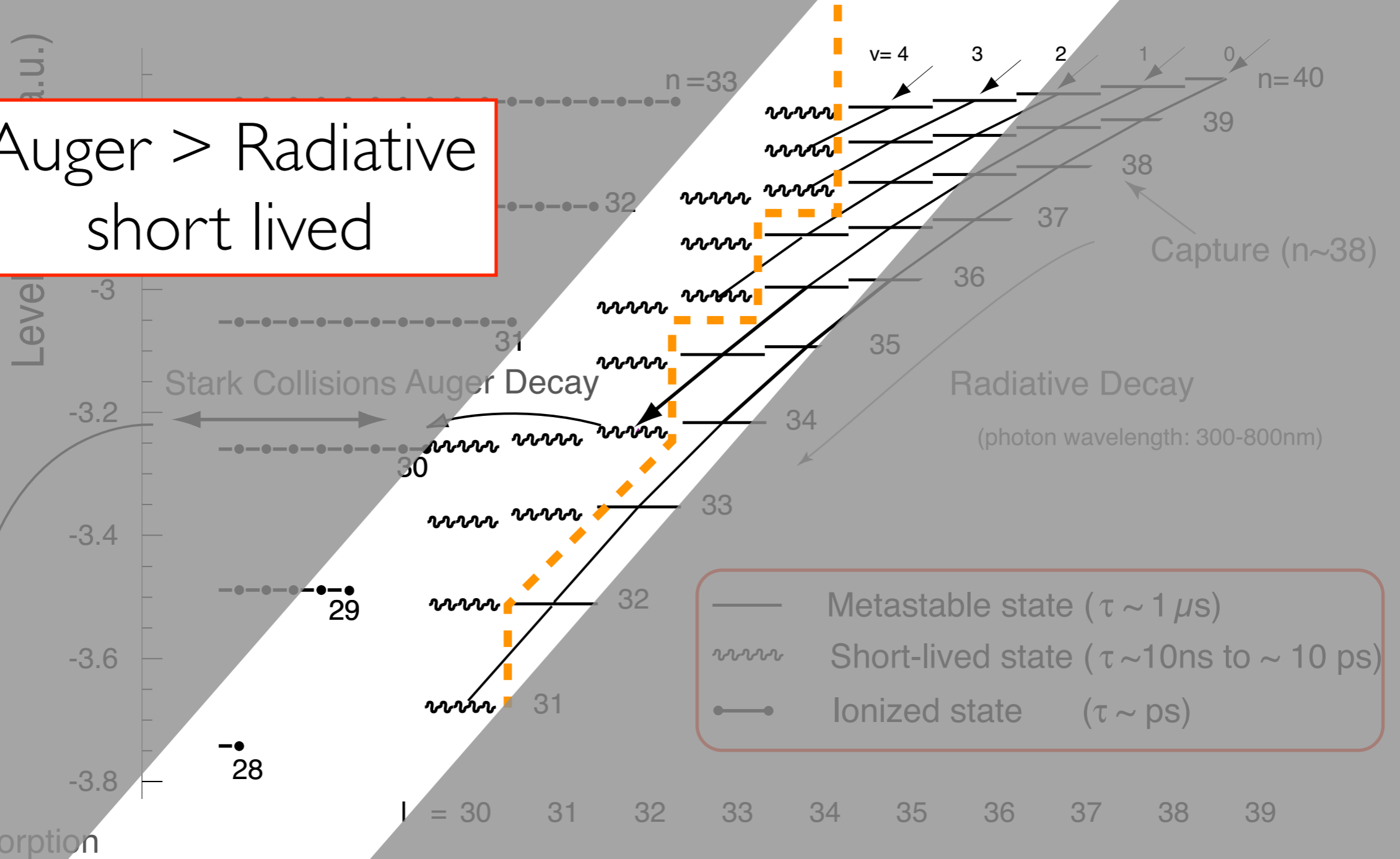


$\bar{p}^4\text{He}^{++}$ ion

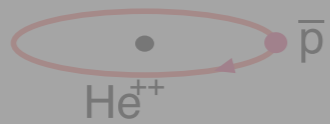
$\bar{p}^4\text{He}^+$ atom



Auger > Radiative
short lived

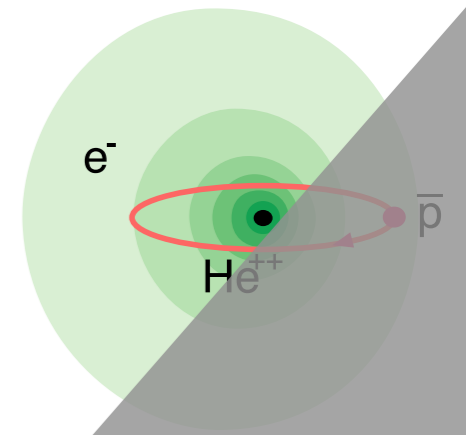


Nuclear Absorption



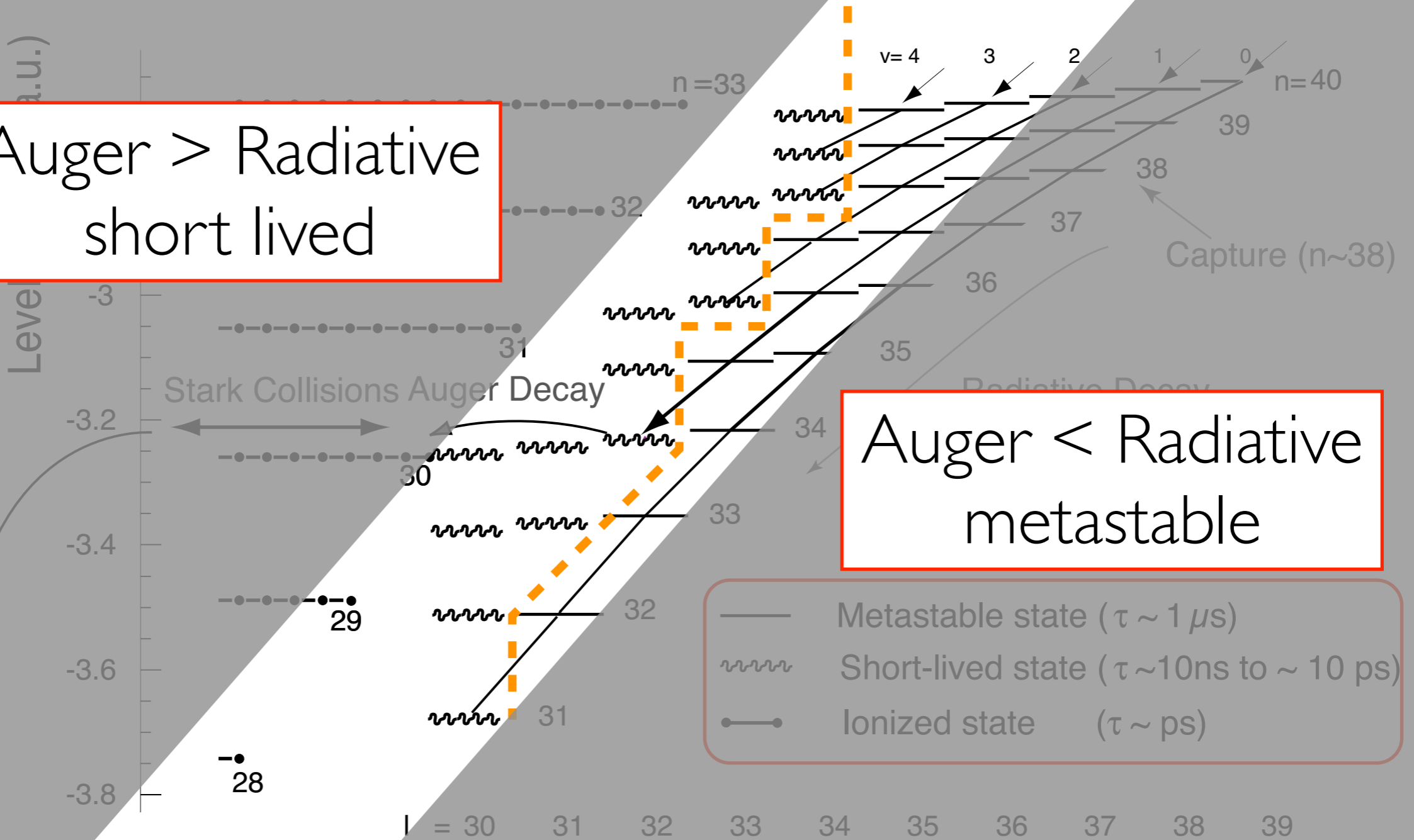
$\bar{p}^4\text{He}^{++}$ ion

$\bar{p}^4\text{He}^+$ atom

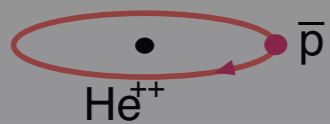


Auger > Radiative
short lived

Auger < Radiative
metastable

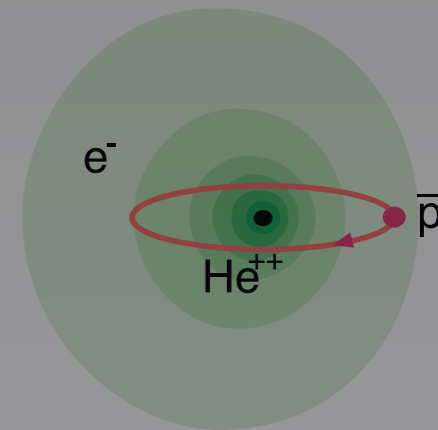


Nuclear Absorption

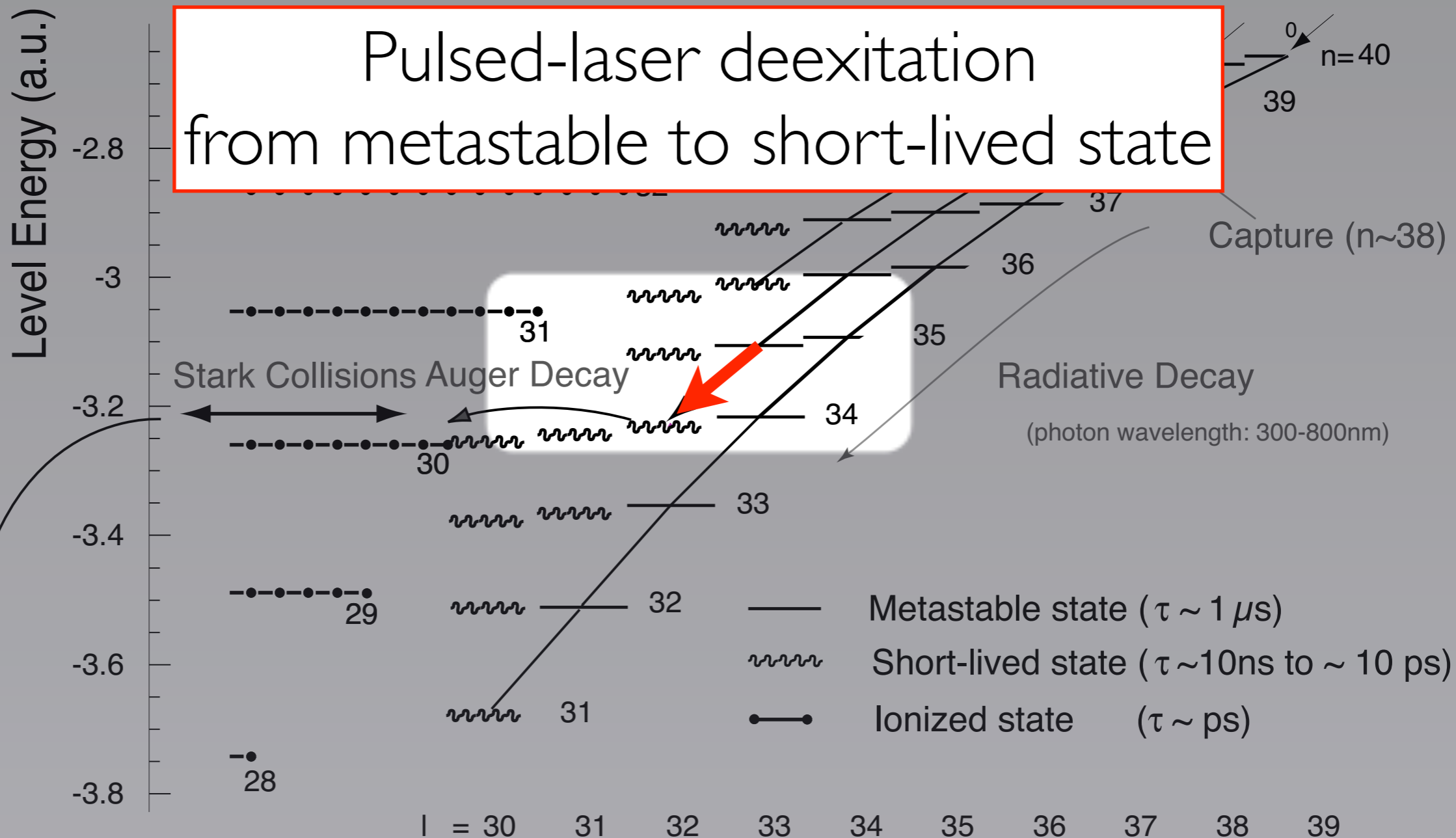


$\bar{p}^4\text{He}^{++}$ ion

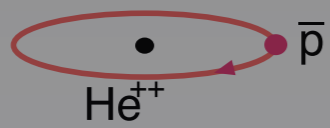
$\bar{p}^4\text{He}^+$ atom



Pulsed-laser deexcitation
from metastable to short-lived state

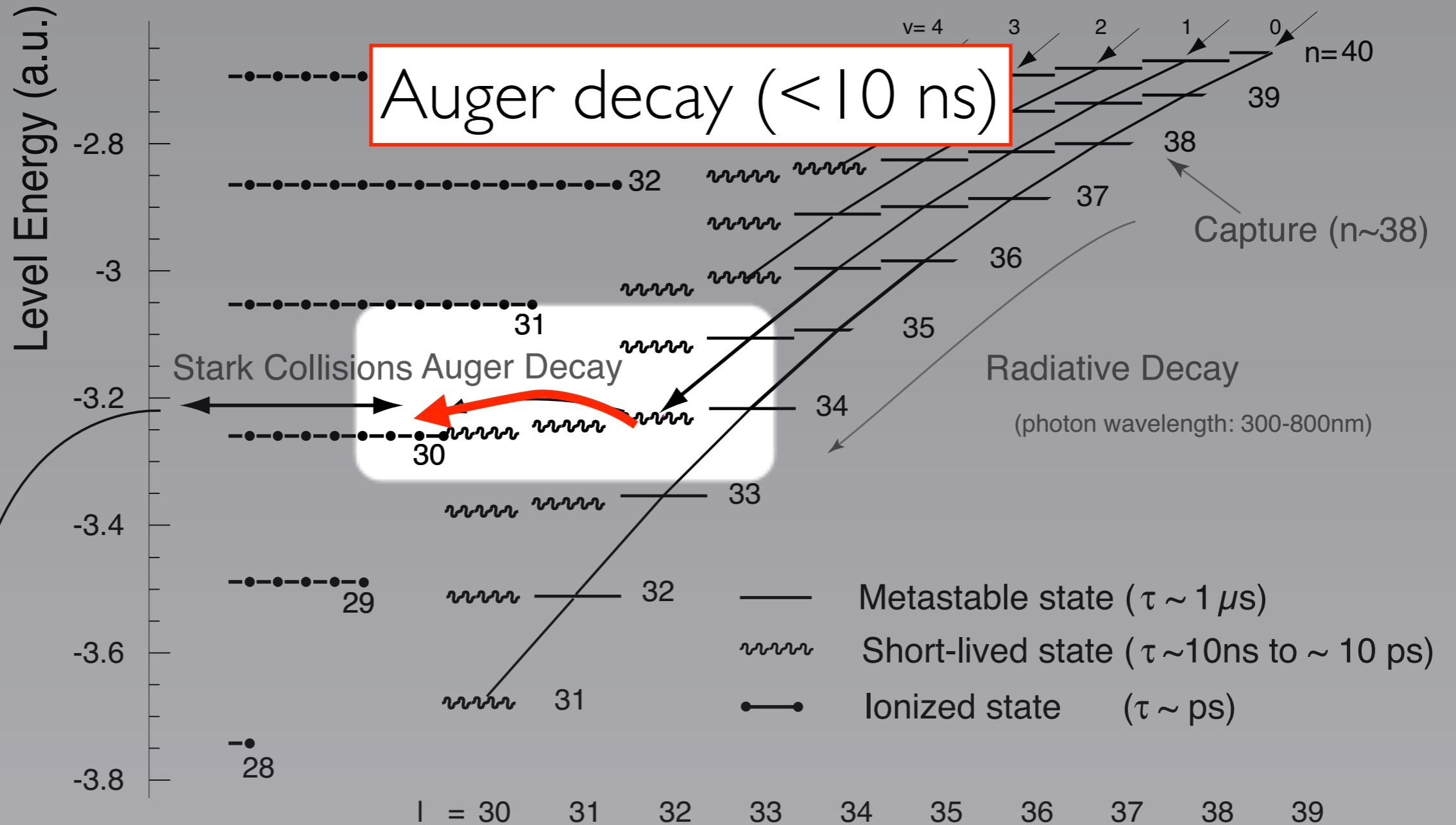
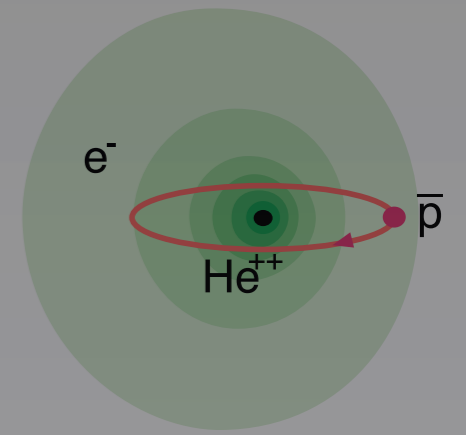


