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# Measurements on the ${}^3\text{He} + \eta$ system at ANKE

## International Symposium on Mesic Nuclei

June 16th, 2010

wissen.leben  
WWU Münster

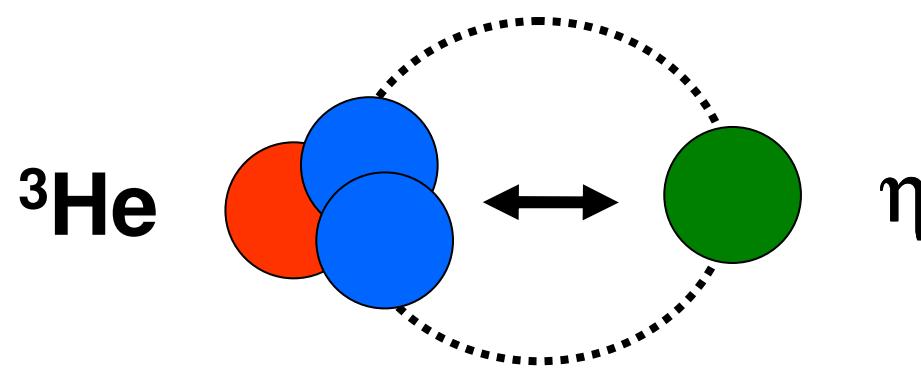
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Institut für Kernphysik



## Why $\eta$ -Meson Production Close to Threshold?

- Do bound meson-nucleus systems exist?



- Investigation of symmetries and conservation laws
- Determination of „technical data“ of elementary particles
  - Mass, life time, ...



# The COSY-Accelerator at Jülich



**COSY (Cooler Synchrotron)**

## Energy range

- 0.045 – 2.8 GeV (p)
- 0.023 – 2.3 GeV (d)  
(momentum 3.7 GeV/c)

## Beam cooling

- Electron cooling
- Stochastic cooling

## Polarisation

- p, d beams & targets

## Beams

- internal, external

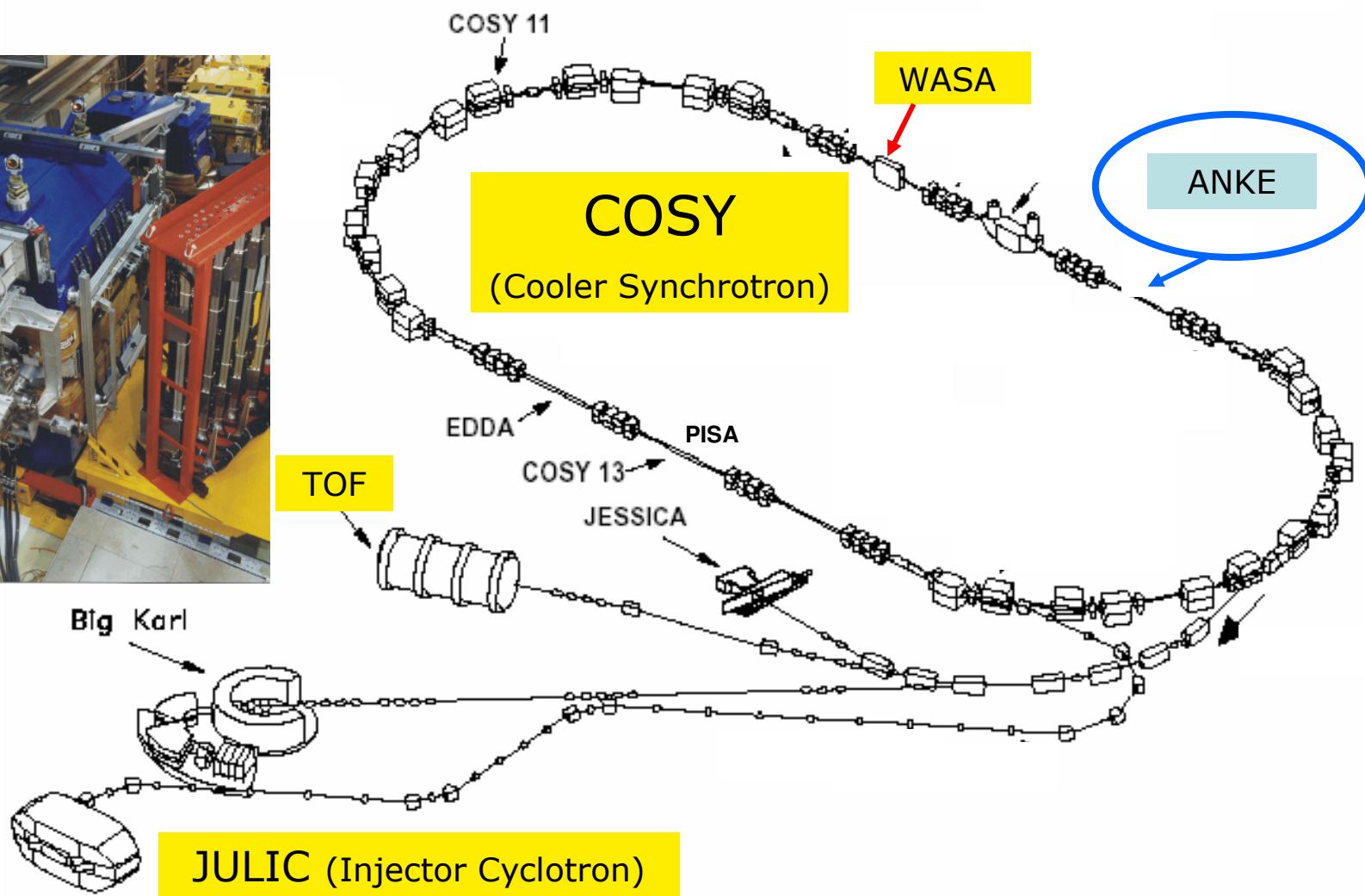
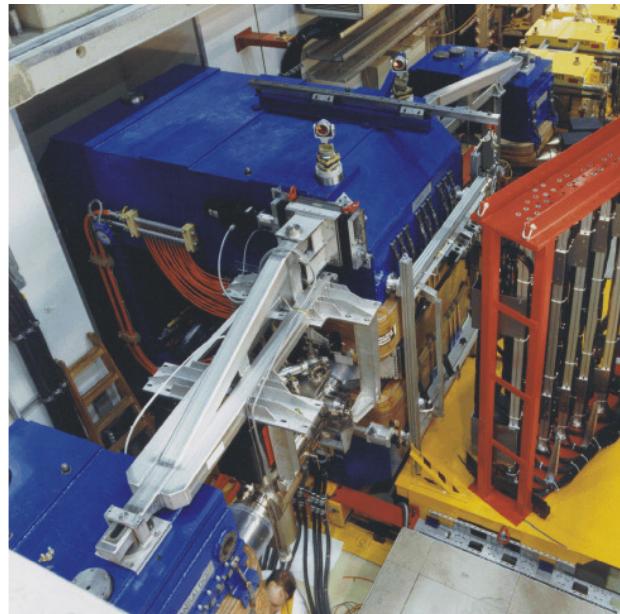
## Experiments, Detectors

- ANKE, TOF, WASA, ...