Nuclear Absorption

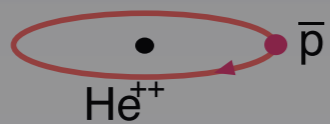


$\bar{p}^4\text{He}^{++}$ ion

$\bar{p}^4\text{He}^+$ atom

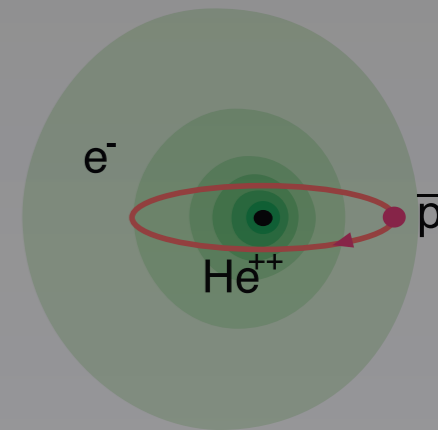


Nuclear Absorption

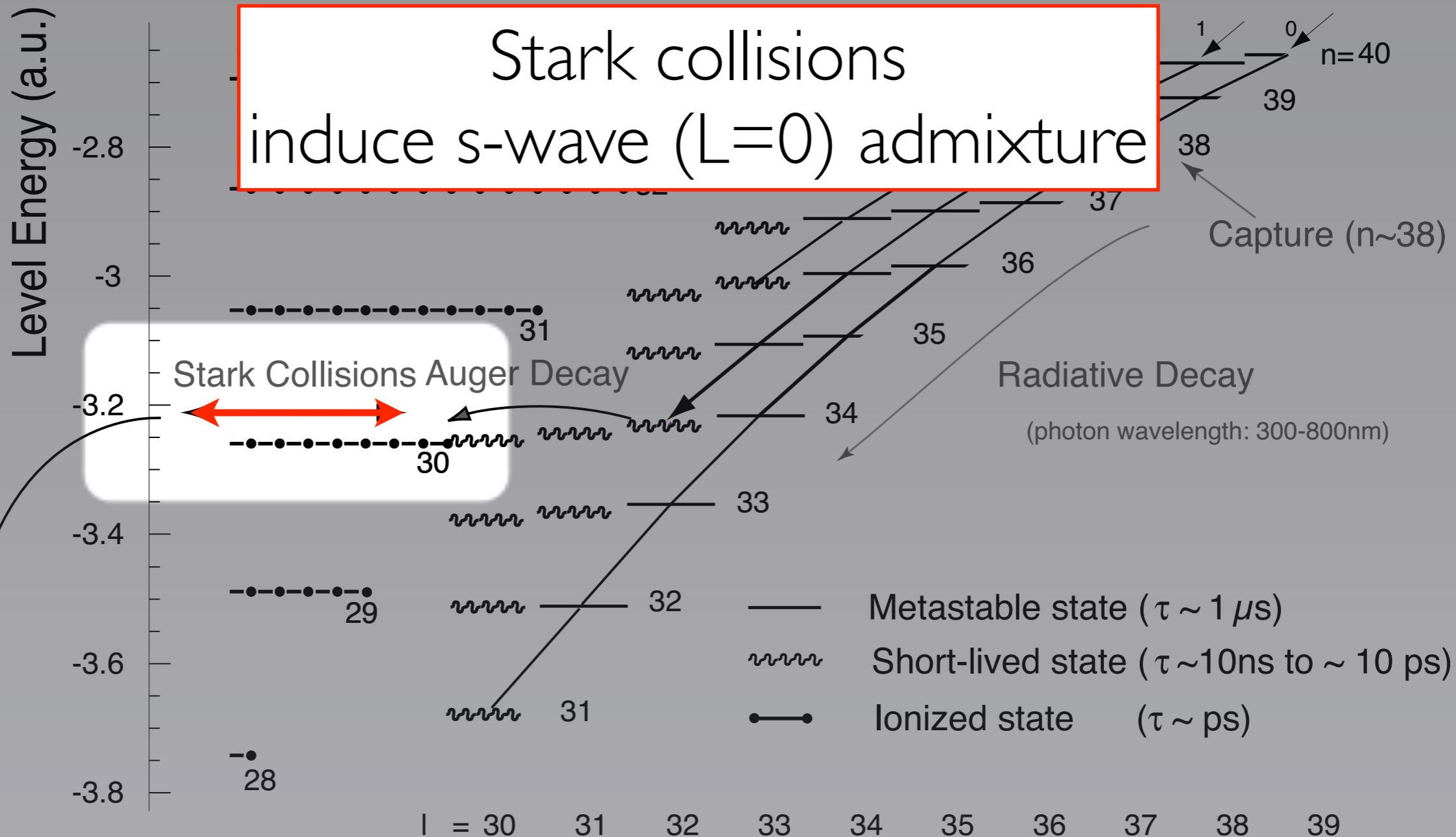


$\bar{p}^4\text{He}^{++}$ ion

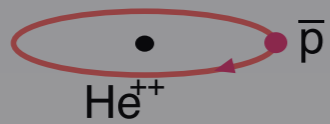
$\bar{p}^4\text{He}^+$ atom



Stark collisions induce s-wave ($L=0$) admixture

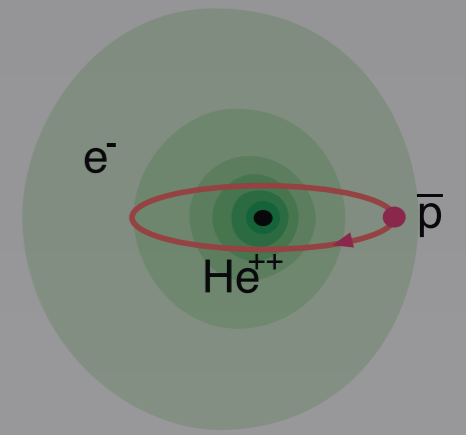


Nuclear Absorption



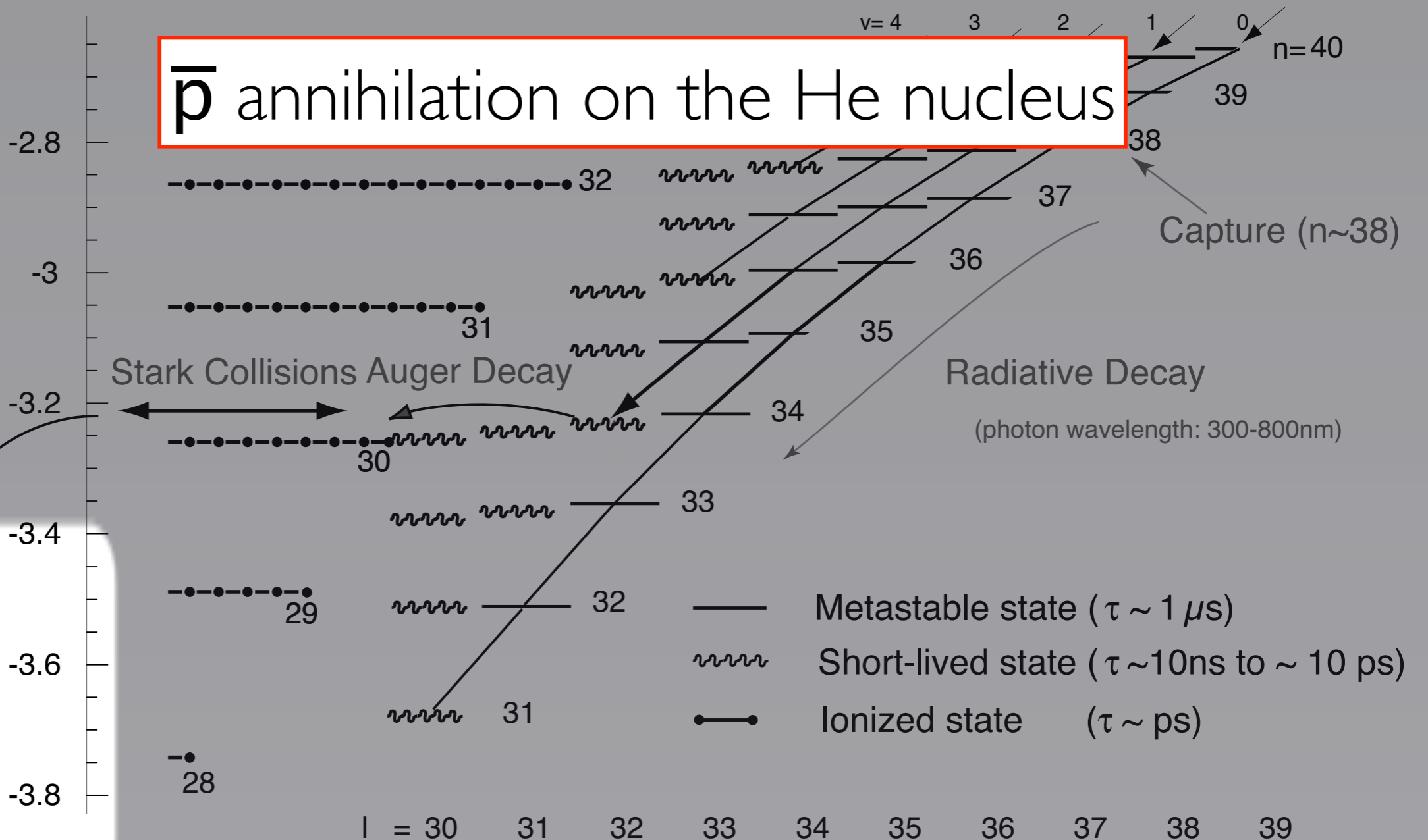
$\bar{p}^4\text{He}^{++}$ ion

$\bar{p}^4\text{He}^+$ atom

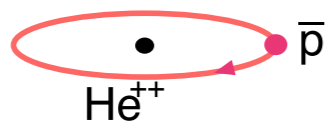


Level Energy (a.u.)

\bar{p} annihilation on the He nucleus

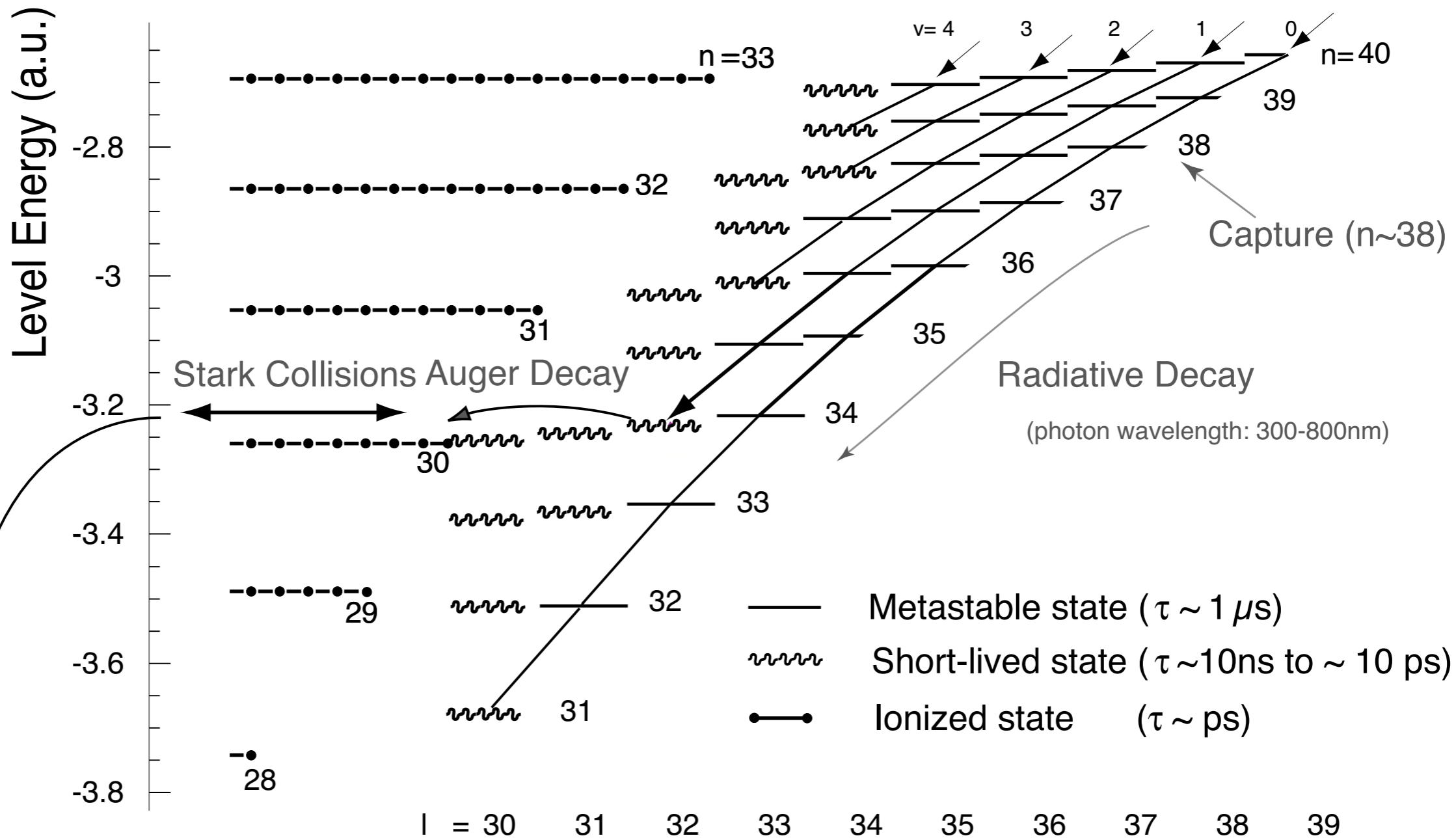
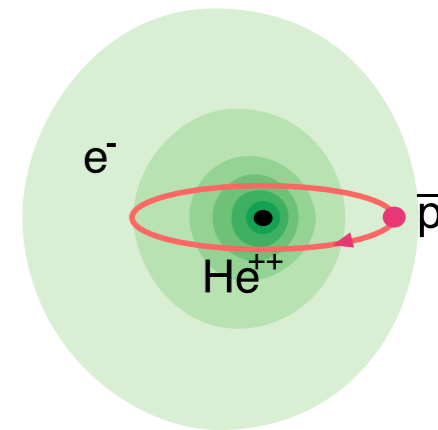


Nuclear Absorption



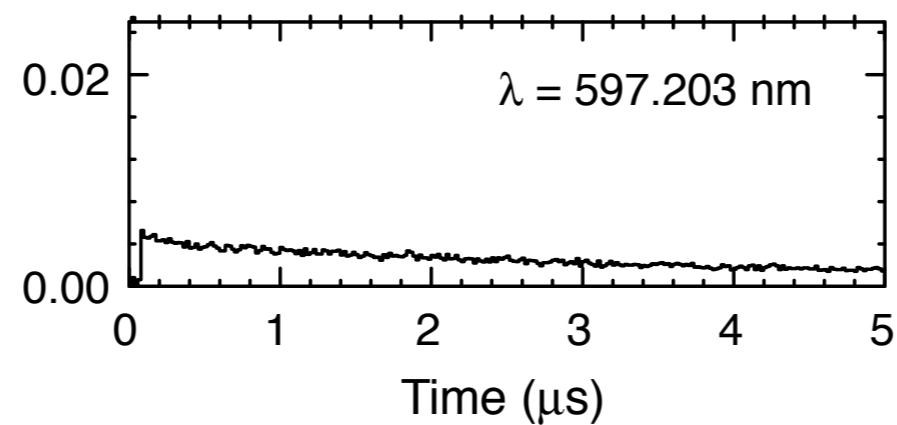
$\bar{p}^4\text{He}^{++}$ ion

$\bar{p}^4\text{He}^+$ atom

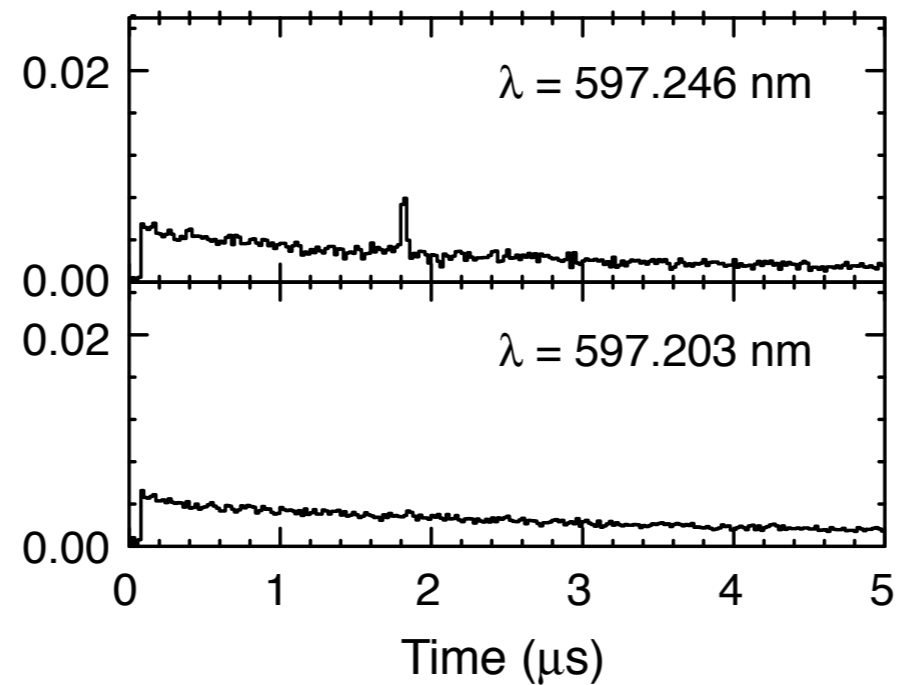


Nuclear Absorption

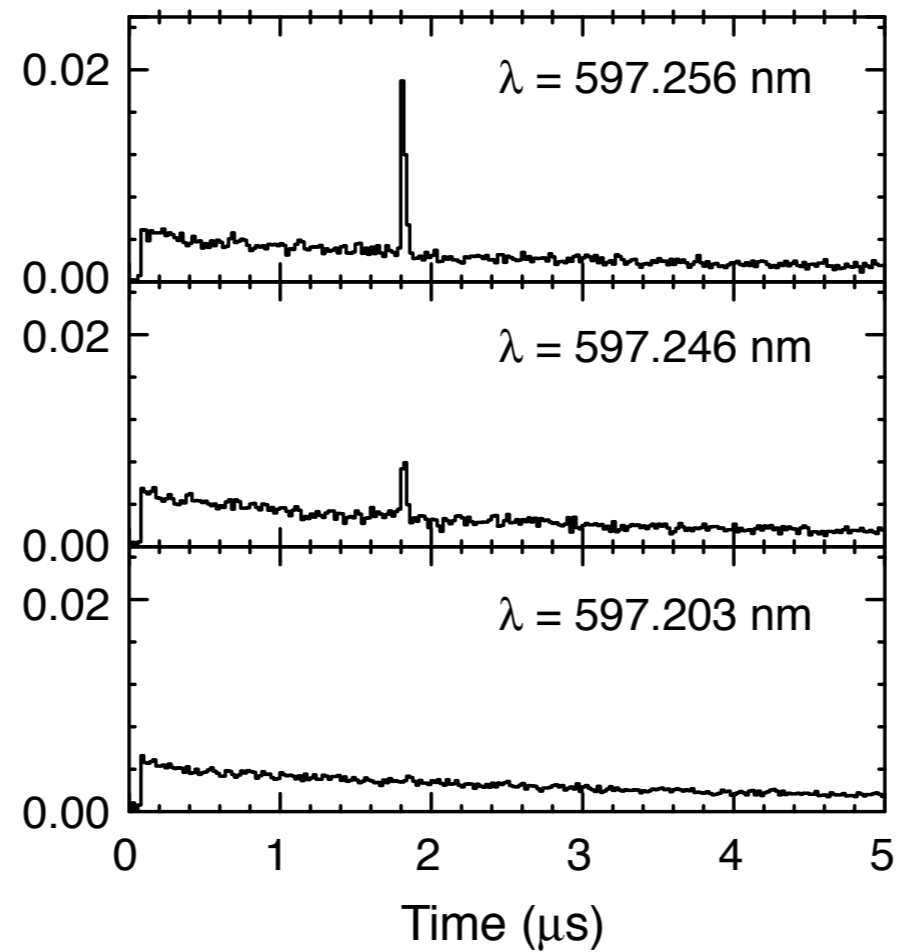
An example, $(n,l)=(39,35) \rightarrow (38,34)$



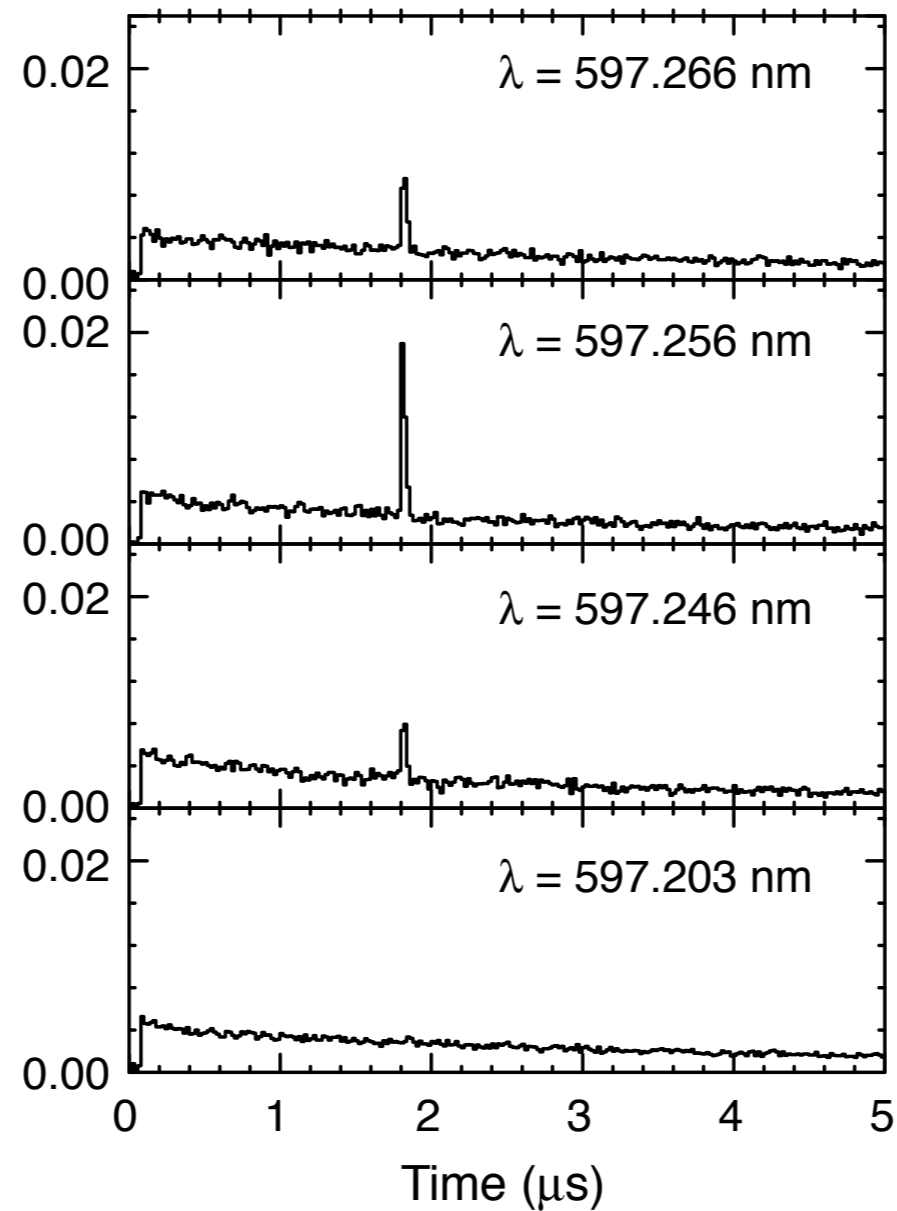
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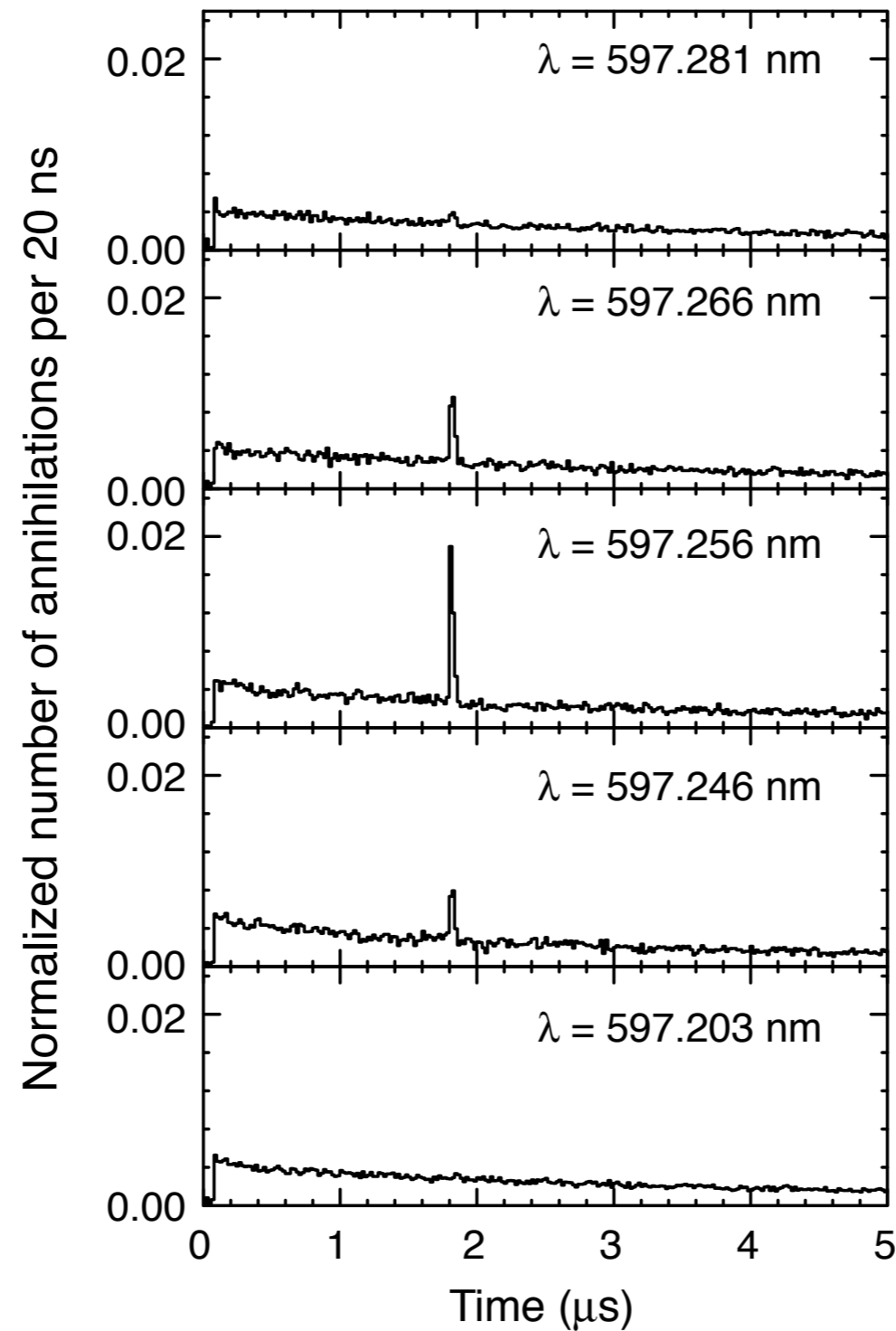