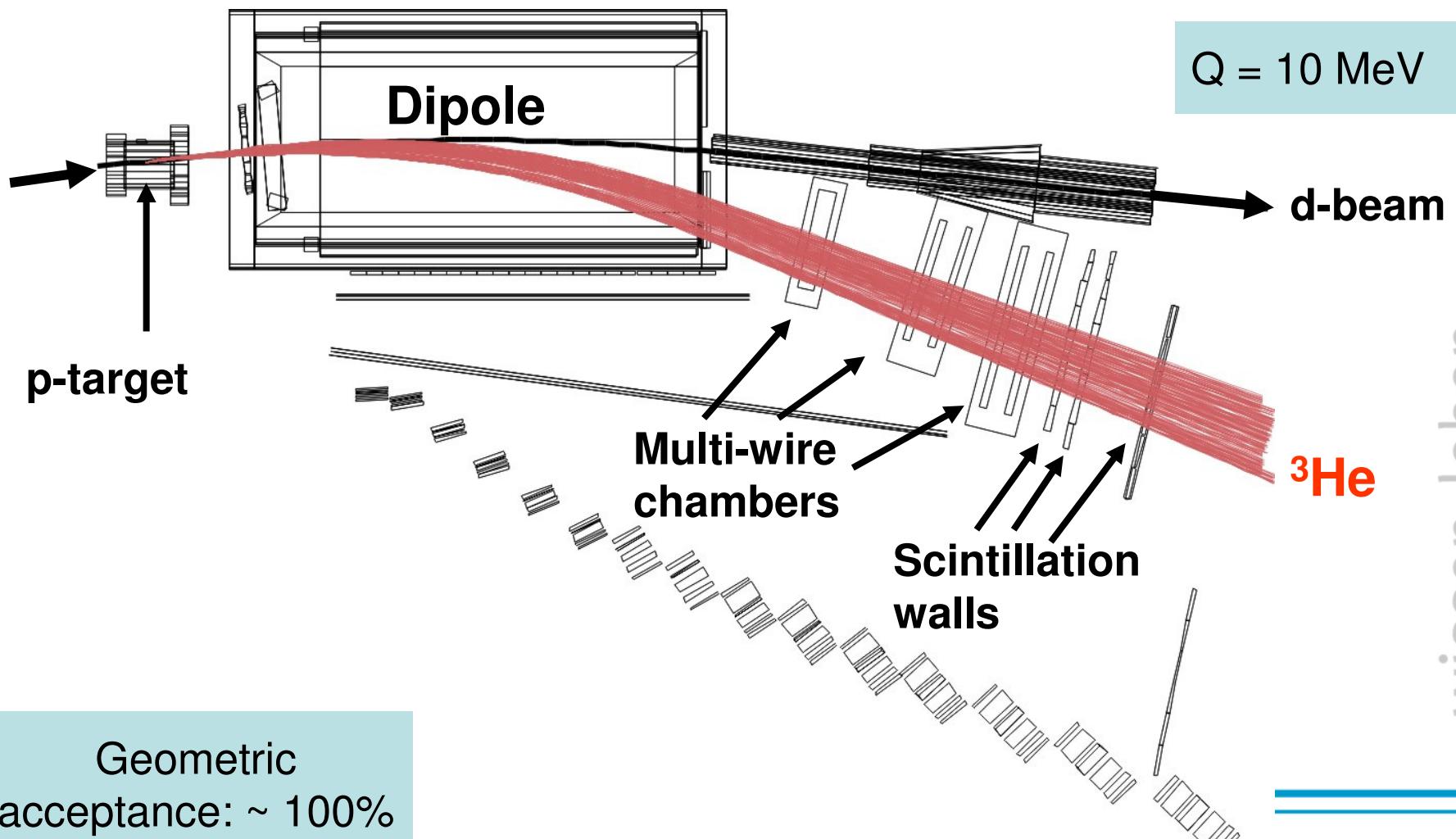


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# The ANKE-Facility

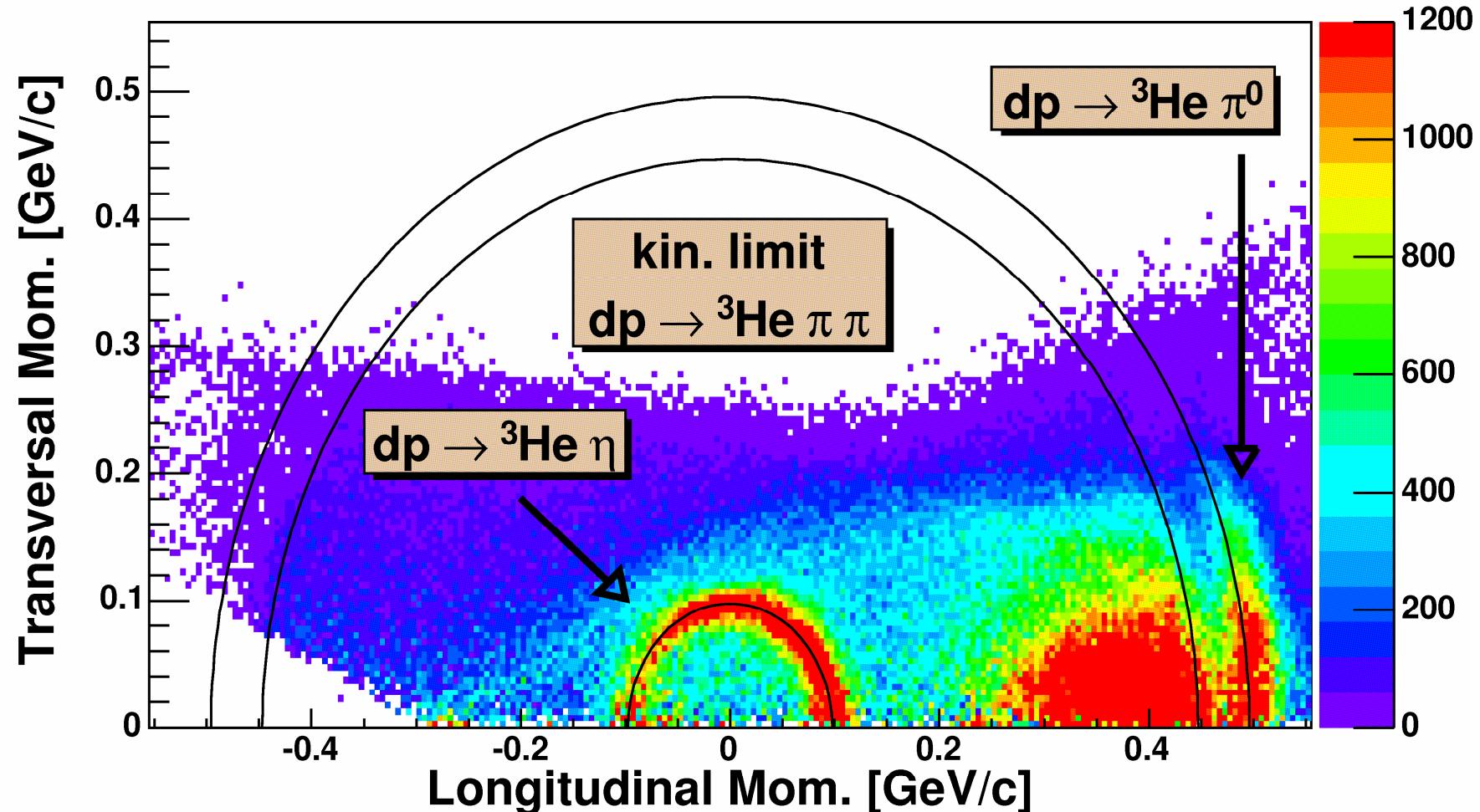


## Identification of ${}^3\text{He}$ Nuclei at ANKE



# Identification of the Reactions: $d+p \rightarrow {}^3\text{He}+X$

„Momentum rabbit“





## Identification of the Reactions: $d+p \rightarrow {}^3\text{He}+X$

- Energies and momenta of the incoming particles ( $d,p$ ) known
  - Deuteron (mass =  $m_d$ ):  
*energy + momentum: Adjustable by the accelerator*
  - Proton (mass =  $m_p$ ):  
*target particle at rest, momentum = 0*
- Energy of the  ${}^3\text{He}$  nucleus measurable by detectors
- $\eta$ -meson: Not directly detectable at ANKE
  - Identification of the reaction via the missing mass analysis

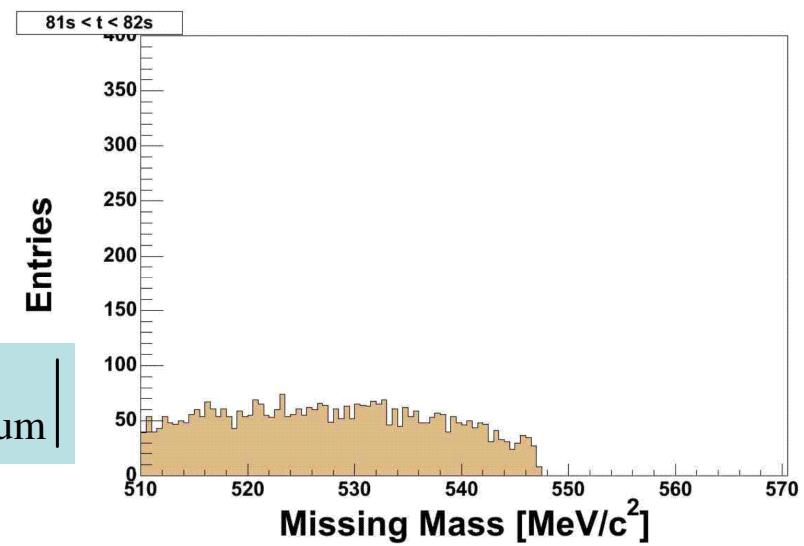
## Identification of the Reactions: $d+p \rightarrow {}^3\text{He}+X$

Missing-mass analysis: Use four-momenta  $P=(E,p_x,p_y,p_z)$

$$P_{\text{Deuteron}} + P_{\text{Proton}} = P_{\text{Helium}} + P_X$$

$$P_X = P_{\text{Deuteron}} + P_{\text{Proton}} - P_{\text{Helium}}$$

$$m_X = |P_X| = |P_{\text{Deuteron}} + P_{\text{Proton}} - P_{\text{Helium}}|$$



$m_X$ : Invariant mass of the not detected system  
(one or more particles)

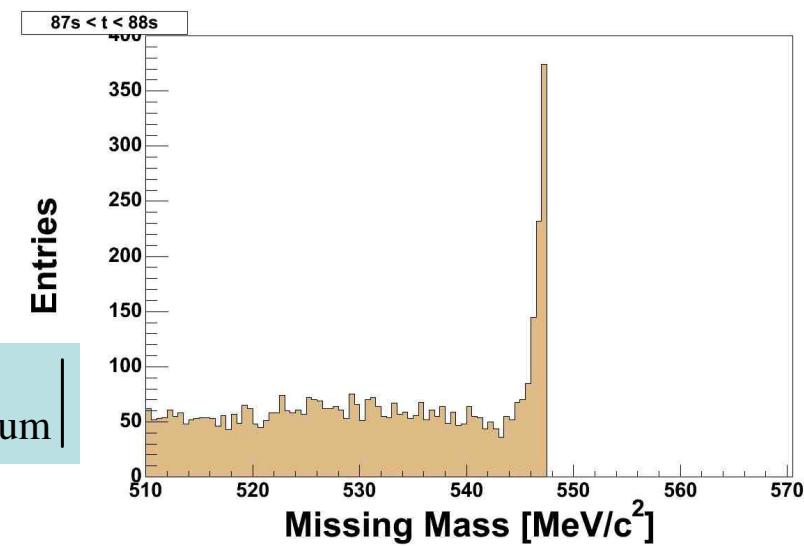
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$$m_X = |P_X| = |P_{\text{Deuteron}} + P_{\text{Proton}} - P_{\text{Helium}}|$$