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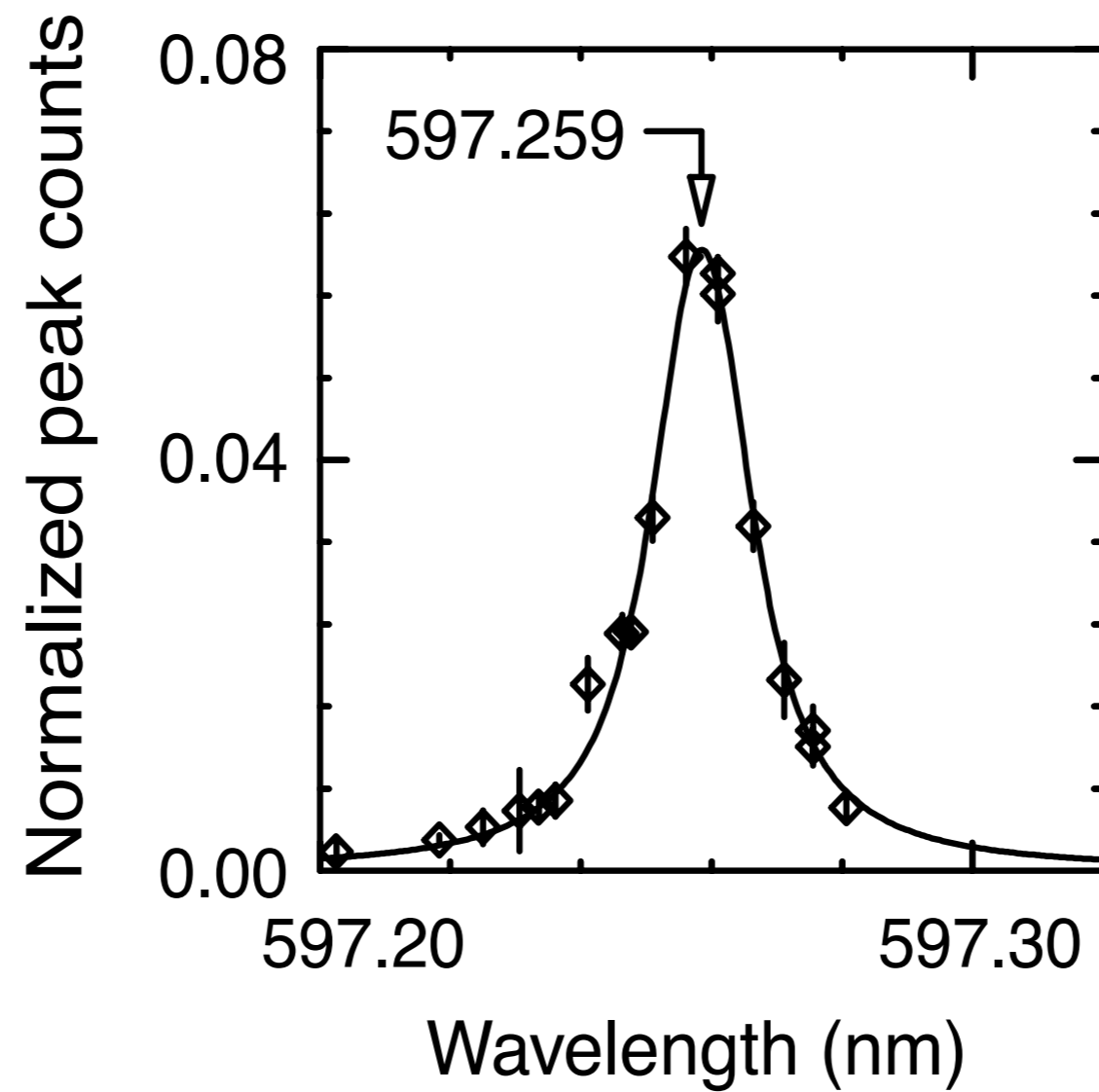
An example, $(n,l)=(39,35) \rightarrow (38,34)$

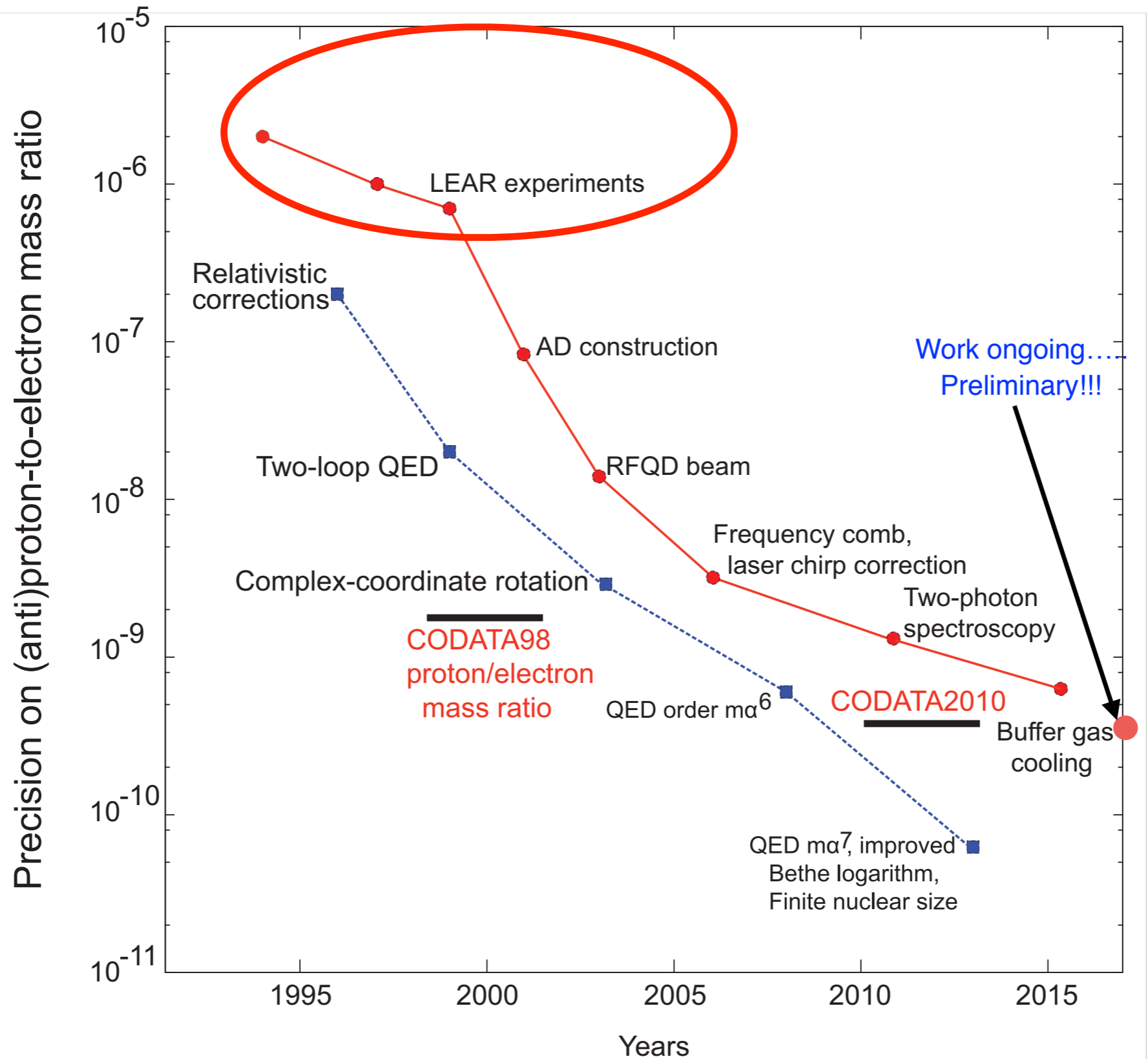
N. Morita et al, Phys. Rev. Lett. 72 (1994) 1180.



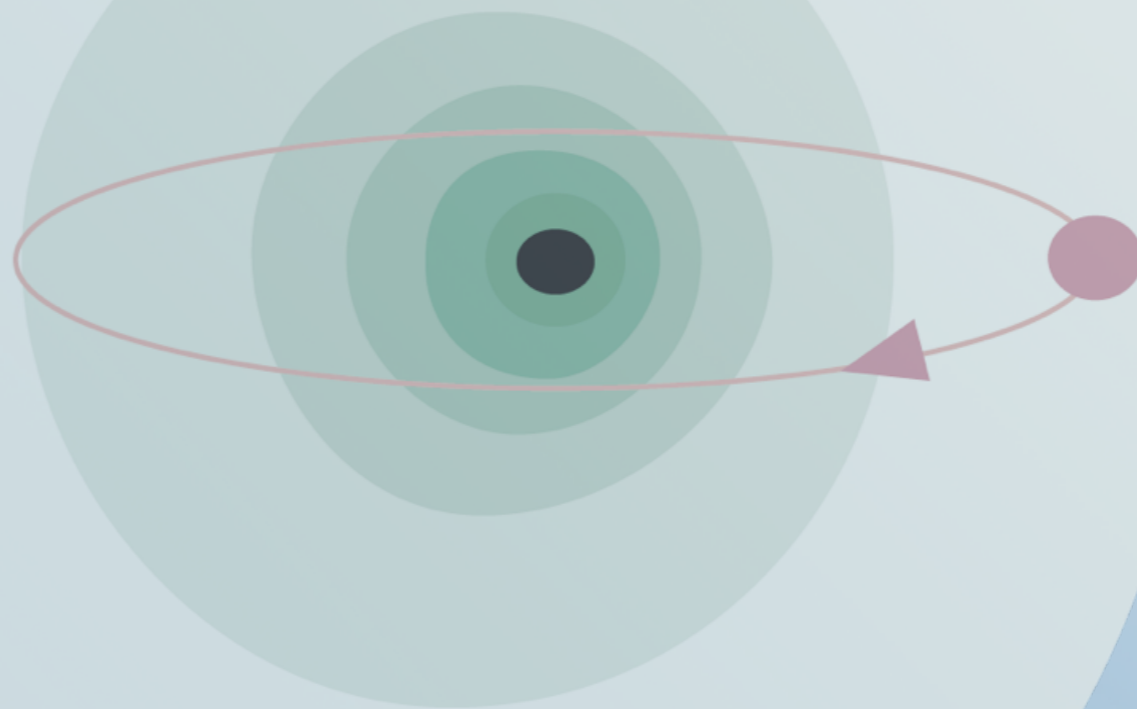
Laser Resonance Curve

N. Morita et al, Phys. Rev. Lett. 72 (1994) 1180.

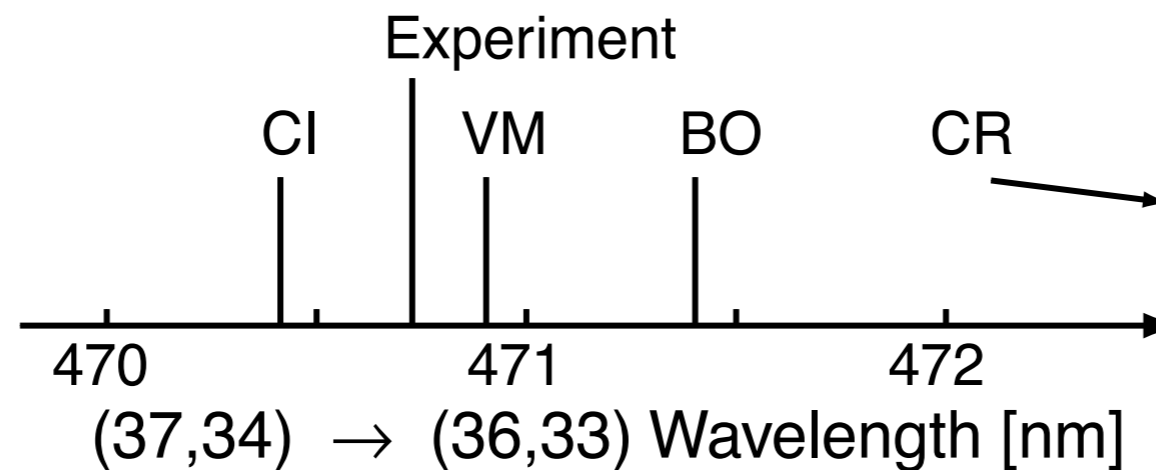
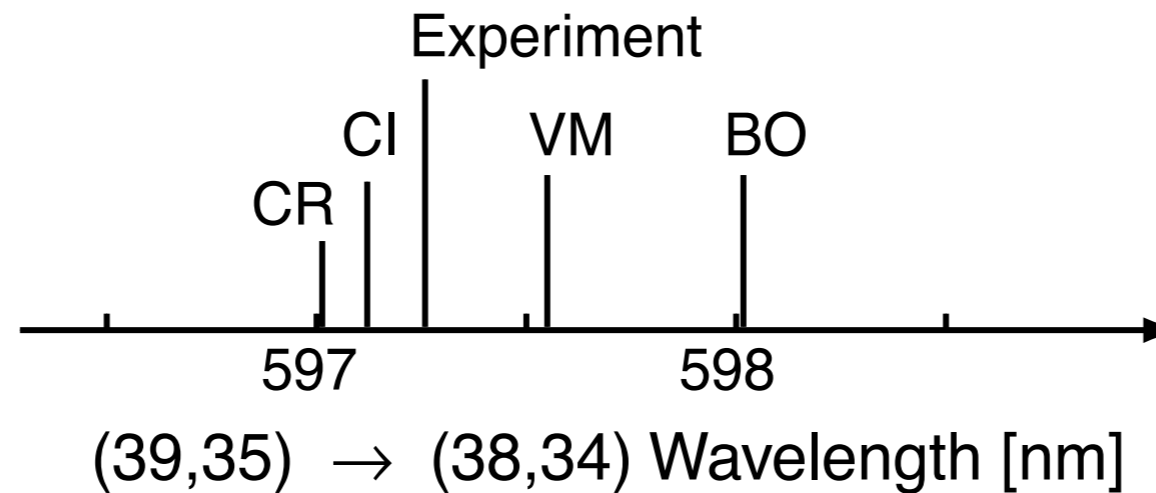




Theory



20 years ago - Theory precision ~ 1000 ppm



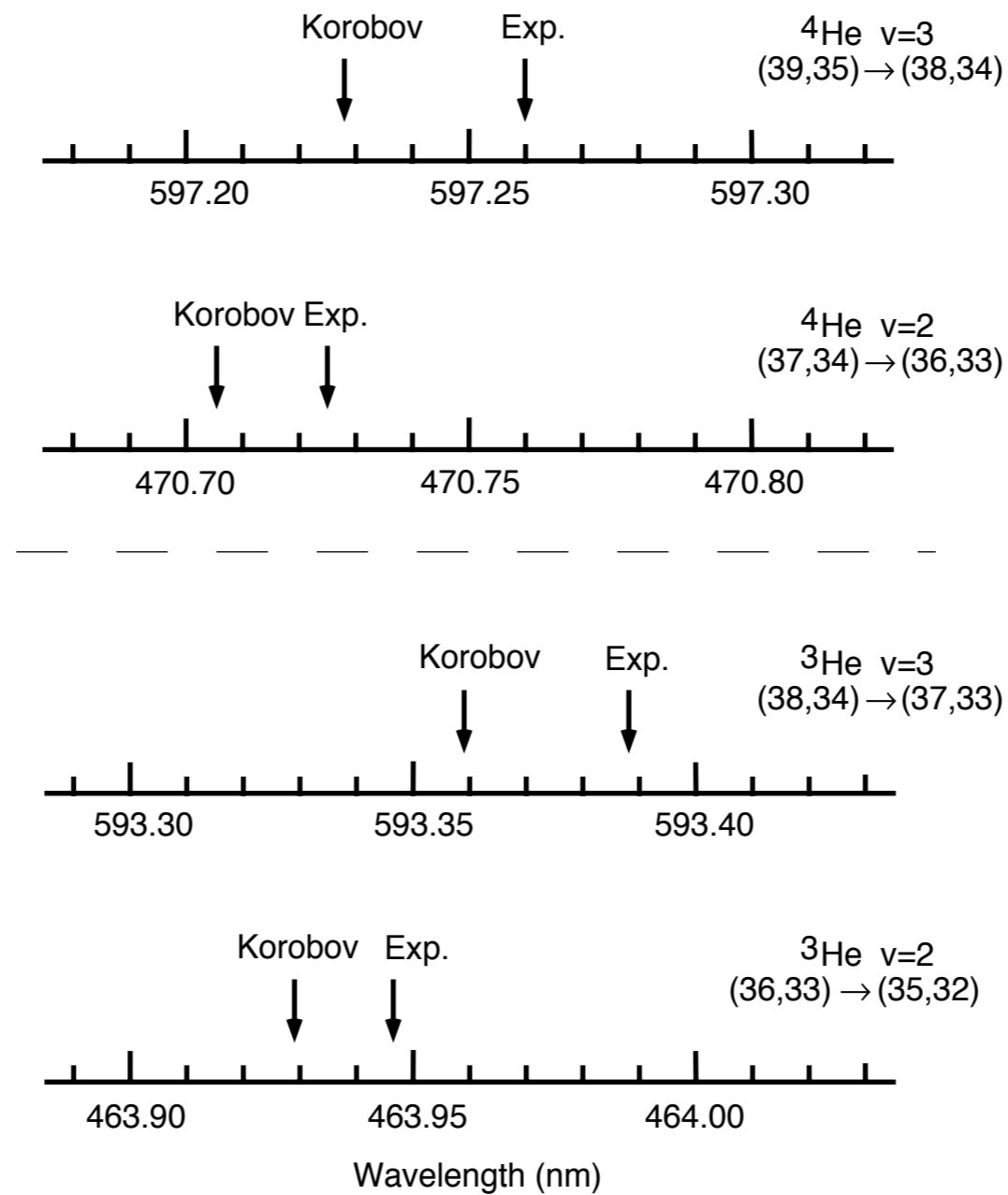
F.E. Maas et al., Phys. Rev. A 52 (1995) 4266.

Variational calculation of energy levels in $p\text{He}^+$ molecular systems

V. I. Korobov

Joint Institute for Nuclear Research, Dubna, Russia

(Received 29 April 1996)

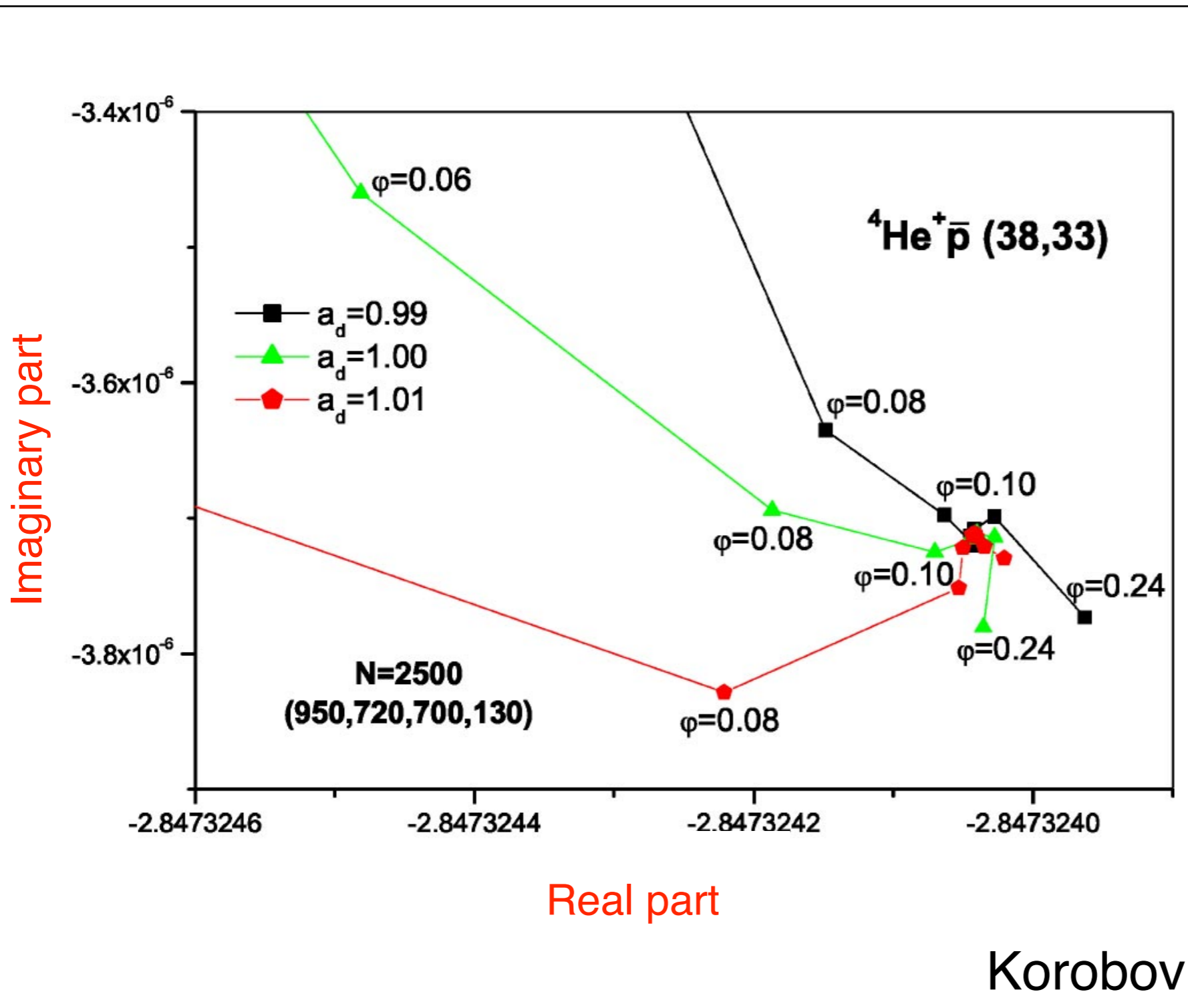


Theory - non-relativistic H

$$H = T + V$$
$$= -\frac{1}{2\mu_1} \nabla_{\mathbf{R}}^2 - \frac{1}{2\mu_2} \nabla_{\mathbf{r}}^2 - \frac{1}{M_{\text{He}}} \nabla_{\mathbf{R}} \cdot \nabla_{\mathbf{r}} - \frac{2}{R} - \frac{2}{r} + \frac{1}{|\mathbf{R} - \mathbf{r}|},$$

$\mu_1^{-1} = M_{\text{He}}^{-1} + M_X^{-1}, \quad \mu_2^{-1} = M_{\text{He}}^{-1} + m_e^{-1},$

Complex coordinate rotation (CCR) method



Careful treatment of Auger decay is needed

CCR calculates complex eigen values

add relativistic correction (~ 100 ppm)

V.I. Korobov, D.D. Bakalov, Phys. Rev. Lett. 79 (1997) 3379.

$$H = T + V$$

$$= -\frac{1}{2\mu_1} \nabla_{\mathbf{R}}^2 - \frac{1}{2\mu_2} \nabla_{\mathbf{r}}^2 - \frac{1}{M_{\text{He}}} \nabla_{\mathbf{R}} \cdot \nabla_{\mathbf{r}} - \frac{2}{R} - \frac{2}{r} + \frac{1}{|\mathbf{R} - \mathbf{r}|},$$

$$\mu_1^{-1} = M_{\text{He}}^{-1} + M_X^{-1}, \quad \mu_2^{-1} = M_{\text{He}}^{-1} + m_e^{-1},$$

$$E_{rc} = \alpha^2 \left\langle -\frac{\mathbf{p}_e^4}{8m_e^3} + \frac{4\pi}{8m_e^2} [Z_{\text{He}} \delta(\mathbf{r}_{\text{He}}) + Z_p^- \delta(\mathbf{r}_p^-)] \right\rangle.$$

add self energy (~15 ppm)

$$H = T + V$$

$$= -\frac{1}{2\mu_1} \nabla_{\mathbf{R}}^2 - \frac{1}{2\mu_2} \nabla_{\mathbf{r}}^2 - \frac{1}{M_{\text{He}}} \nabla_{\mathbf{R}} \cdot \nabla_{\mathbf{r}} - \frac{2}{R} - \frac{2}{r} + \frac{1}{|\mathbf{R} - \mathbf{r}|},$$

$$\mu_1^{-1} = M_{\text{He}}^{-1} + M_X^{-1}, \quad \mu_2^{-1} = M_{\text{He}}^{-1} + m_e^{-1},$$

$$E_{rc} = \alpha^2 \left\langle -\frac{\mathbf{p}_e^4}{8m_e^3} + \frac{4\pi}{8m_e^2} [Z_{\text{He}} \delta(\mathbf{r}_{\text{He}}) + Z_p^- \delta(\mathbf{r}_p^-)] \right\rangle.$$

Bethe logarithm

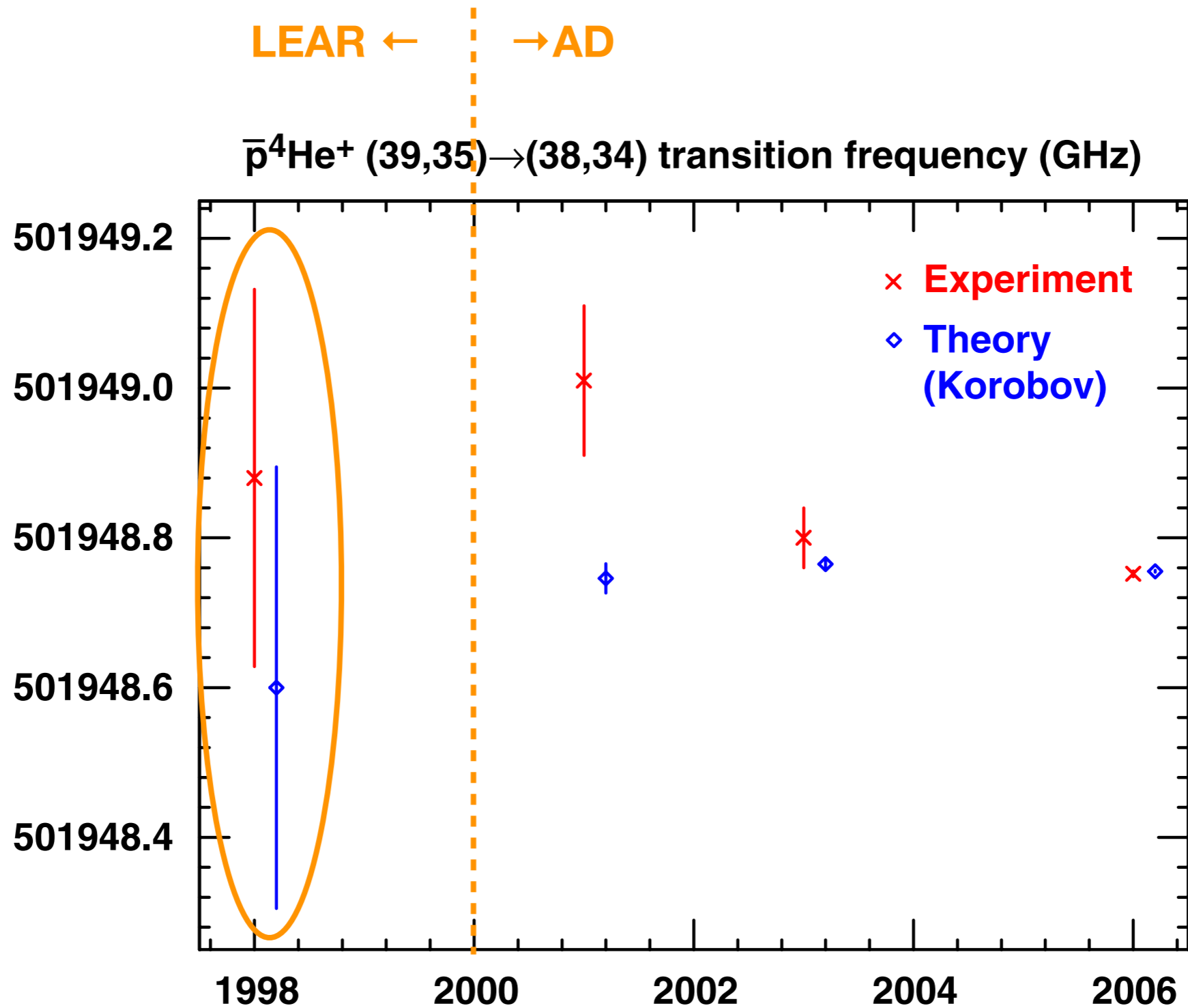
$$E_{se} = \frac{4\alpha^3}{3m_e^2} \left[\ln \frac{1}{\alpha^2} - \ln \frac{k_0}{R_\infty} + \frac{5}{6} - \frac{3}{8} \right] \langle Z_{\text{He}} \delta(\mathbf{r}_{\text{He}}) + Z_p^- \delta(\mathbf{r}_p^-) \rangle$$

$$+ \frac{4\alpha^4}{3m_e^2} \left[3\pi \left(\frac{139}{128} - \frac{1}{2} \ln 2 \right) \right] \langle Z_{\text{He}}^2 \delta(\mathbf{r}_{\text{He}}) + Z_p^-^2 \delta(\mathbf{r}_p^-) \rangle$$

$$- \frac{4\alpha^5}{3m_e^2} \left[\frac{3}{4} \right] \langle Z_{\text{He}}^3 \ln^2(Z_{\text{He}} \alpha)^{-2} \delta(\mathbf{r}_{\text{He}}) \rangle$$

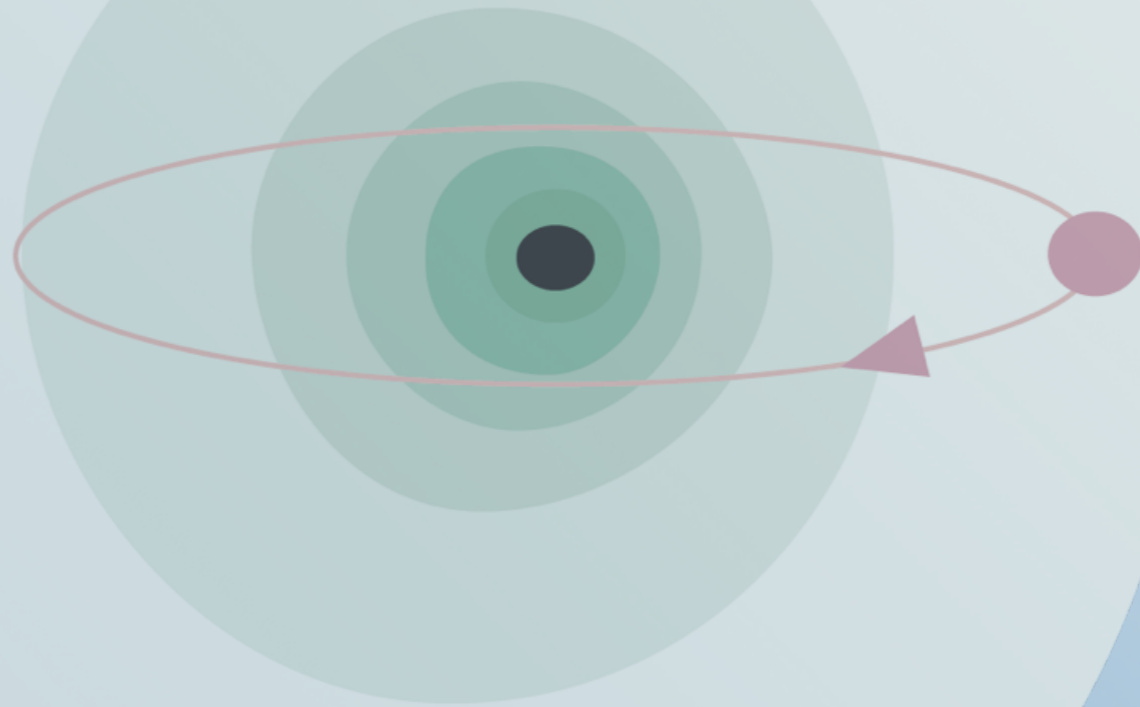
$$+ Z_p^-^3 \ln^2(Z_p^- \alpha)^{-2} \delta(\mathbf{r}_p^-) \rangle,$$

Theory vs experiment

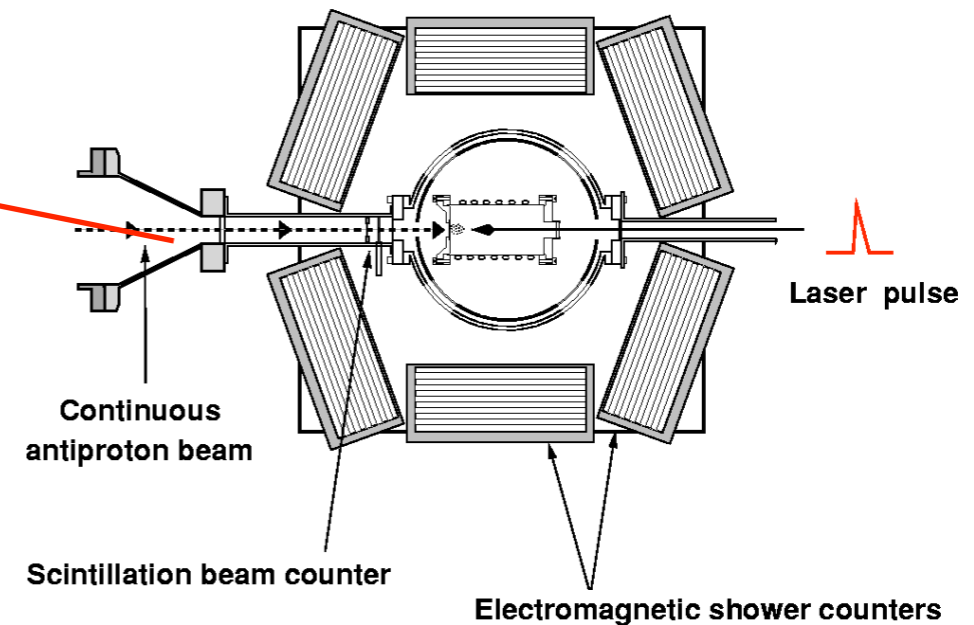
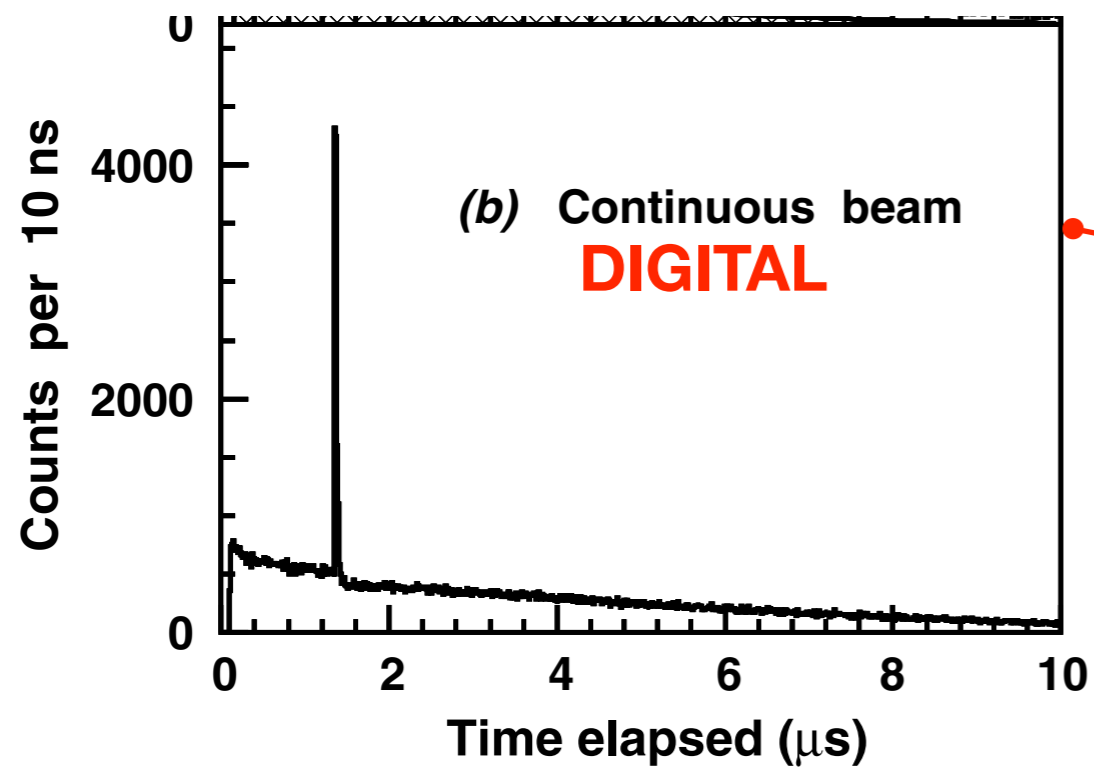


ASACUSA @ CERN AD

How to work with pulsed \bar{p} ?