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## Two-Particle Final State: Phase Space

Assumption:

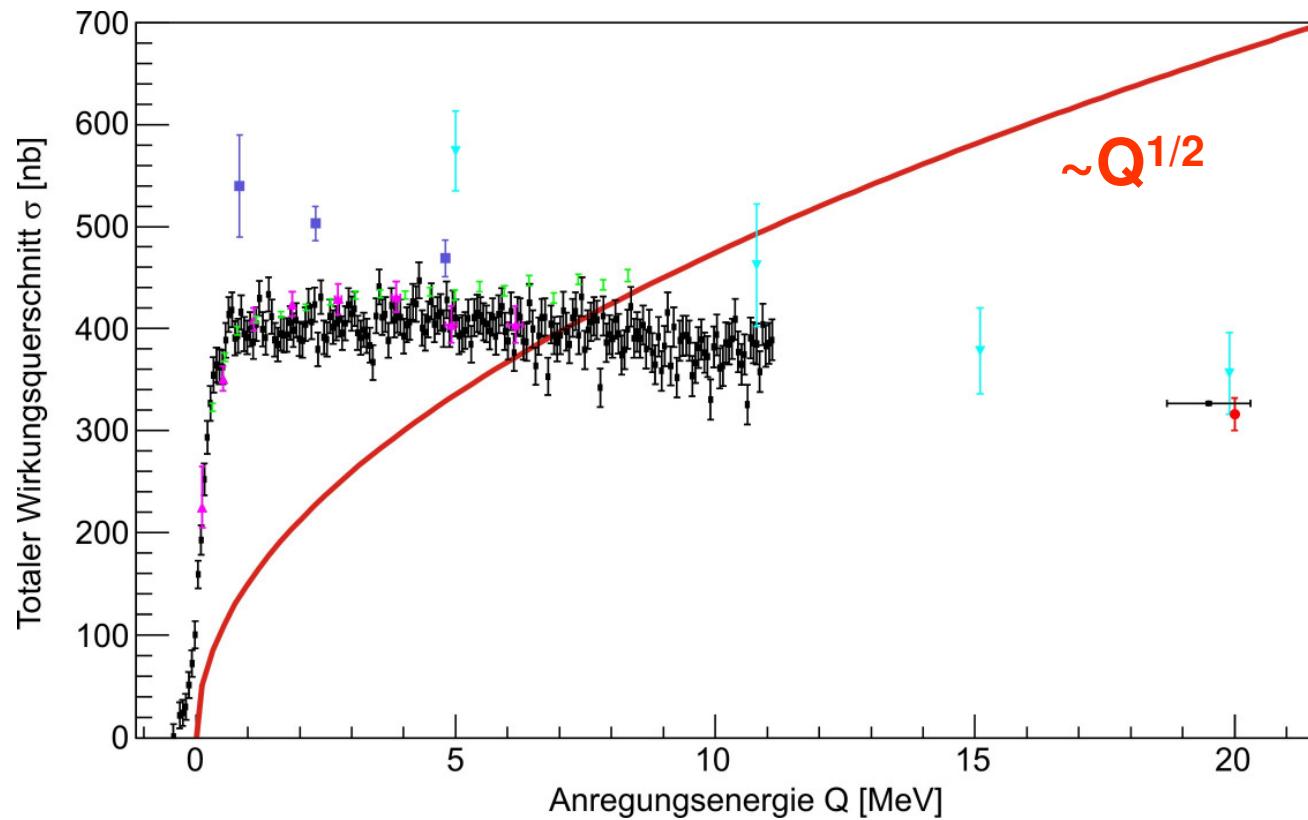
- Two-particle reaction  $a+b \rightarrow c+d$  without initial and final state interactions („ISI“ and „FSI“):
- Scattering (and production) amplitude  $f = \text{const.}$   
→ Increase of the cross section according to phase space expectations

$$\frac{d\sigma(\vartheta)}{d\Omega} = \frac{p_f}{p_i} |f_s|^2 \propto p_f \propto \sqrt{Q}$$

$p_i / p_f$ : Momenta of in- and outgoing particles in the CMS

$Q$ : Q-value = Sum of kinetic energies im CMS

## Results for the Reaction $d+p \rightarrow {}^3\text{He}+\eta$



But:

- Strong deviation from phase space expectation!
- Most probably not caused by higher partial waves



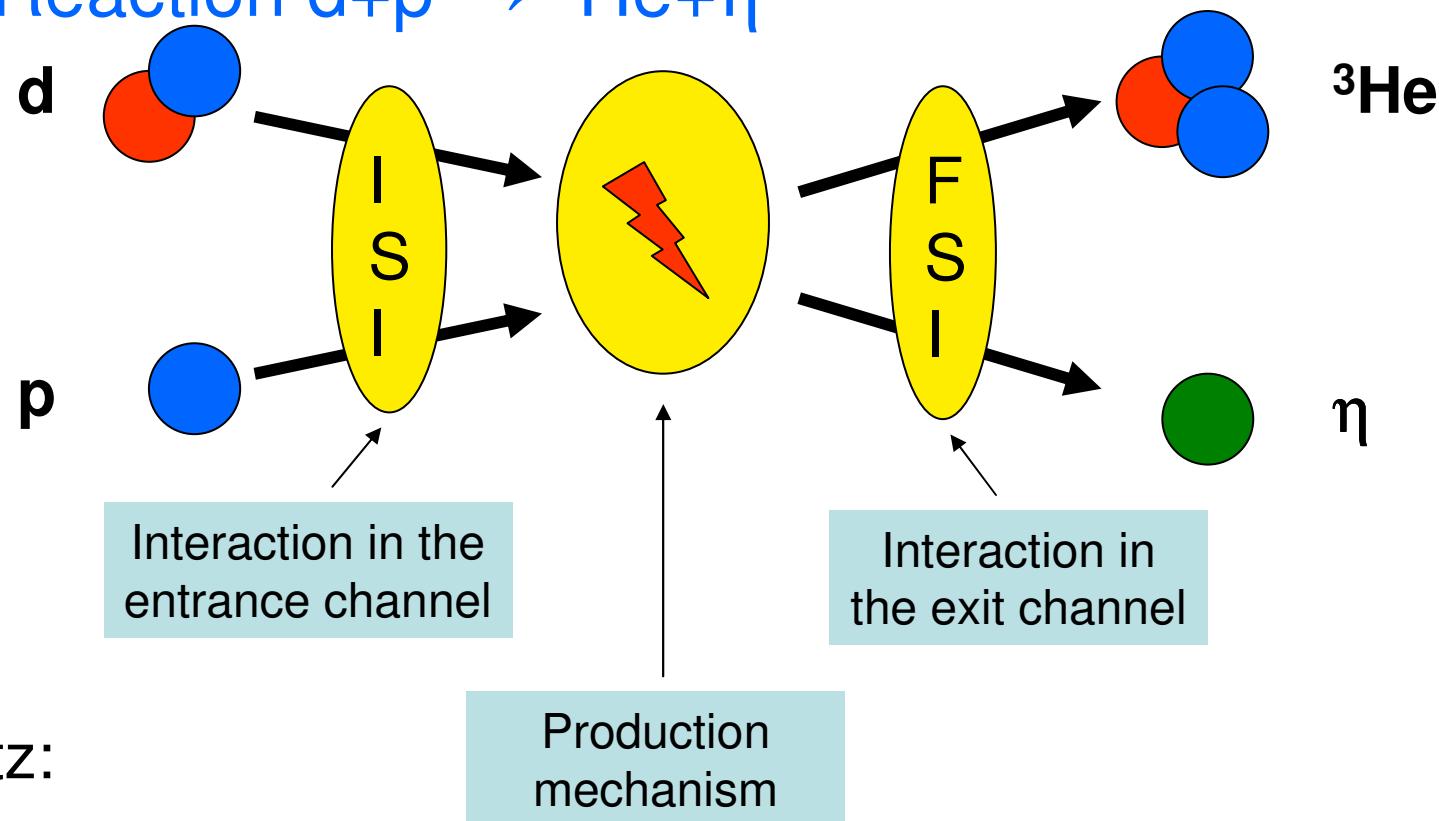
## The Reaction $d+p \rightarrow {}^3\text{He}+\eta$

- Extreme increase of the total cross section close to the production threshold
- Increase of the cross sections within  $\Delta Q < 1 \text{ MeV}$ 
  - strong energy dependence at threshold
- After that total cross sections remain almost constant
  - Additional effect beside pure phase space

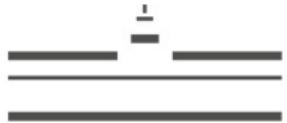
Explanation: Strong final state interaction (FSI) between  ${}^3\text{He}$  nucleus and  $\eta$ -meson