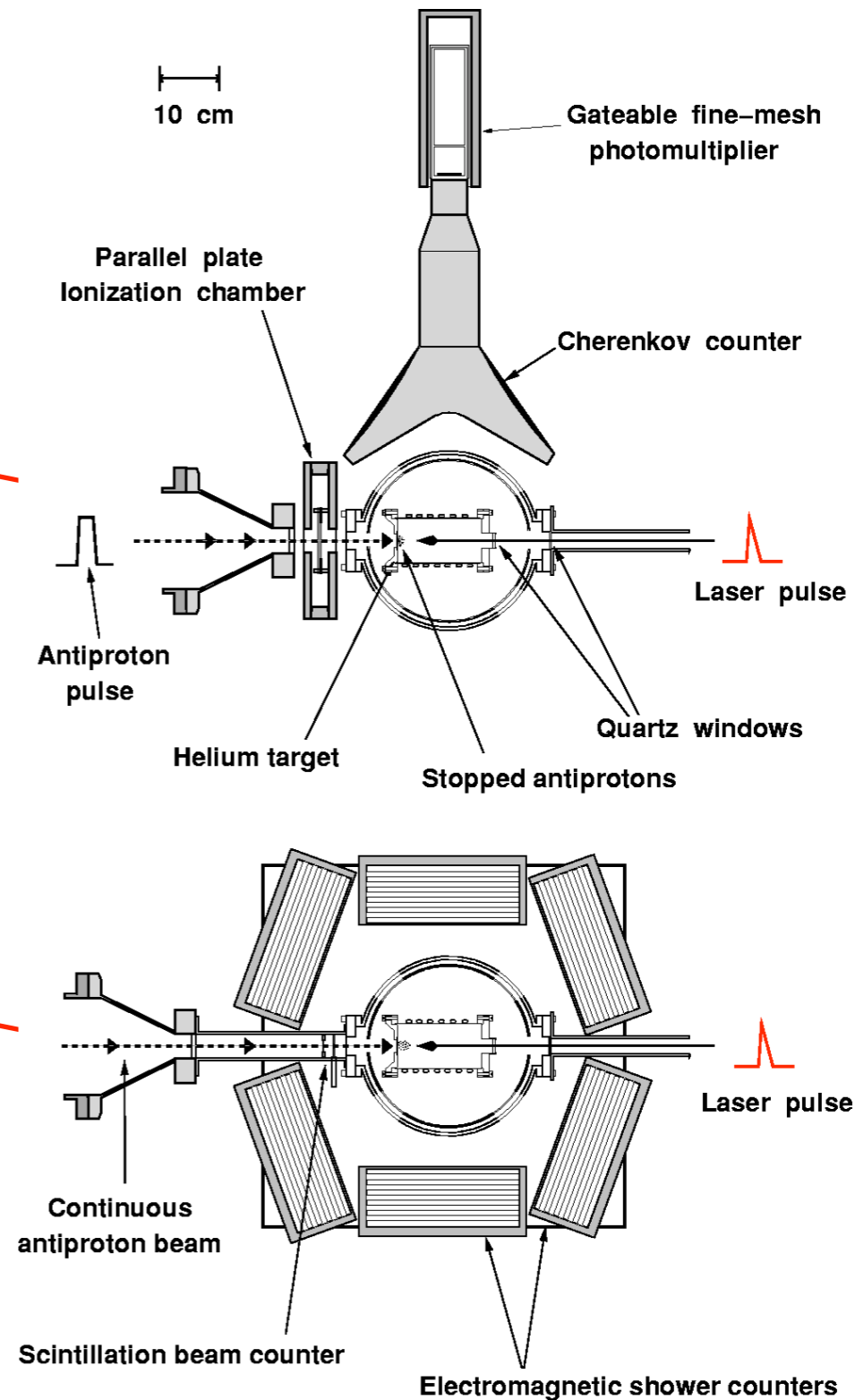
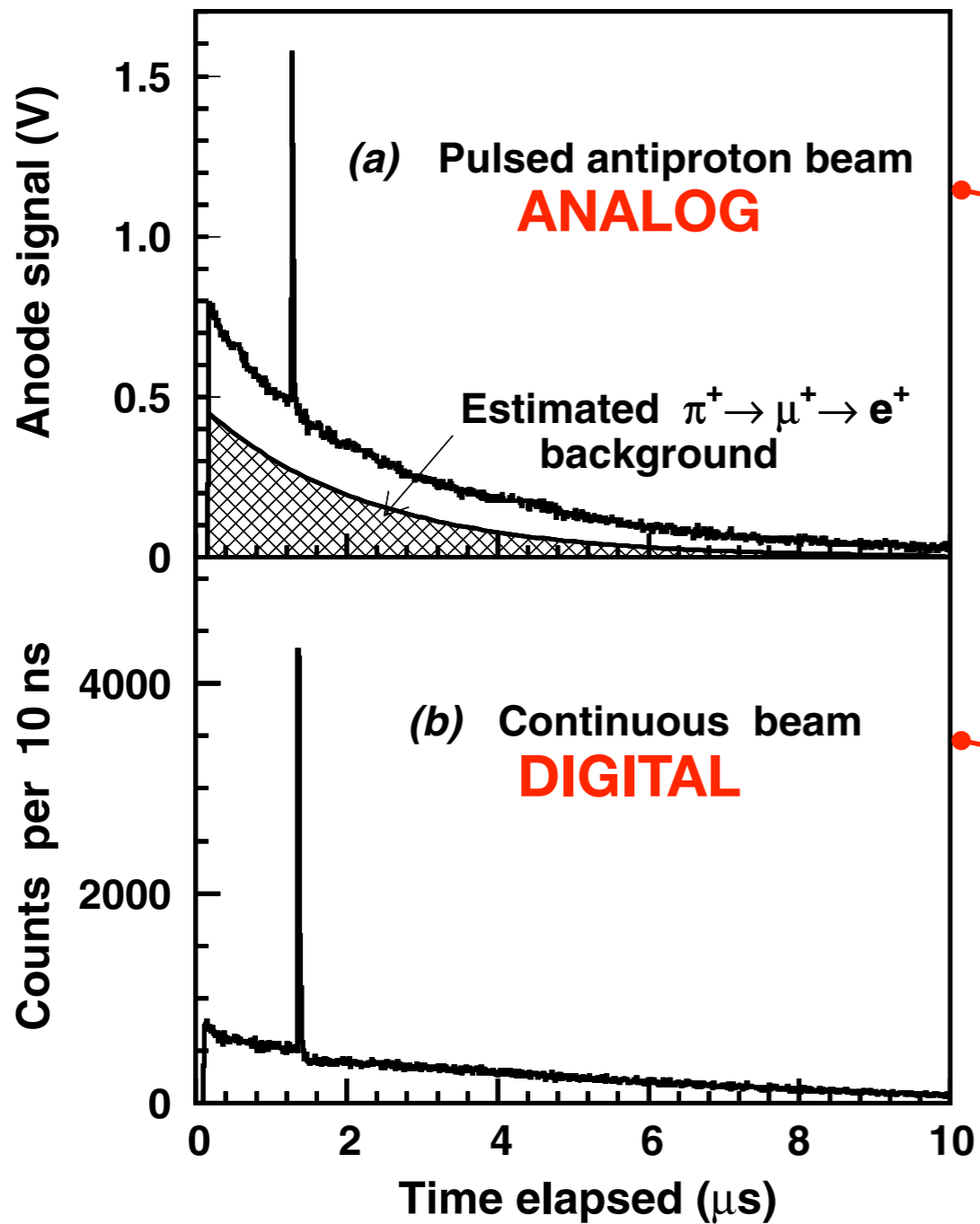


Conventional event-by-event counting

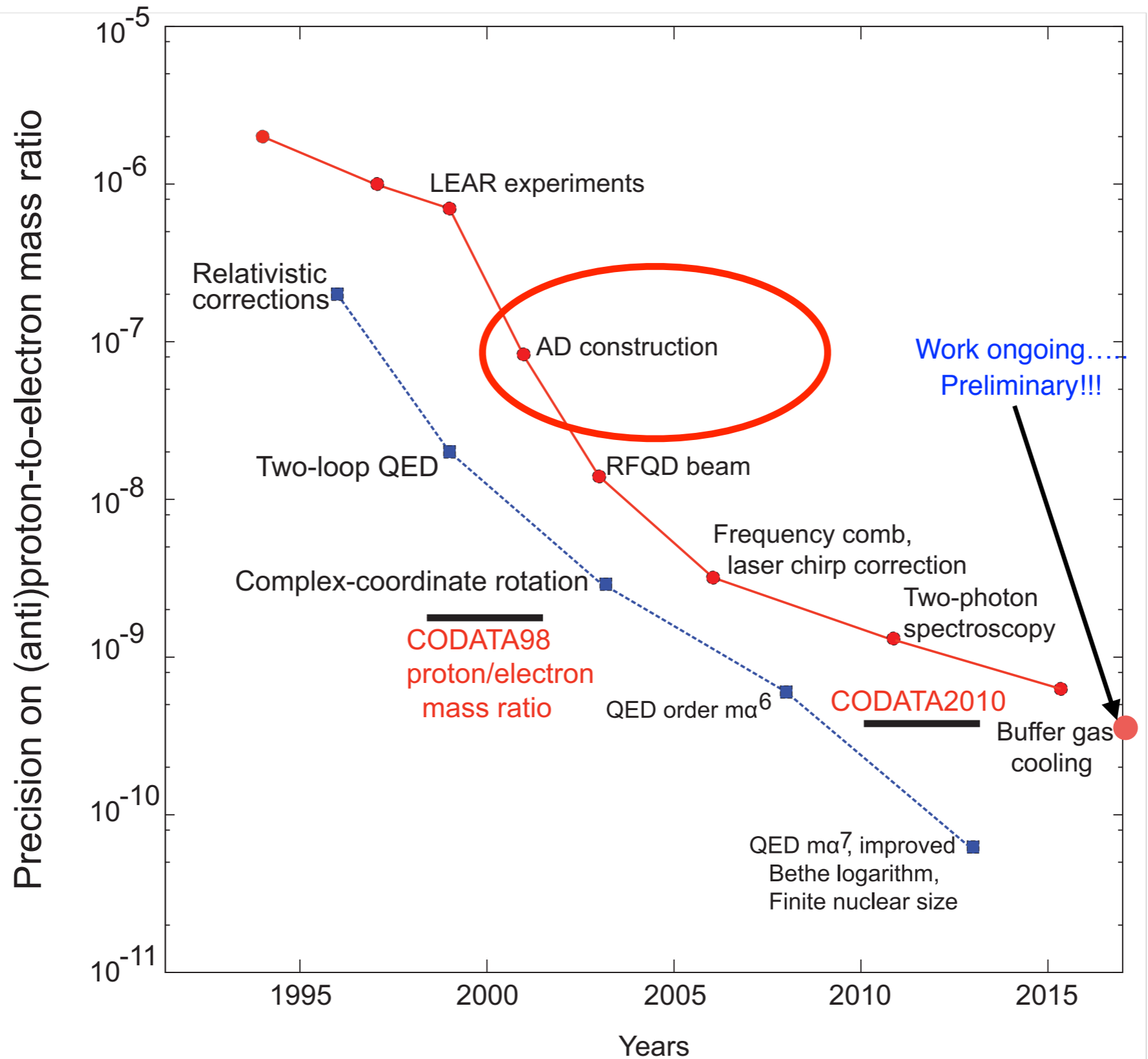


M. Hori et al., PHYSICAL REVIEW A 70, 012504 (2004).

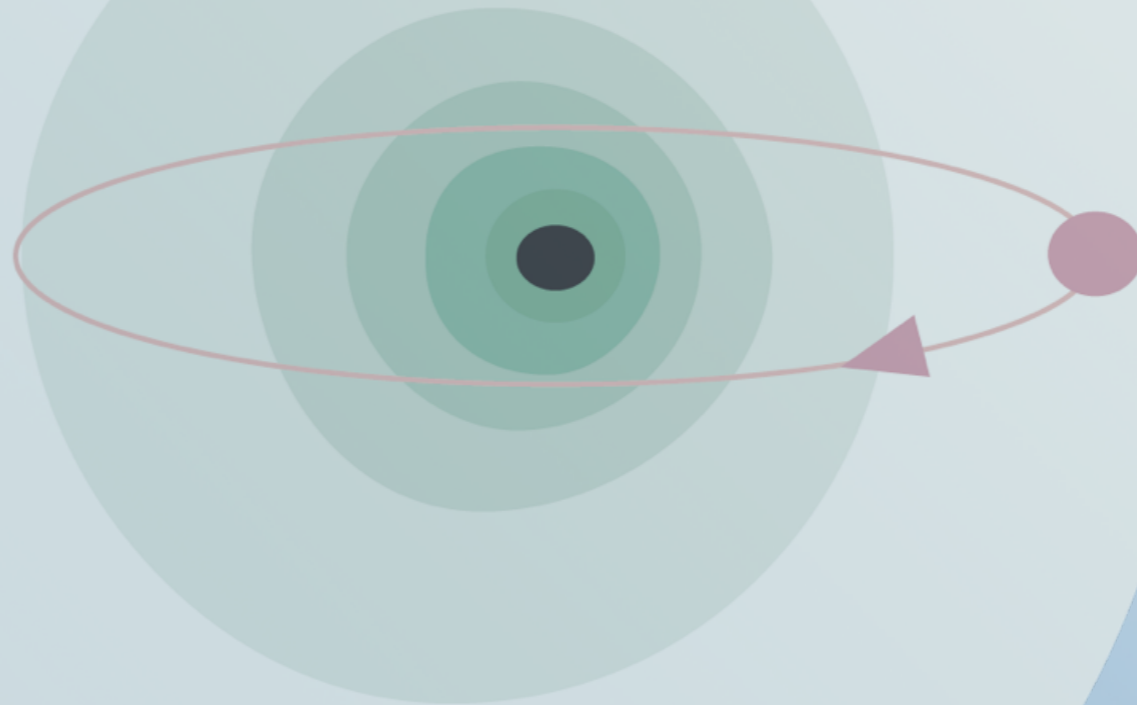
Can't use event-by-event counting



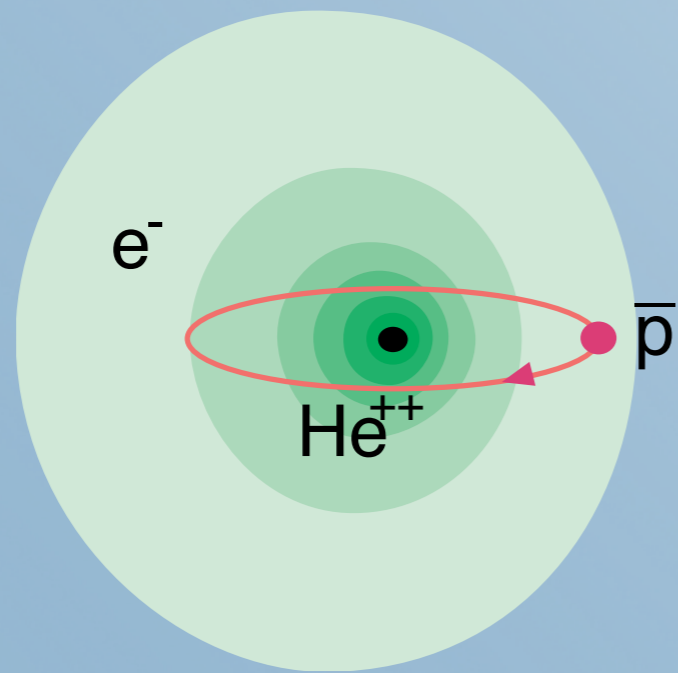
M. Hori et al., PHYSICAL REVIEW A 70, 012504 (2004).



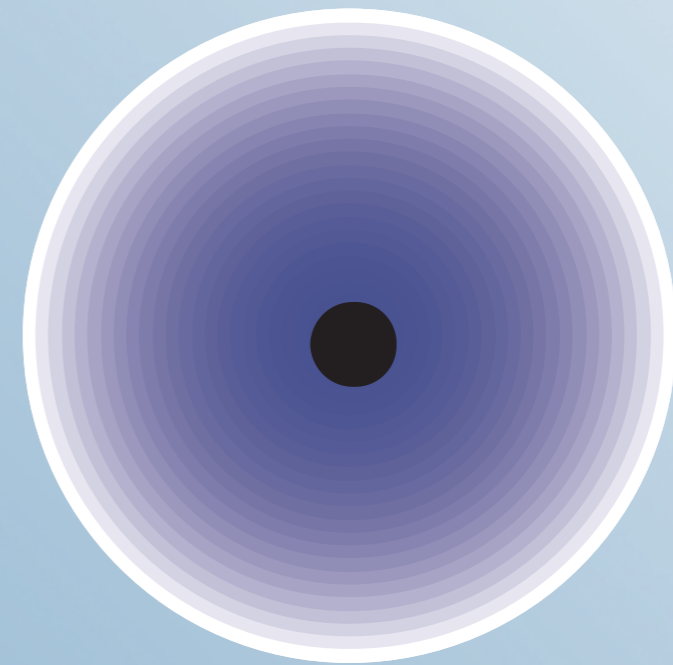
reducing collisions



$\bar{p}\text{He}$ - He collisions do not destroy $\bar{p}\text{He}$
but have consequences

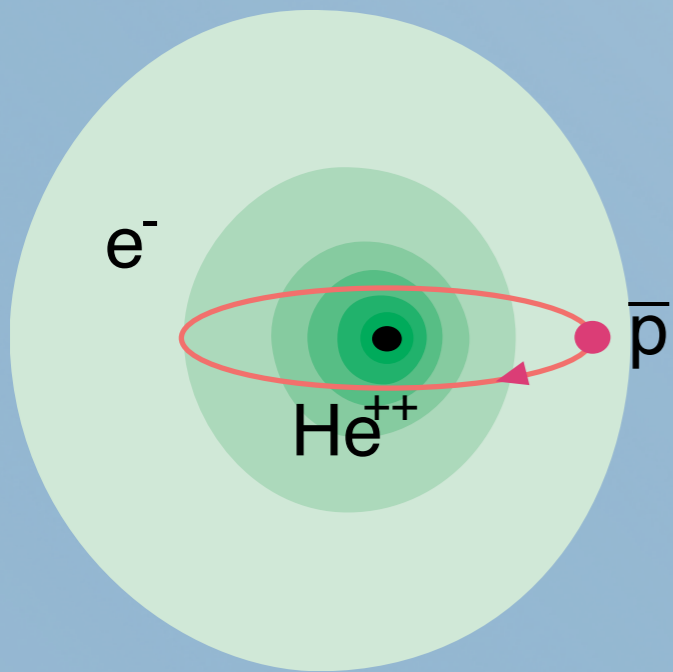


$\bar{p}\text{He}$



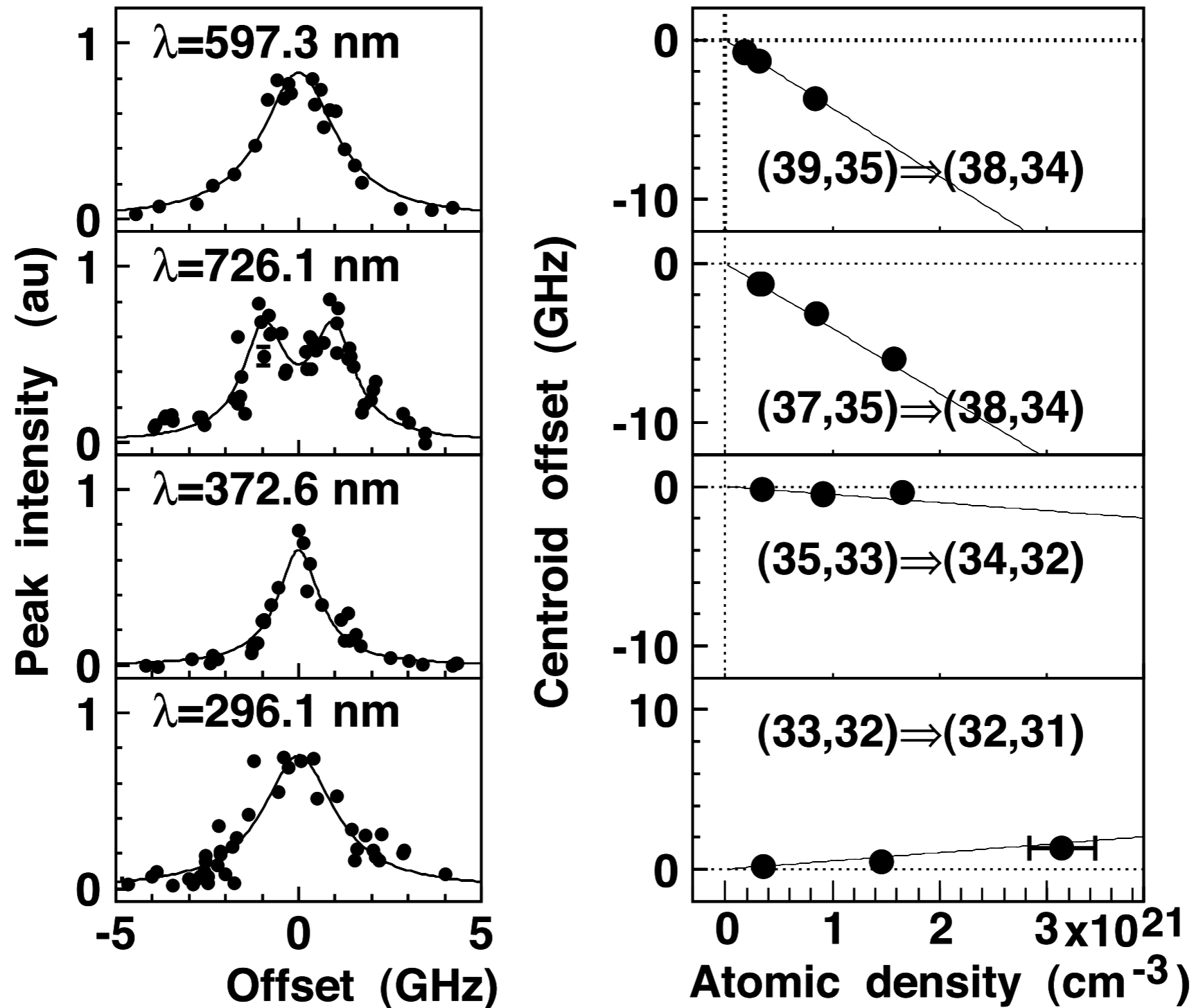
He

$\bar{p}\text{He} - \text{He}$ collisions do not destroy $\bar{p}\text{He}$
 He
but have consequences

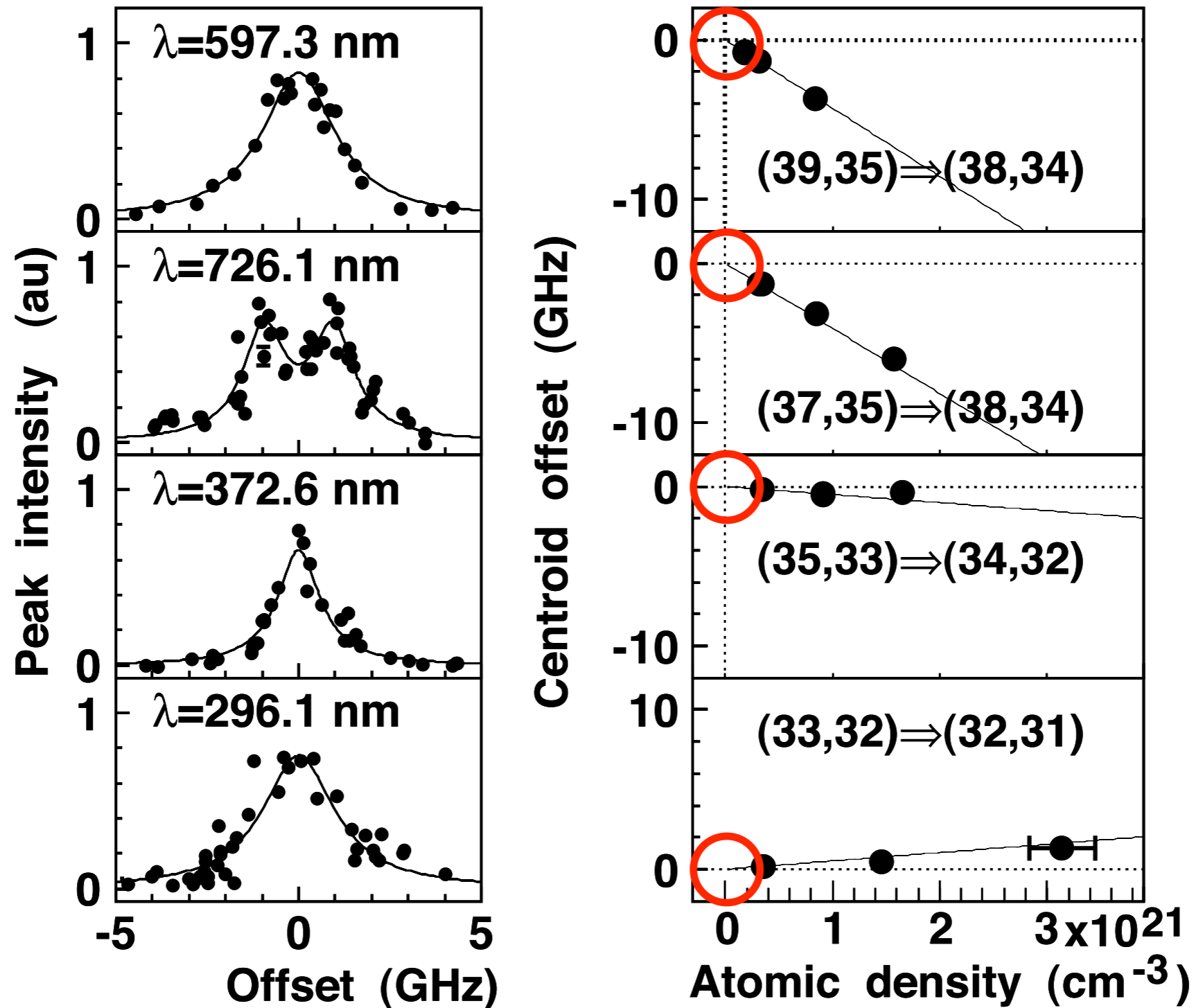


$\bar{p}\text{He}$

Density-dependent shift

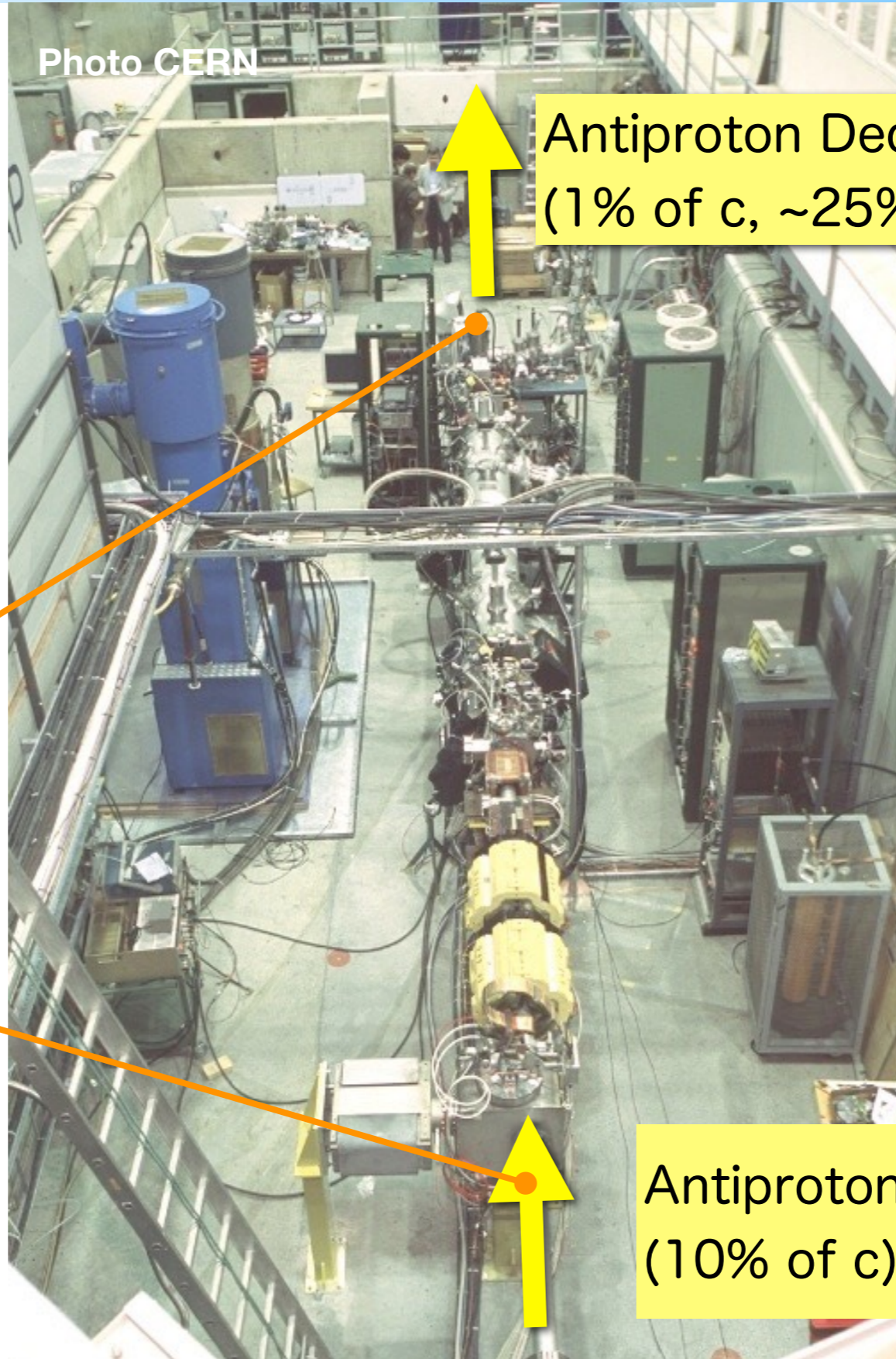


Density-dependent shift



RFQD

Photo CERN



Antiproton Decelerator
(1% of c, ~25% efficiency)

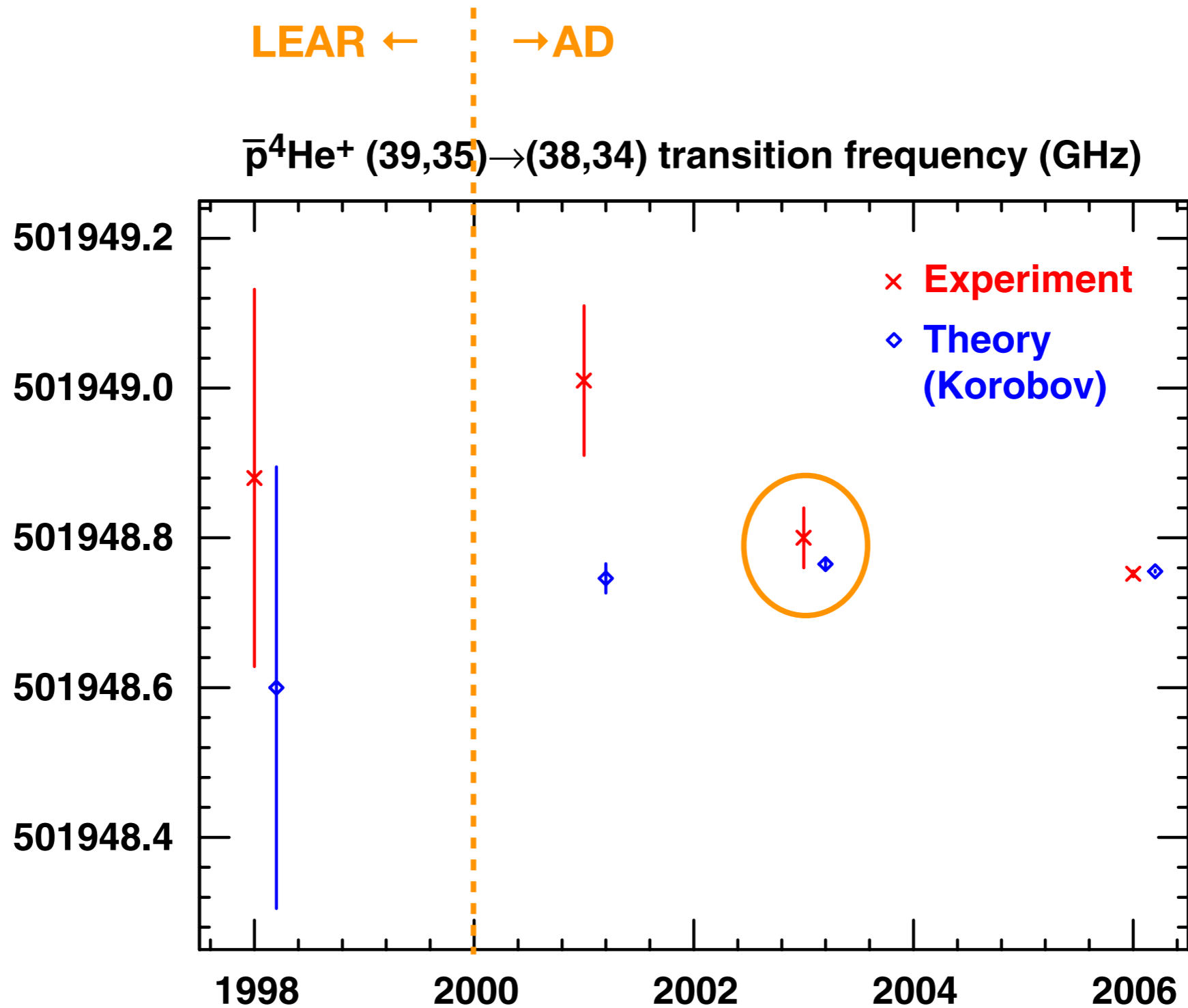
Typical target density

$10^{16} - 10^{18} \text{cm}^{-3}$

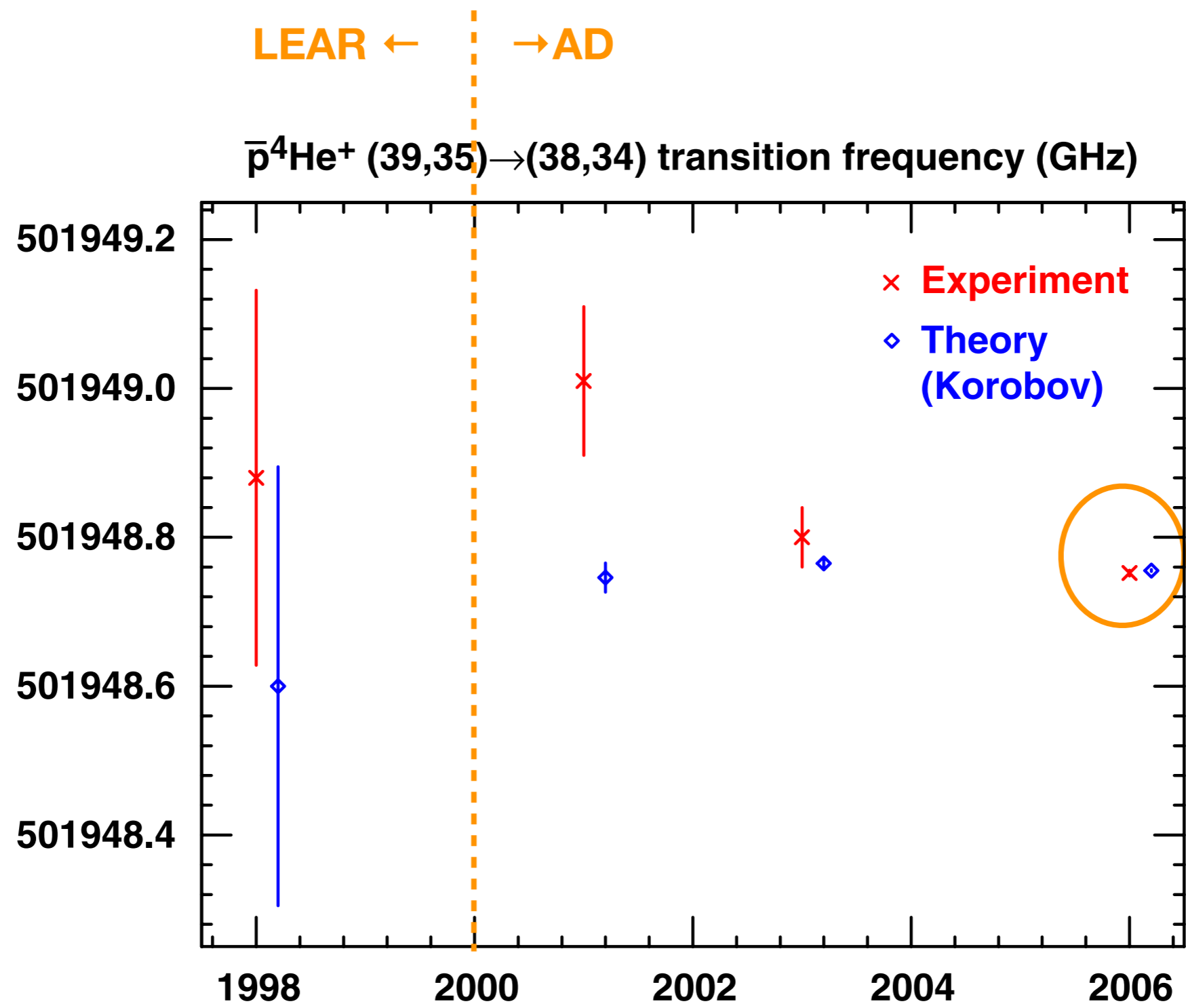
10^{21}cm^{-3}

Antiproton pulse from AD
(10% of c)

“Direct” measurement w RFQD



with RFQD+Comb



An example (39,35) → (38,34)

E_{nr}	=	501 972 347.9	Non relativistic
E_{rc}	=	-27 525.3	+ Relativistic & QED corrections
E_{rc-qed}	=	233.3	
E_{se}	=	3 818.0	
E_{vp}	=	-122.5	
E_{kin}	=	37.3	
E_{exch}	=	-34.7	
E_{α^3-rec}	=	0.8	
$E_{two-loop}$	=	0.9	
E_{nuc}	=	2.4	
E_{α^4}	=	-2.6	

$$\Delta E_{vp} = \frac{4z_i\alpha^3}{3m_3^2} \left[-\frac{1}{5} + (z_i\alpha)\pi \frac{5}{64} \right] \langle \delta(\mathbf{r}_i) \rangle,$$

$$\Delta E_{kin} = \alpha^2 \left\langle -\frac{\nabla_1^4}{8m_1^3} - \frac{\nabla_2^4}{8m_2^3} + \frac{(1+2a_2)z_2}{8m_2^2} 4\pi\delta(\mathbf{r}_2) \right\rangle,$$

$$\Delta E_{exch} = -\alpha^2 \frac{z_i}{2m_i m_3} \left\langle \frac{\nabla_i \nabla_3}{r_i} + \frac{\mathbf{r}_i (\mathbf{r}_i \nabla_i) \nabla_3}{r_i^3} \right\rangle,$$

$$\Delta E_{recoil}^{(3)} = \frac{z_i\alpha^3}{m_i m_3} \left\{ \frac{2}{3} \left(-\ln\alpha - 4\beta + \frac{31}{3} \right) \langle \delta(\mathbf{r}_i) \rangle - \frac{14}{3} \langle Q(\mathbf{r}_i) \rangle \right\},$$

$$\Delta E_{two-loop} = \alpha^4 \frac{z_i}{m_3^2 \pi} \left[-\frac{6131}{1296} - \frac{49\pi^2}{108} + 2\pi^2 \ln 2 - 3\zeta(3) \right] \langle \delta(\mathbf{r}_i) \rangle$$

$$\Delta E_{nuc} = \frac{2\pi z_i (R_i/a_0)^2}{3} \langle \delta(\mathbf{r}_i) \rangle,$$

$$\Delta E_{\alpha^4} \approx -\alpha^4 \frac{\pi}{2} \delta(\mathbf{r}_1).$$

E_{total}	=	501 948 755.6(1.3) MHz	Theory (Korobov)
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	=	501 948 752.0(4.0) MHz	Exp.
		(error)	

12 such transitions
 CODATA 2006

contribution to CODATA, 2006 & 2010

REVIEWS OF MODERN PHYSICS, VOLUME 80, APRIL–JUNE 2008

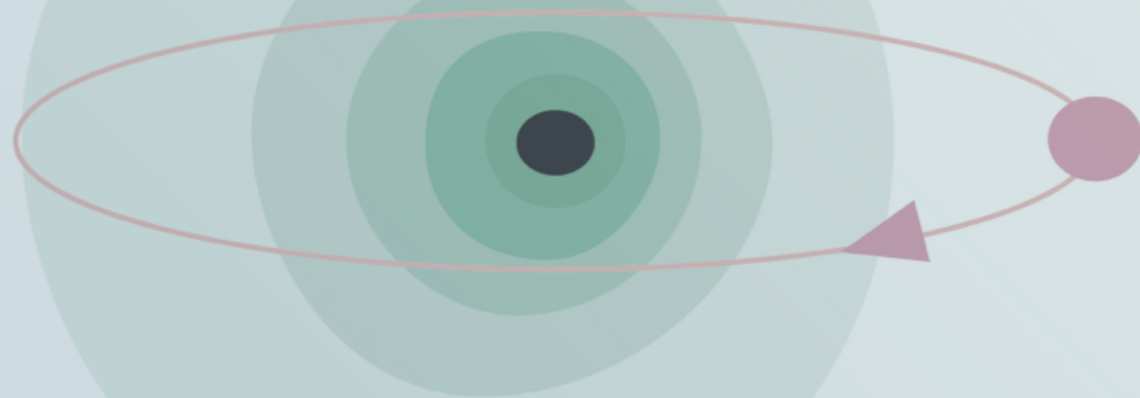
CODATA recommended values of the fundamental physical constants: 2006*

Peter J. Mohr,[†] Barry N. Taylor,[‡] and David B. Newell[§]