## The Reaction $d+p \rightarrow {}^3\text{He}+\eta$



$$\left( \frac{d\sigma(\vartheta)}{d\Omega} \right) = \frac{p_f}{p_i} \cdot |f_{\text{scatt}}|^2 = \frac{p_f}{p_i} \cdot |ISI \cdot f_{\text{prod}} \cdot FSI|^2 = \frac{p_f}{p_i} \cdot |ISI|^2 \cdot |f_{\text{prod}}|^2 \cdot |FSI|^2$$



# Scattering Theory and Final State Interaction

Description of the cross section including FSI:

$$\frac{d\sigma(\vartheta)}{d\Omega} = \frac{p_f}{p_i} |f_s|^2 = \frac{p_f}{p_i} \cdot \frac{|f_{\text{prod}}|^2}{\left|1 - i \cdot a \cdot p_f + \frac{1}{2} a \cdot r_0 \cdot p_f^2\right|^2}$$

Assumption:

- Energy dependence of the production amplitude  $f_{\text{Prod}}$  is negligible close to threshold:  $f_{\text{Prod}} \sim \text{const.}$
- Initial State Interaction (ISI) also:  $\text{ISI} = \text{const.}$



# Scattering Theory and Final State Interaction

- The scattering length can deliver informationen about possible bound states
- Conditions for bound  $\eta^3\text{He}$  state:
  - Existence of a pole in the complex  $p_f$  plane

$$f_s = \frac{f_{\text{prod}}}{1 - i \cdot a \cdot p_f + \frac{1}{2} a \cdot r \cdot p_f^2}$$

$$a \equiv a_r + ia_i$$

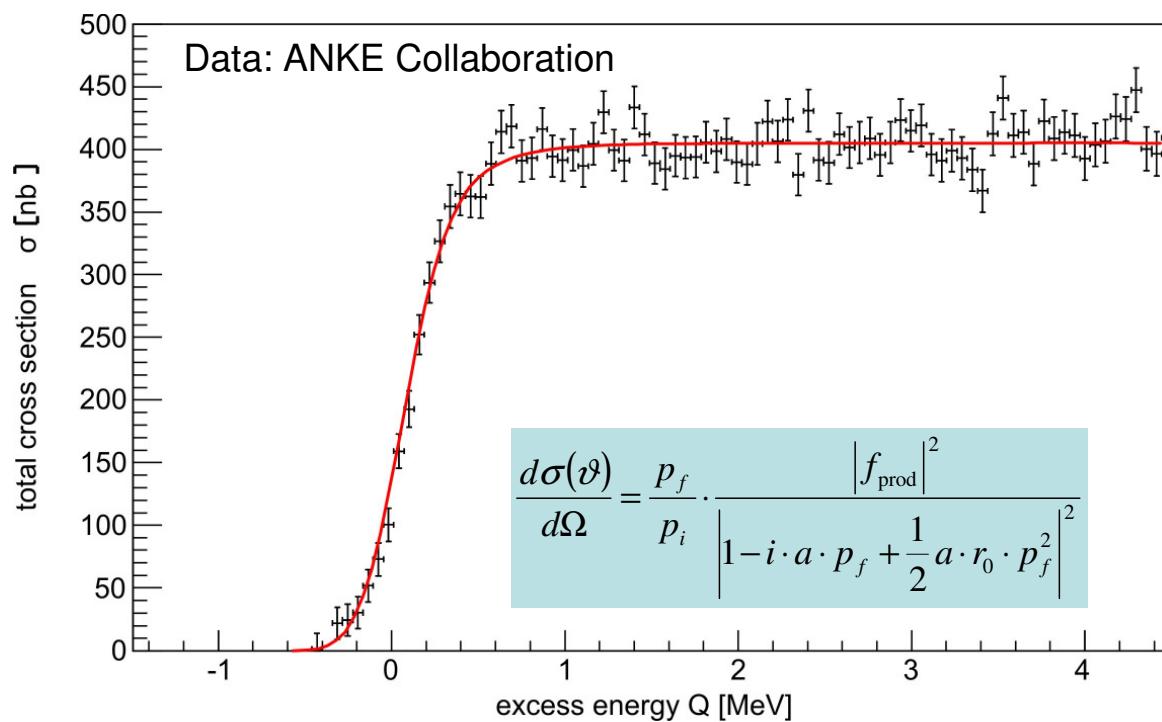
$$r \equiv r_r + ir_i$$

- As well as

$$a_r < 0, \quad a_i > 0, \quad R = \frac{|a_i|}{|a_r|} < 1$$

# The Reaction $d+p \rightarrow {}^3\text{He}+\eta$

Fit to data very close to threshold: Only s-wave



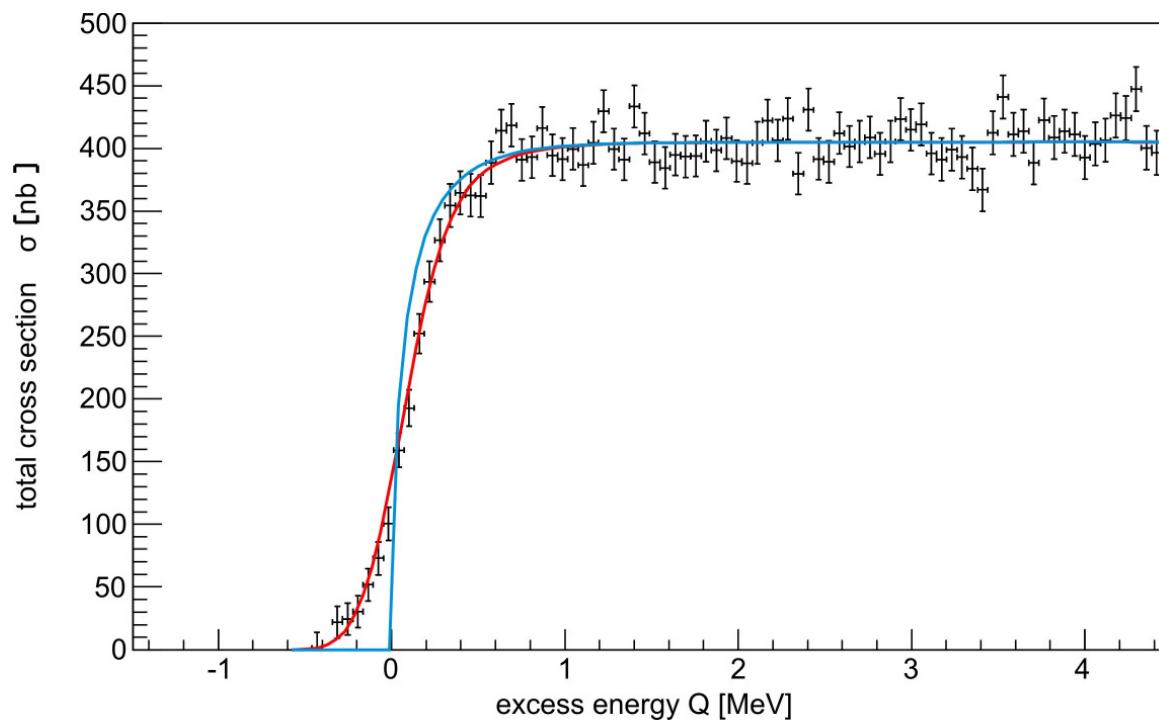
Fit parameter:

- Complex scattering length  $a=a_r+ia_i$
- Complex effective range  $r=r_r+ir_i$
- Finite momentum width  $\delta p_{\text{beam}}$  of the accelerator beam



## The Reaction $d+p \rightarrow {}^3\text{He}+\eta$

Excitation function without accelerator beam smearing  $\delta p_{\text{beam}}$ :

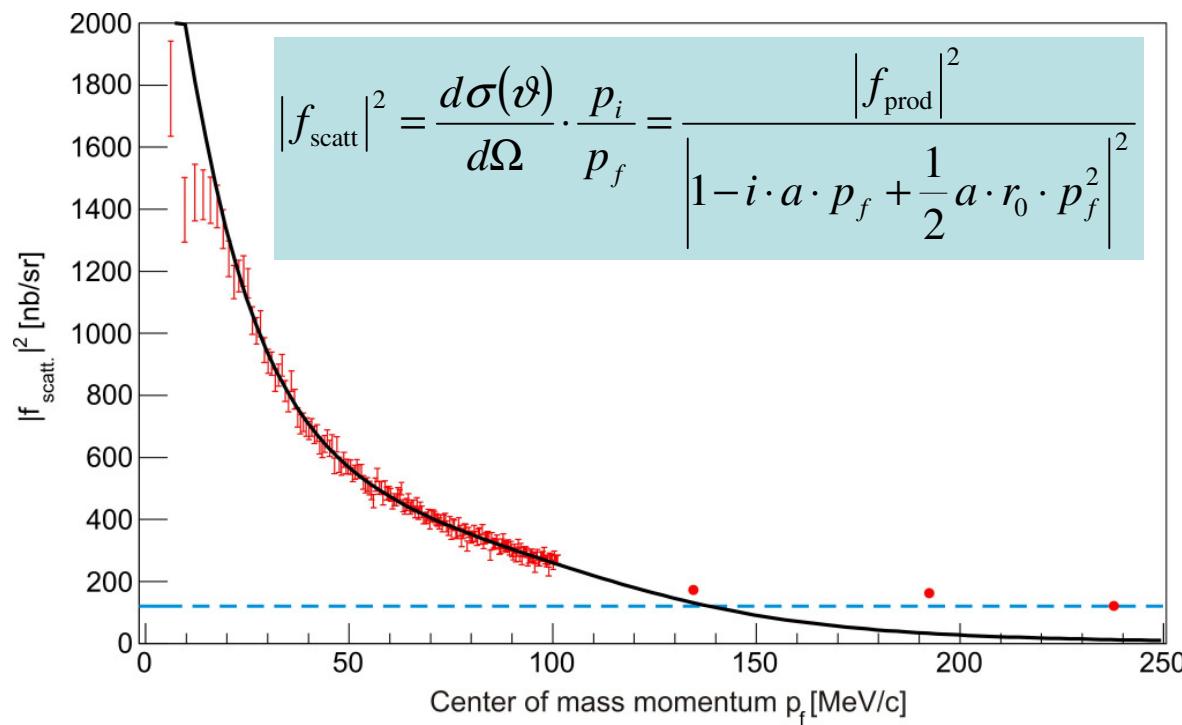


Blue line:

- Defolded shape, extracted from data (no accelerator beam smearing)
- 
- Total cross section reaches maximum already  $\Delta Q < 0.5$  MeV above threshold

# The $d+p \rightarrow {}^3\text{He}+\eta$ Scattering Amplitude

Extracted scattering amplitude ( $Q > 0$  MeV)



- Scattering amplitude decreases rapidly with increasing final state momentum  $p_f$
- Scattering amplitude almost constant at high energies

→ strong FSI in  $\eta {}^3\text{He}$  system



## $\eta$ - ${}^3\text{He}$ Scattering Length

Fit to data delivers information about the complex  $\eta$ - ${}^3\text{He}$  scattering length:

$$\left( \frac{d\sigma(\vartheta)}{d\Omega} \right) \cdot \frac{p_i}{p_f} = |f_{\text{scat}}|^2 = |f_{\text{prod}} \cdot FSI|^2 = |f_{\text{prod}}|^2 \cdot |FSI|^2$$



Result:

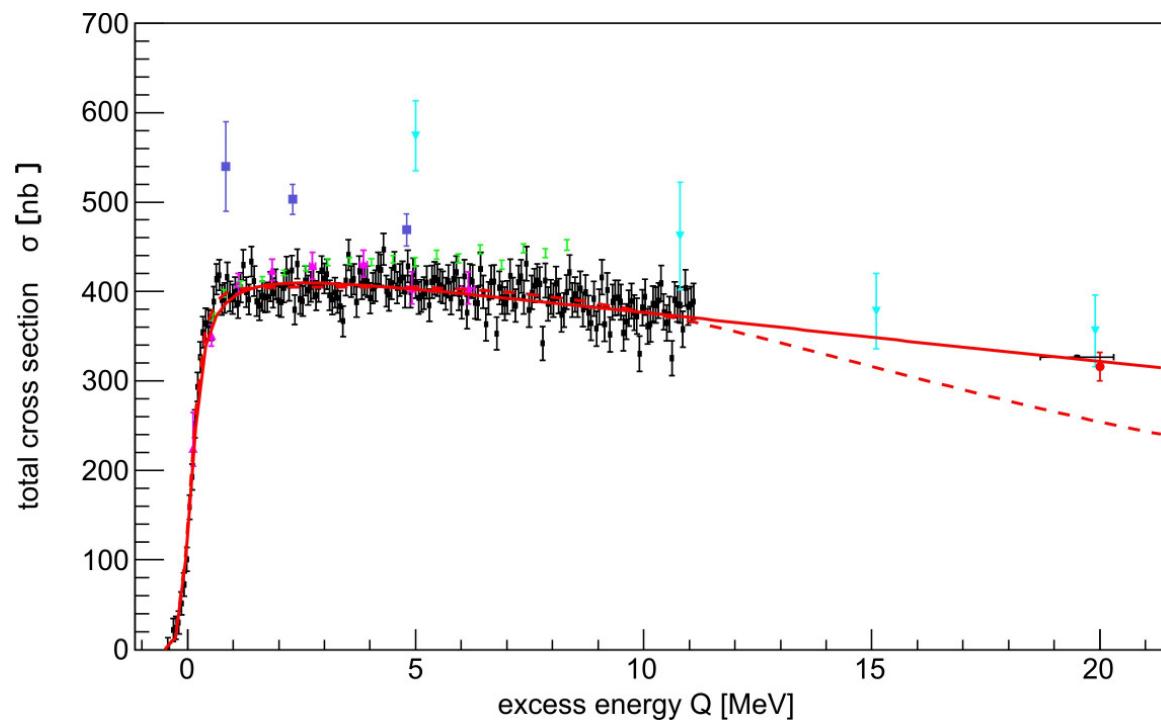
$$a = [\pm (10.7 \pm 0.8^{+0.1}_{-0.5}) + i(1.5 \pm 2.6^{+1.0}_{-0.9})] \text{ fm}$$

$$FSI = \frac{1}{1 - i \cdot a \cdot p_f + \frac{1}{2} a \cdot r_0 \cdot p_f^2}$$

Notice: Determination of  $|a_r|$ !

# The Reaction $d+p \rightarrow {}^3\text{He}+\eta$

Fit to the near-threshold ANKE data:



Fit to 0-11 MeV: dashed

Fit to 0-20 MeV: solid

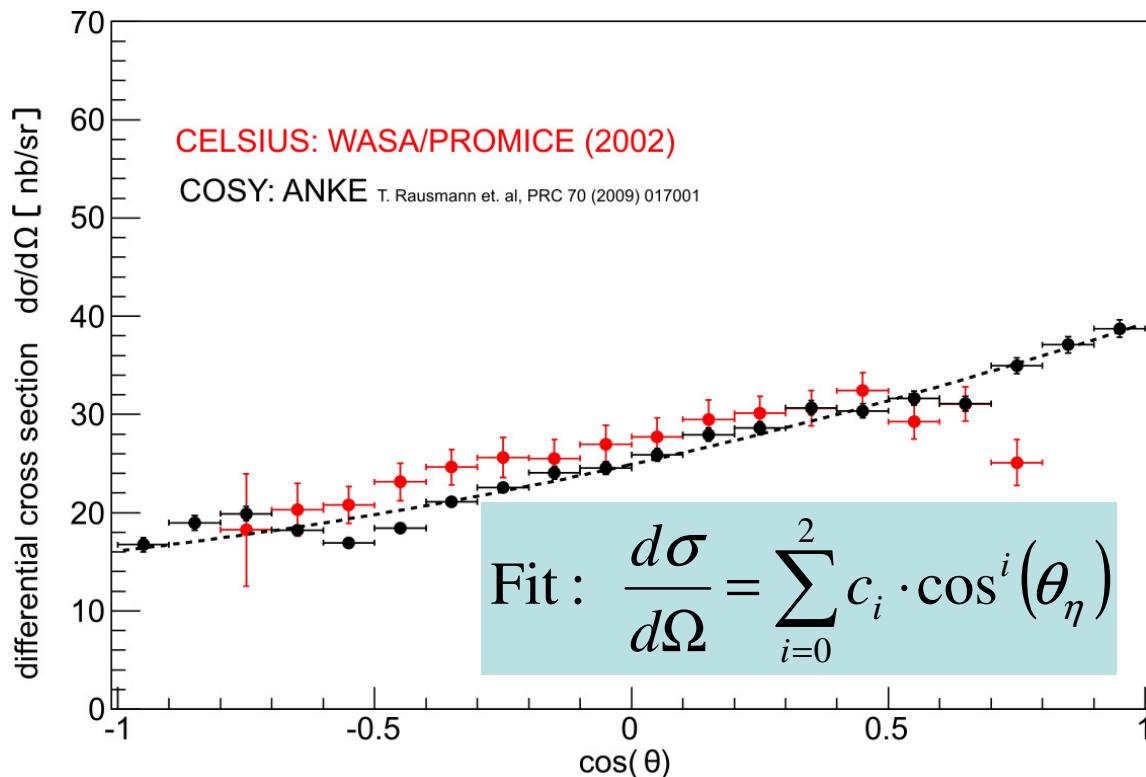


- Shape of the fit curve depends slightly on the fit range

- Reason:  
E.g. contributions from higher partial waves

## Differential Cross Sections

Angular distributions of  $\eta$ -mesons at  $Q = 20$  MeV:



Data up to  $Q \sim 2$  MeV:

- s-wave:  
 $(d\sigma/d\Omega)(\theta) = \text{const.}$

Above  $Q \sim 2$  MeV:

- s+p-waves:  
linear + quadratic term  
in  $\cos(\theta)$   
(interference possible)

## $\eta$ - $^3\text{He}$ -Interaction: Determination of $\text{Pols}$

$$\left( \frac{d\sigma(\vartheta)}{d\Omega} \right) \cdot \frac{p_i}{p_f} = |f_{\text{scatt}}|^2 = |f_{\text{prod}} \cdot FSI|^2 = |f_{\text{prod}}|^2 \cdot |FSI|^2$$

$$FSI = \frac{1}{1 - i \cdot a \cdot p_f + \frac{1}{2} a \cdot r_0 \cdot p_f^2}$$

$$FSI = \frac{1}{\left(1 - \frac{p_f}{p_1}\right) \cdot \left(1 - \frac{p_f}{p_2}\right)}$$

$$a = -i \cdot \frac{p_1 + p_2}{p_1 \cdot p_2} \quad r_0 = + \frac{2 \cdot i}{p_1 + p_2}$$

$$p_1 = \left[ (-5 \pm 7^{+2}_{-1}) \pm i \cdot (19 \pm 2 \pm 1) \right] \text{MeV/c}$$

$$p_2 = \left[ (106 \pm 5) \pm i \cdot (76 \pm 13^{+1}_{-2}) \right] \text{MeV/c}$$