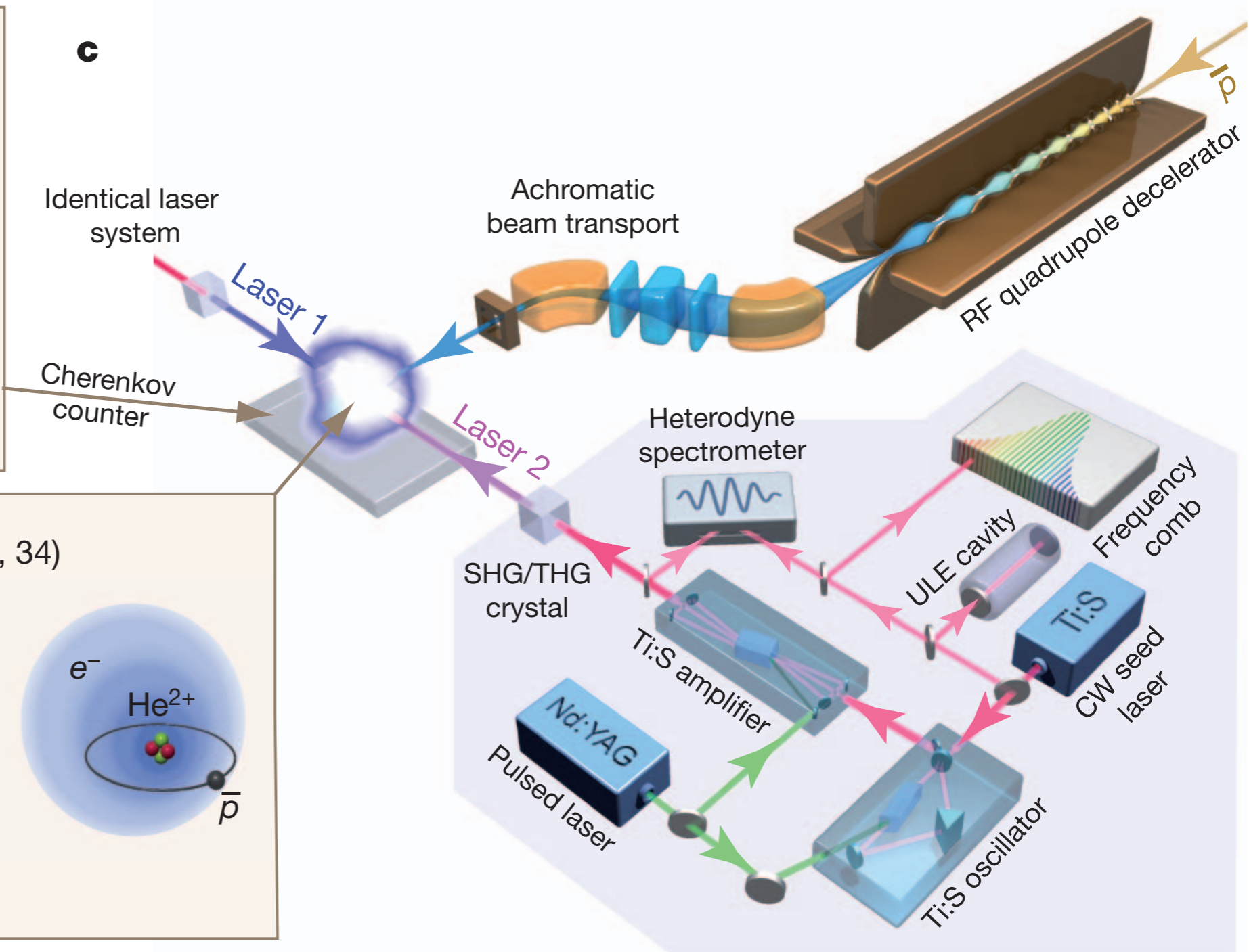
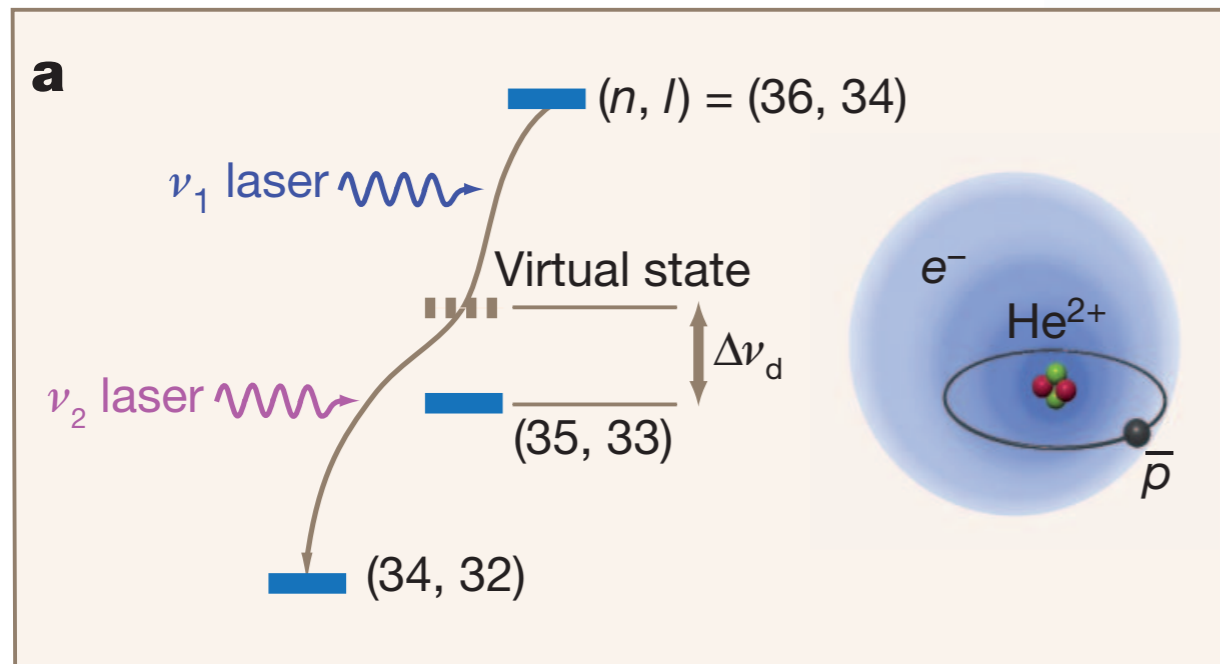
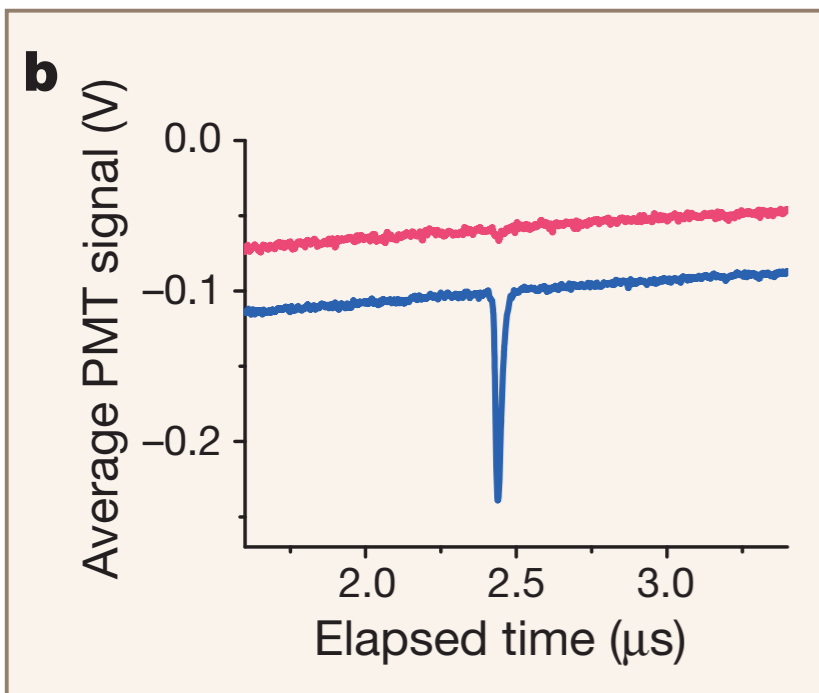
IV. ATOMIC TRANSITION FREQUENCIES

Atomic transition frequencies in hydrogen, deuterium, and antiprotonic helium yield information on the Rydberg constant, the proton and deuteron charge radii, and the relative atomic mass of the electron. The hyper-

Reduce Doppler width 2-photon spectroscopy



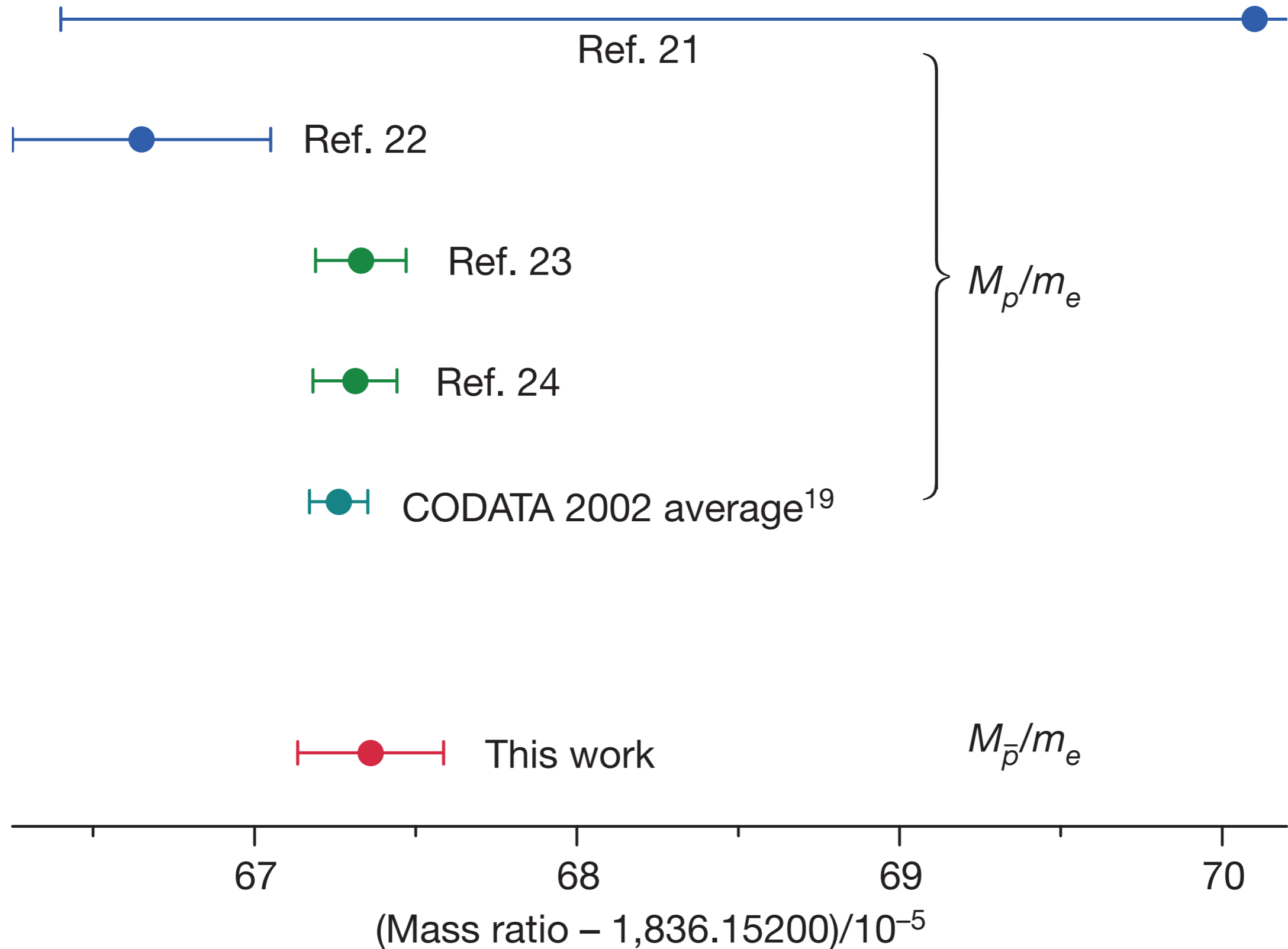
\bar{p} He 2-photon spectroscopy



Hori et al., Nature 475 (2011) 484

m_p/m_e vs $m_{\bar{p}}/m_e$

Hori et al., Nature 475 (2011) 484



How to improve?
theory & exp



Theory progress

PHYSICAL REVIEW A **89**, 014501 (2014)

Bethe logarithm for resonant states: Antiprotonic helium

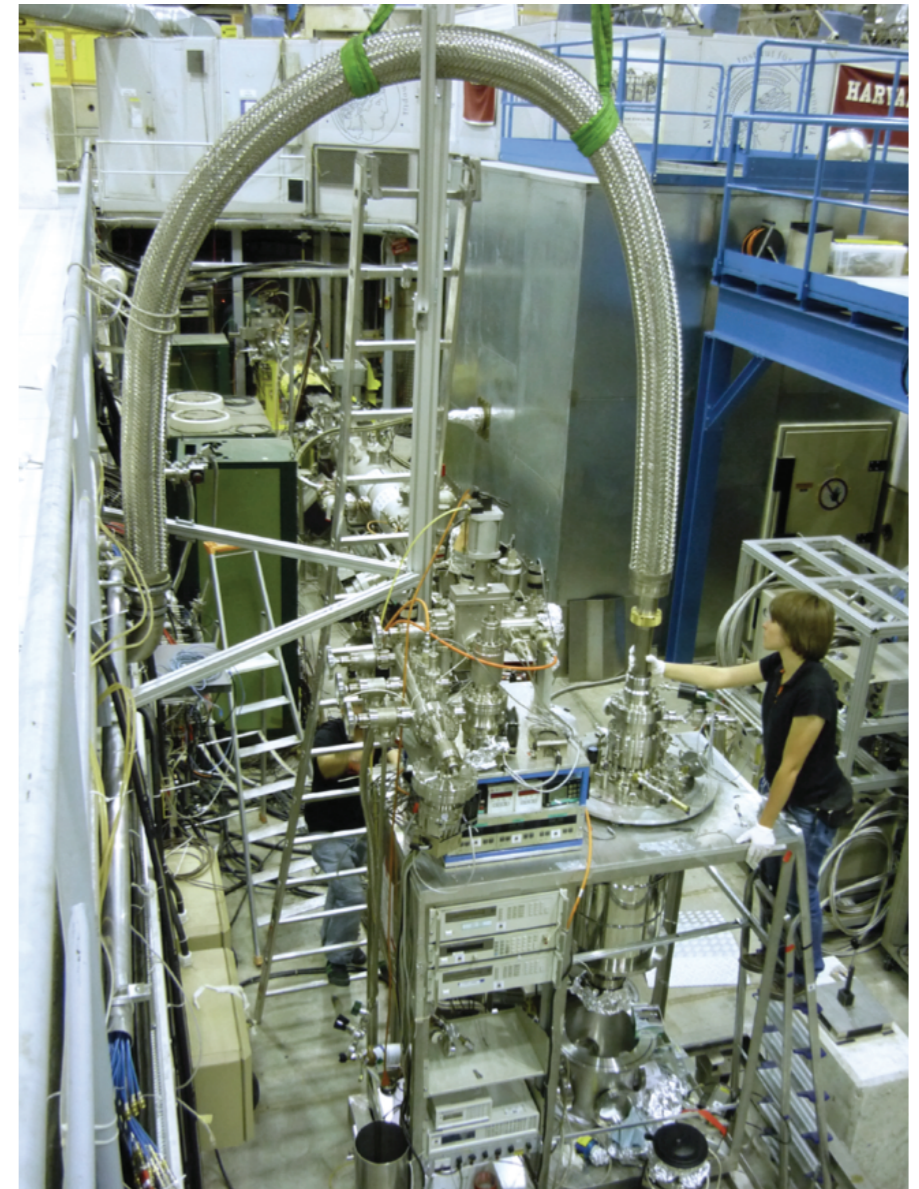
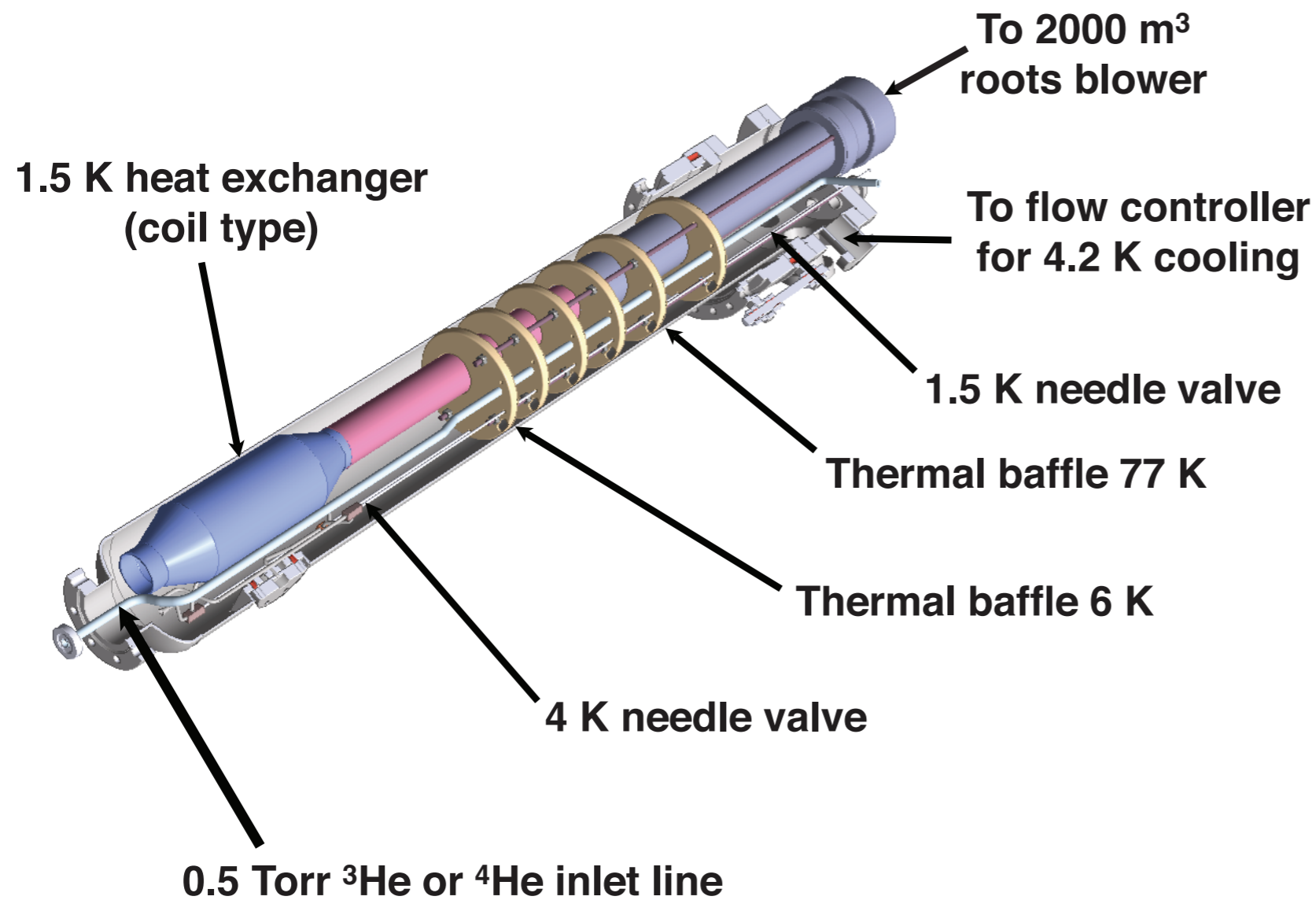
Vladimir I. Korobov