## $\eta$ - $^3\text{He}$ -Interaction: Determination of $\text{Pols}$

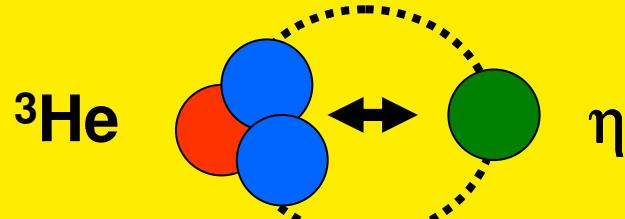
- Pole close to the reaction threshold

$$|Q_0| = \left| \frac{p_1^2}{2 \cdot m_{red}} \right| = 0.37 \text{ MeV}$$

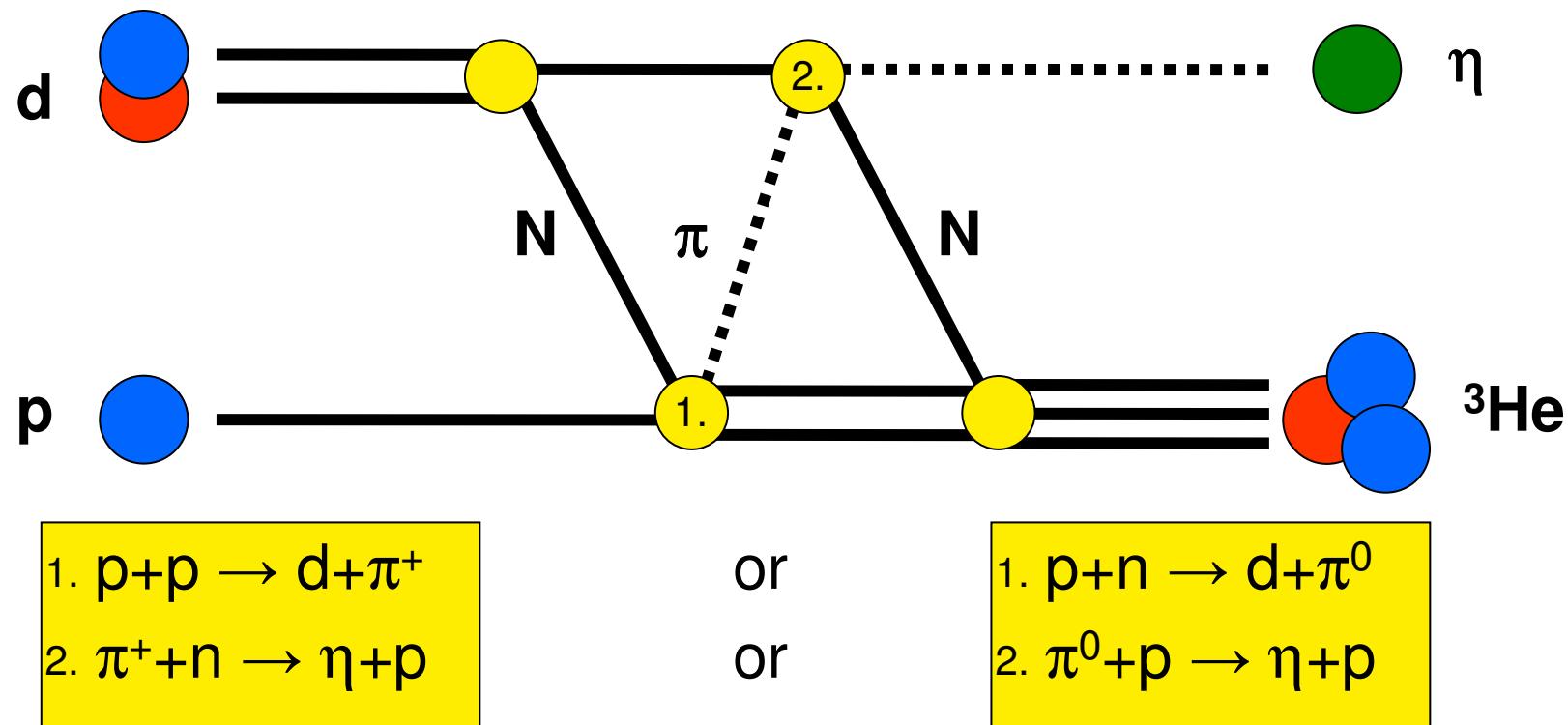
- Position of the near-threshold pole (and scattering length) stable, i.e. nearly independent of fit range
- Large real part of scattering length and  $|a_r| > a_i$

→ indication for the existence of a bound state

(strong interaction!)



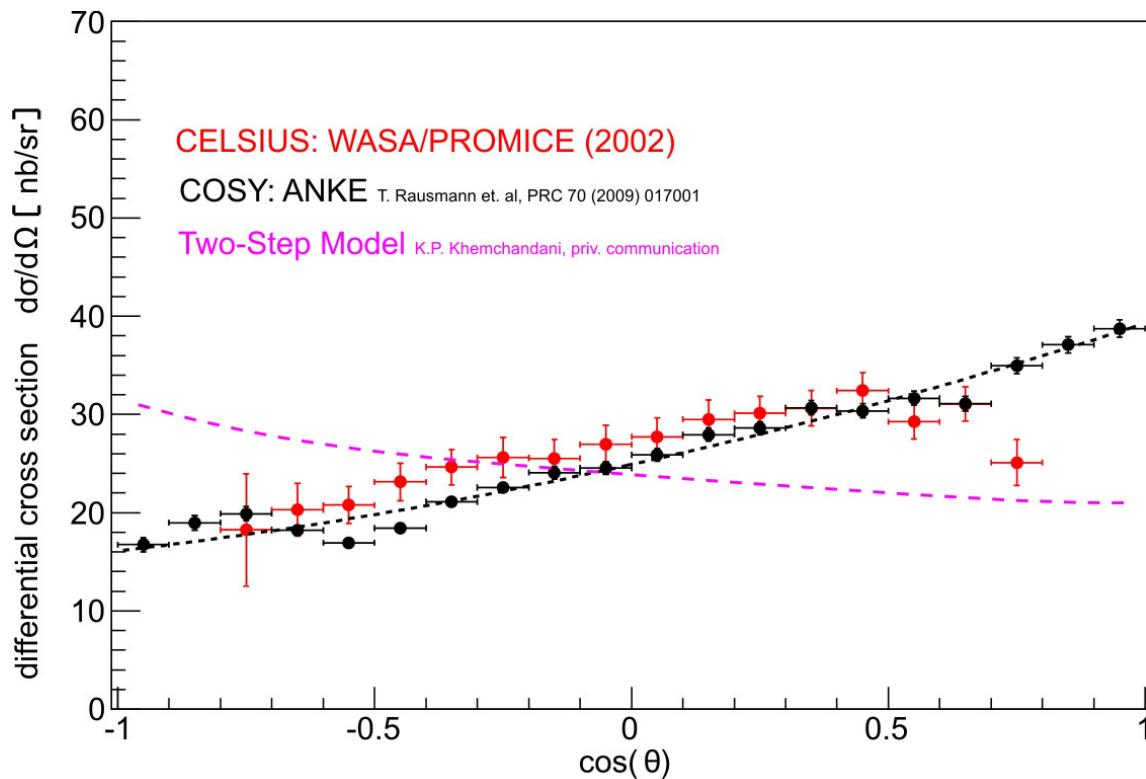
## Production Mechanism: Two-Step-Model



Use known cross sections for complete process

## Prediction of the Two-Step-Model

Angular distributions of  $\eta$ -mesons at  $Q = 20$  MeV:



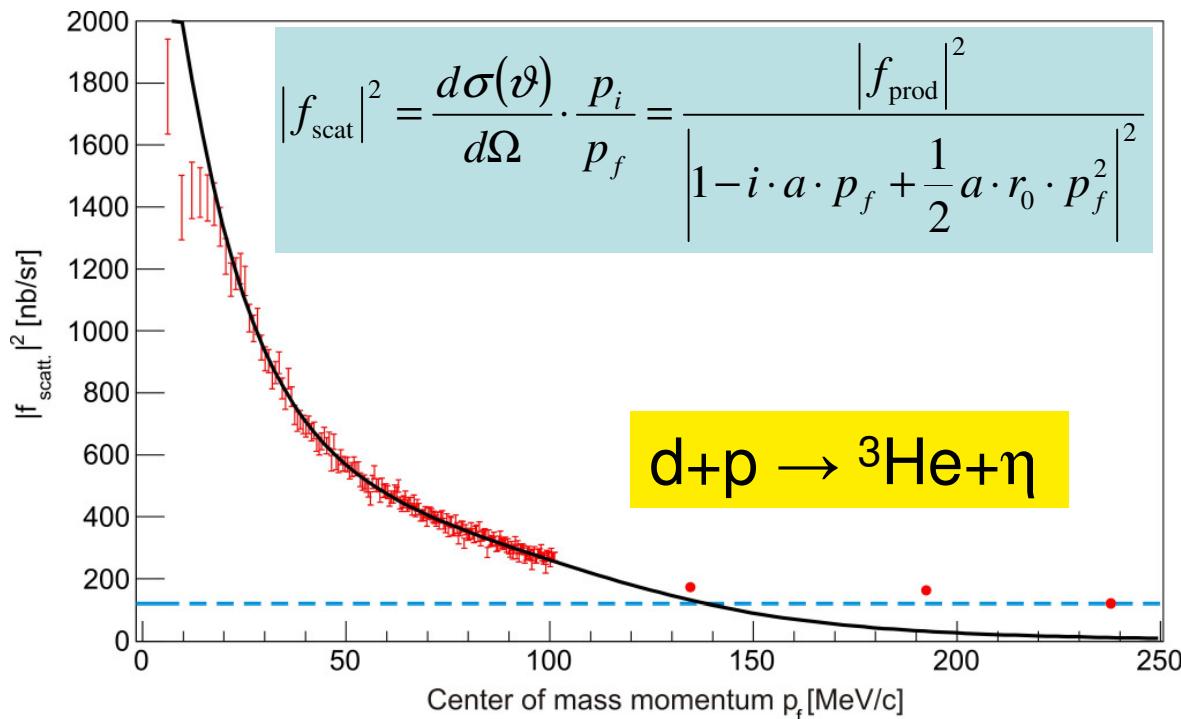
- Two-step-model predicts a different emission of the ejectiles
- Obviously the two-step-model is not sufficient to explain the data



**open questions  
to theory**

## Further Evidences for a Strong FSI

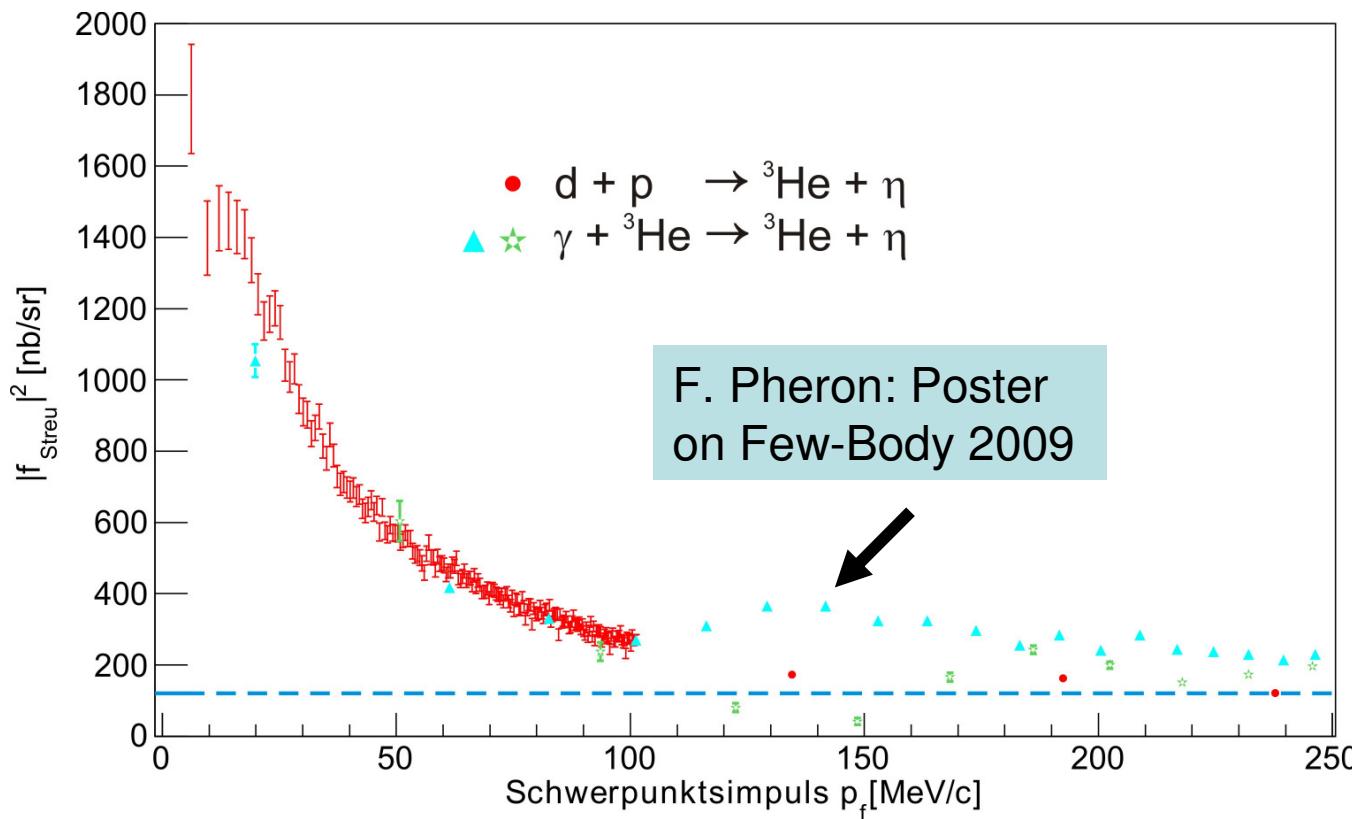
Idea: Compare production amplitudes of different reactions with same final state



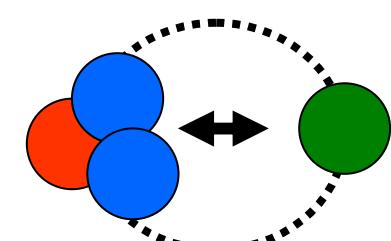
Remember:

- $|f_{\text{prod}}| = \text{const.}$   
for relevant energy range
- energy dependence of ISI neglected
- $|f_{\text{scat}}|$ :  
energy dependence according to FSI

## Compare: dp- and $\gamma^3\text{He}$ -Scattering



- Scattering amplitudes show similar energy dependence
- Strong hint for a strong FSI between He-nuclei and  $\eta$ -mesons



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## So we have...

- Observation of an extremely large scattering length  $a_{\text{He}\eta}$

$$a = \left[ \pm (10.7 \pm 0.8^{+0.1}_{-0.5}) + i(1.5 \pm 2.6^{+1.0}_{-0.9}) \right] \text{fm}$$

- Scattering amplitude has a pole very close to threshold

$$|Q_0| = \left| \frac{p_1^2}{2 \cdot m_{red}} \right| = 0.37 \text{ MeV}$$

- Similar behaviour in case of photoproduction

The  $\eta - {}^3\text{He}$  final state is a good candidate for a bound meson-nucleus system