Joint Institute for Nuclear Research 141980, Dubna, Russia

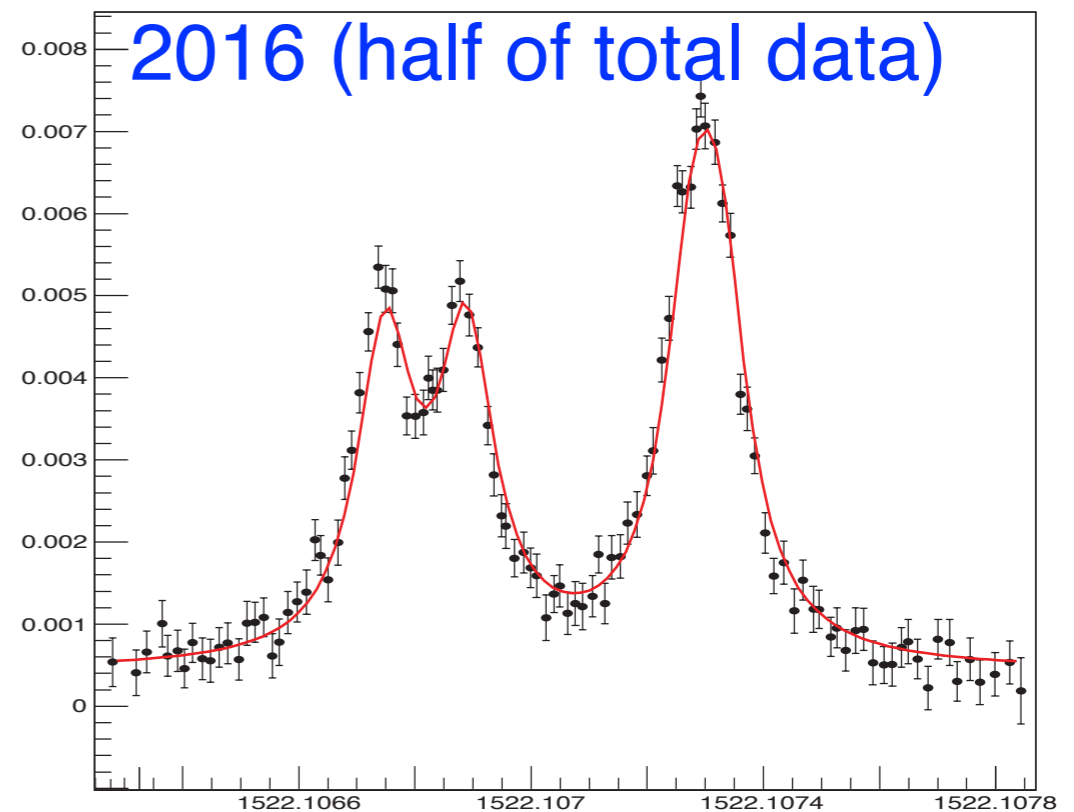
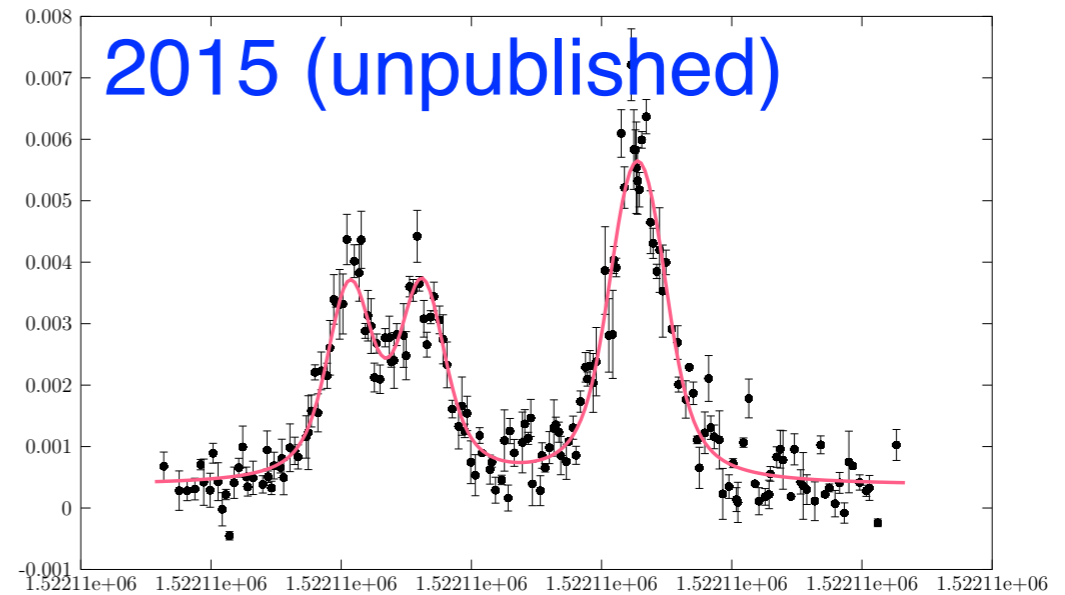
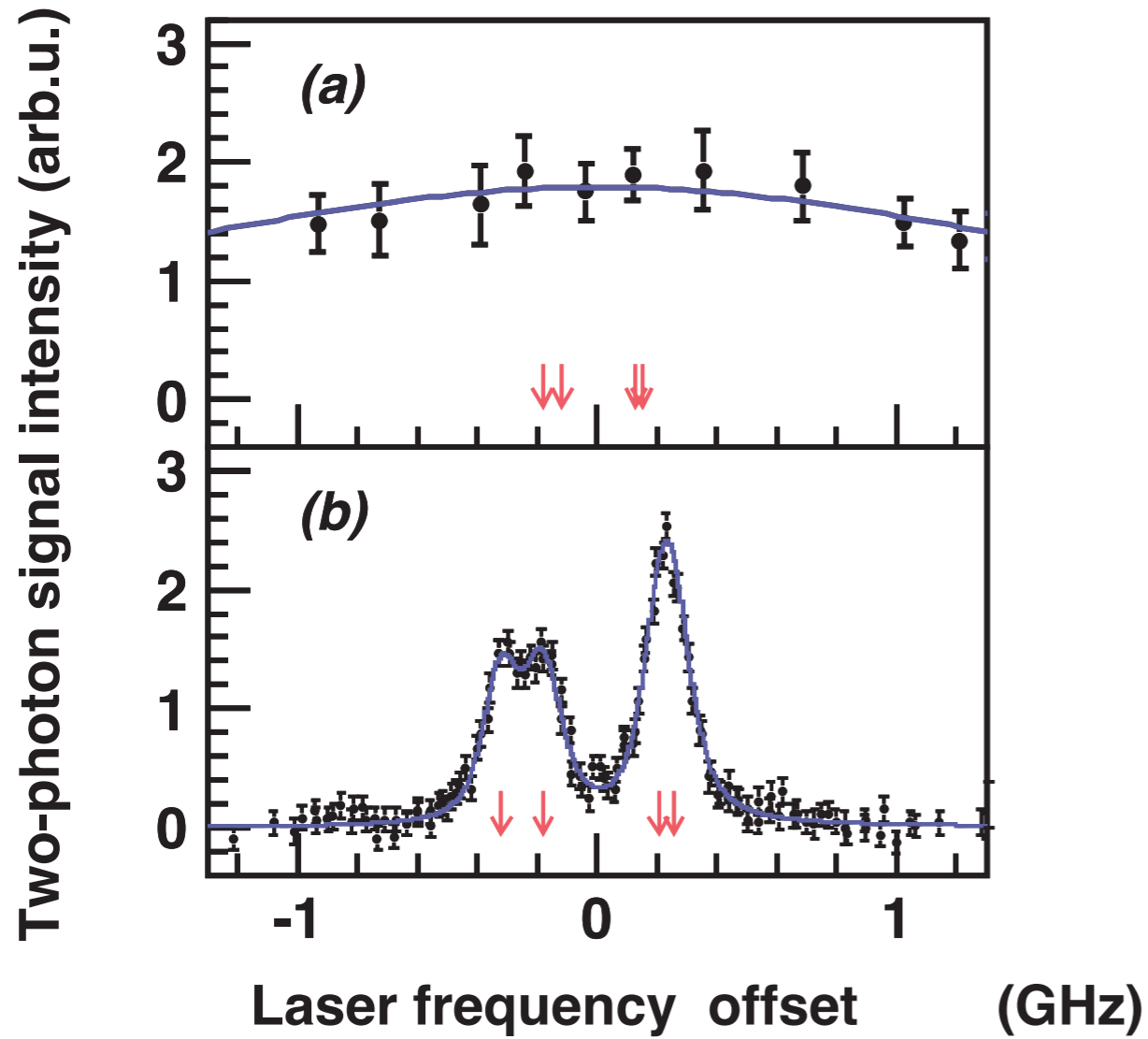
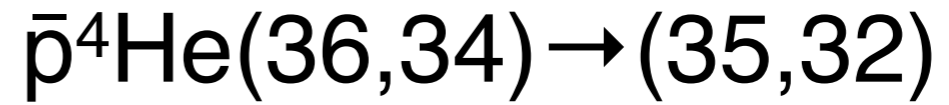
(Received 16 December 2013; published 21 January 2014)

					MHz	
$(33, 32) \rightarrow (31, 30)$	theory	2	145	054	869.9 (1.6)	0.8 ppb
		2	145	054	858.1 (2)	0.09 ppb
<hr/>						
	experiment	2	145	054	858 (5)	2.3 ppb

Experiment - go to 1.5K (and to ELENA)

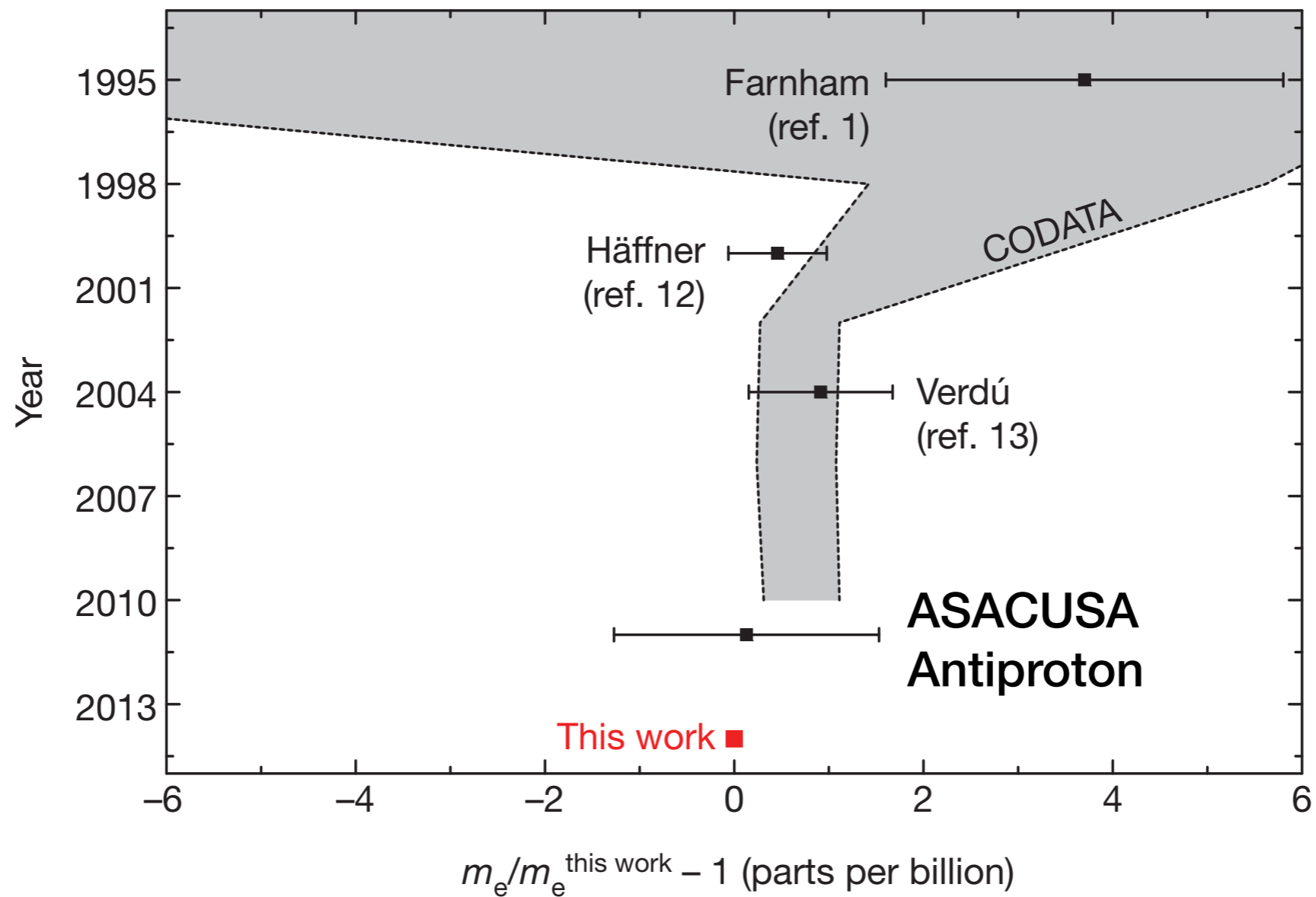


T=1.5K two-photon scan in progress

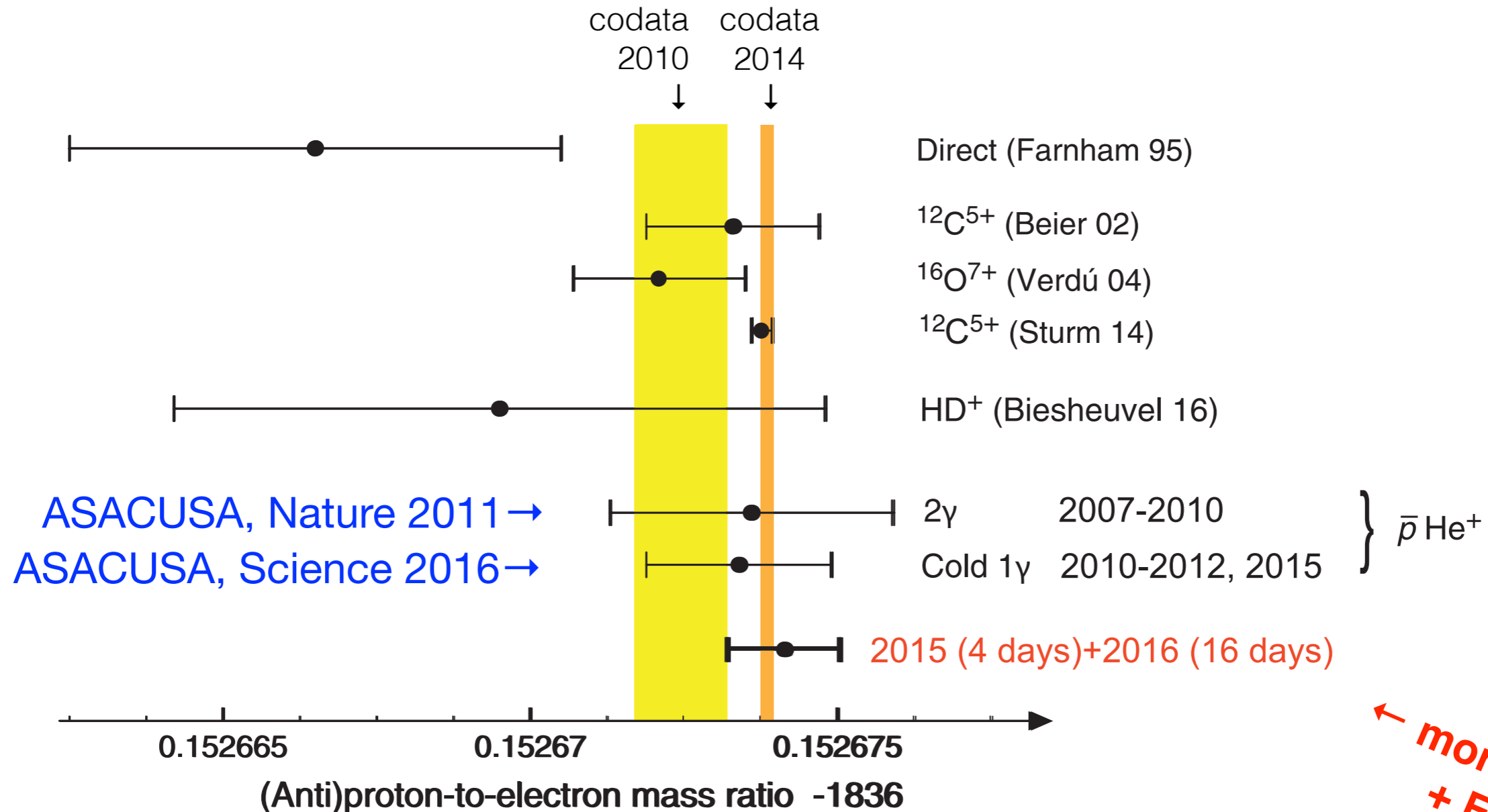


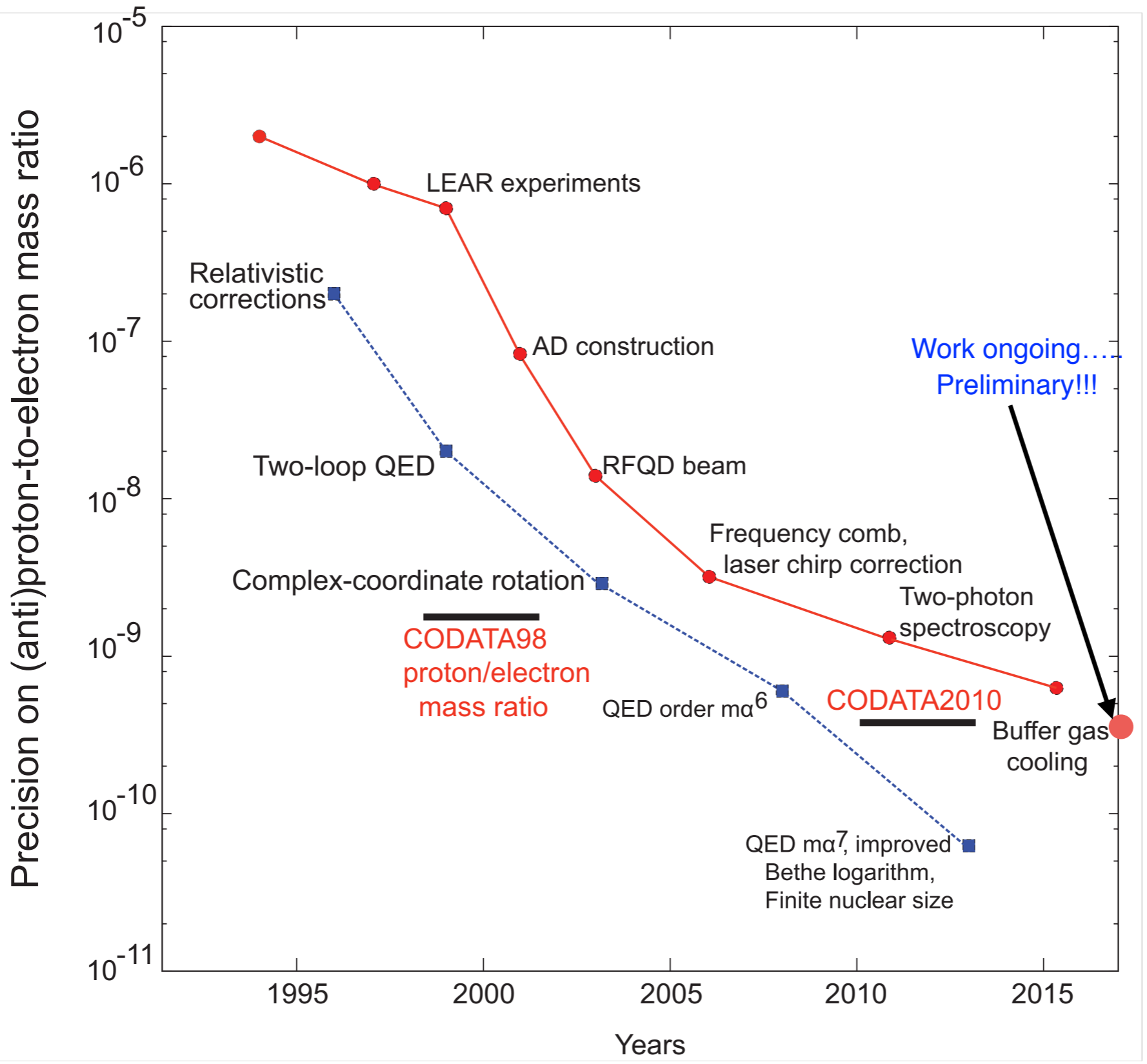
Recently, m_p/m_e much improved

NATURE 506 (2014) 467



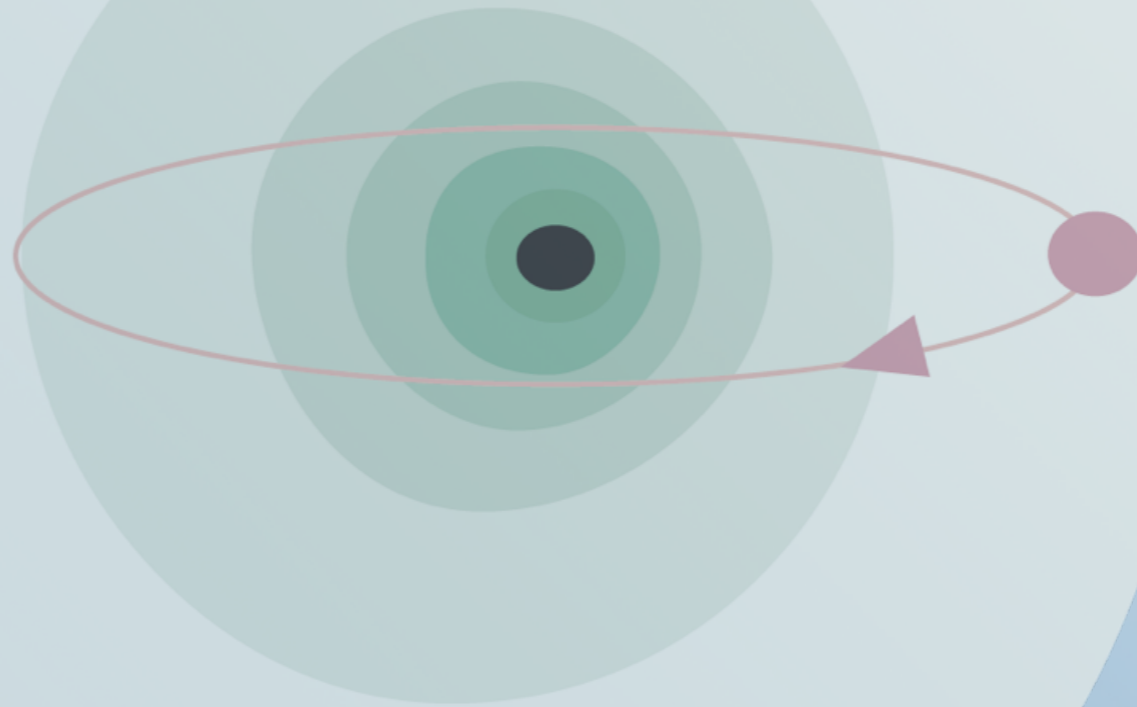
recent (preliminary) result





← *ELENA* →
 ← codata 2014 →

summary



$\bar{p}\text{He}$ contributes to CODATA & tests CPT

Serendipitous discovery

Precision now at $\sim 10^{-9}$ (RFQ, Comb, 2-photon, ...)

Contribute to fundamental constant (m_p/m_e)

Further improvements possible (takes exp/theory efforts), esp. with the ELENA