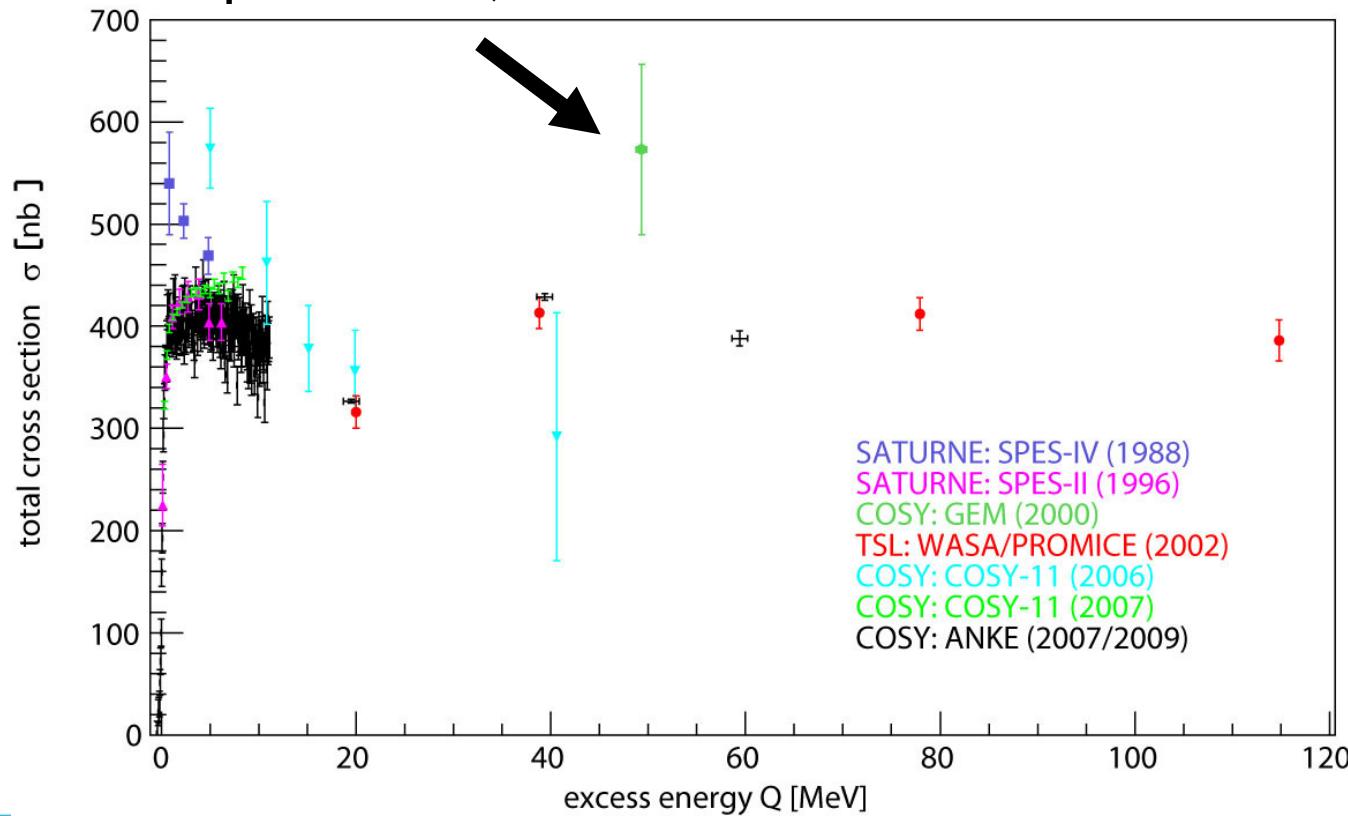


## Next Steps...

- Measurement of  $d+p \rightarrow {}^3\text{He}+\eta$  with polarized beam and/or target
  - Informationen about contributing partial waves
  - Determination of the sign of the scattering length  $a_{\text{He}\eta}$
- Measurement of  $d+n \rightarrow {}^3\text{H}+\eta$  (by  $d+d \rightarrow {}^3\text{H}+\eta + p_{\text{spec}}$ )
  - Informationen about isospin/charge invariance of the FSI
  - Determination of the scattering amplitude
- Measurement of  $d+p \rightarrow {}^3\text{He}+\eta$  at fixed excess energies
  - Is the „GEM-Peak“ real?
  - How do the total and differential cross sections develop?

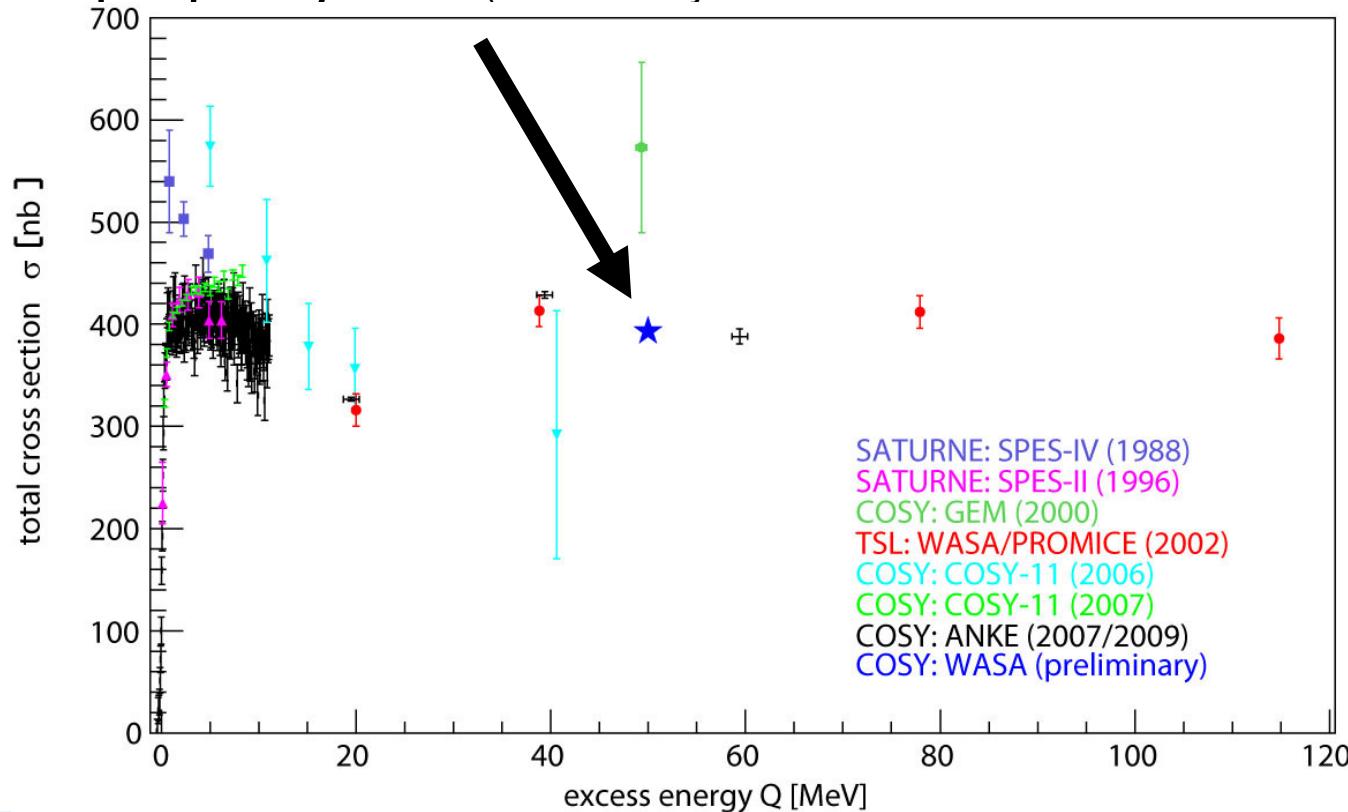
# Investigations at Higher Excess Energies

- Is there a peak at  $Q = 50$  MeV?



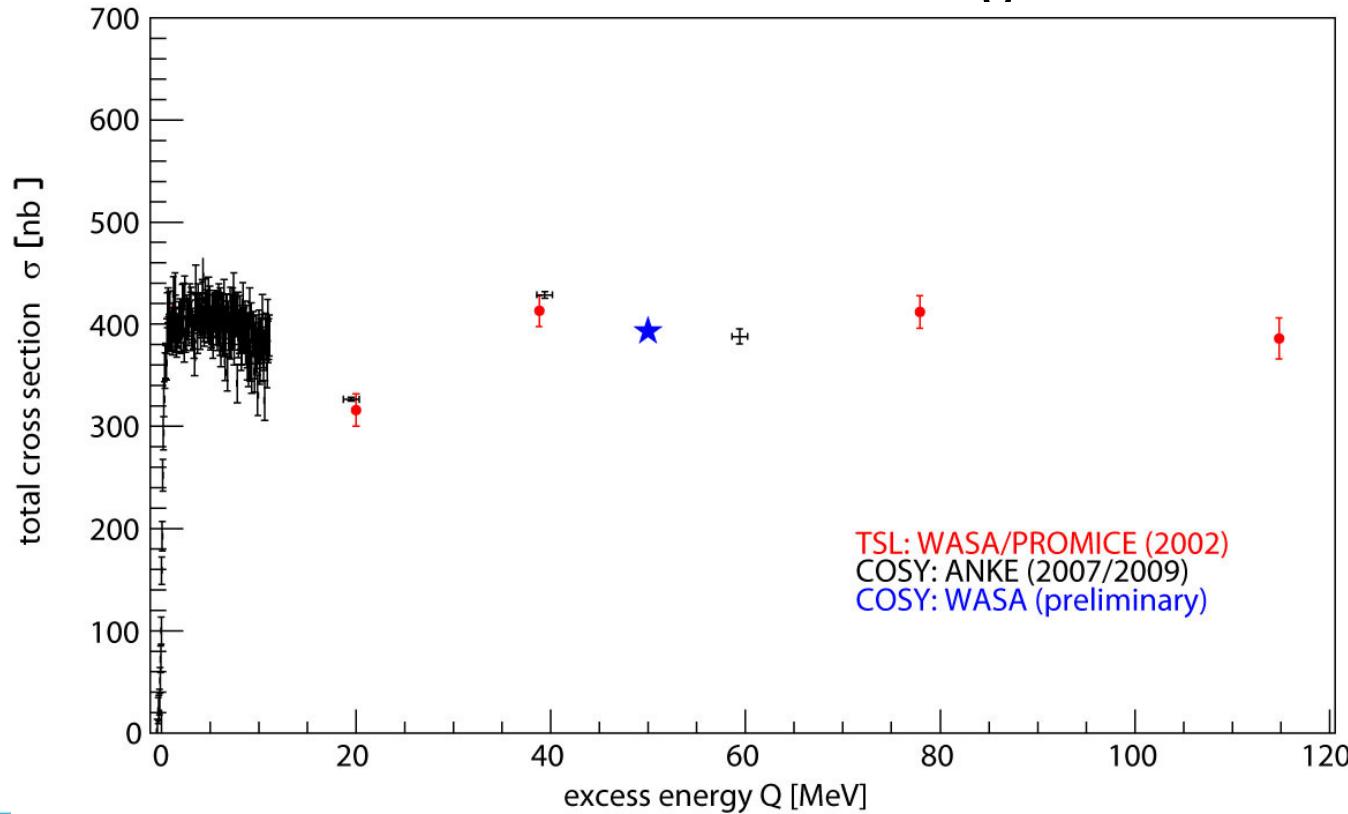
# Investigations at Higher Excess Energies

- Most probably not! (Preliminary WASA-at-COSY data at  $Q = 50$  MeV)



# The ANKE and WASA Data Sets

- Consistent data set for further investigations



## Summary

- The  $\eta$ - ${}^3\text{He}$  system exposes an unexpected strong final state interaction
- The  $\eta$ - ${}^3\text{He}$  system is a good candidate for a bound meson-nucleus state (strong interaction)
- There is need for further theoretical studies
  - on the extraction of FSI parameters from data
  - on the description of the production process: Two-Step Model etc.
- New data coming soon might support further theoretical investigation

Thank you very much....

