Measurements of the CP-violating phase ϕ_s at LHCb



Konrad Klimaszewski

UJ, Kraków NCBJ, Warszawa

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Introduction

LHCb experiment

 B_s^0 measurements

 $B_s^0
ightarrow J/\psi \phi$

 $B_s^0 \to J/\psi \pi^+\pi^-$



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Currently the main focus of particle physics is on searches for physics beyond the Standard Model

There are two ways to discover New Physics:

- Direct searches for production of new particles (Atlas and CMS)
- Indirect searches (LHCb contributes)
 - $\circ~$ Tests of the SM by precision measurements of well known processes
 - Observation of a disagreement is an indirect indication for the existence of new objects
 - $\circ~$ In particular we are interested in CPV in B and D
 - CPV in SM is too small to explain matter domination over antimatter
 - It is a good tool in searches for New Physics

CP violation



- Particles and anti-particles behave differently
- Within the Standard Model (SM) only weak interactions violate CP
- Flavour changing weak interactions characterised by CKM matrix

$$\begin{pmatrix} d'\\s'\\b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub}\\V_{cd} & V_{cs} & V_{cb}\\V_{td} & V_{ts} & V_{tb} \end{pmatrix} \cdot \begin{pmatrix} d\\s\\b \end{pmatrix}$$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} \xrightarrow{V_{vb} V_{vb}^* \sim \mathcal{O}(\lambda^2)} \underbrace{\beta_s}_{V_{cs} V_{cb}^* \sim \mathcal{O}(\lambda^2)} \underbrace{\beta_s}_$$

 $B_{\rm s}^0 - \overline{B}_{\rm s}^0$ mixing

Time development of the mixing described by phenomenological Schroedinger equation:

$$i\frac{d}{dt} \begin{pmatrix} B_s \\ \overline{B}_s \end{pmatrix} = (M - \frac{i}{2}\Gamma) \begin{pmatrix} B_s \\ \overline{B}_s \end{pmatrix}$$
$$M = \begin{pmatrix} M_{11} & M_{12} \\ M_{12}^* & M_{22} \end{pmatrix}; \Gamma = \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma_{22} \end{pmatrix}$$

Diagonalizing it in terms of mass eigenstates:

$$i\frac{d}{dt}(B_L) = \left(m_L - \frac{i}{2}\Gamma_L\right)(B_L)$$
$$i\frac{d}{dt}(B_H) = \left(m_H - \frac{i}{2}\Gamma_H\right)(B_H)$$

Mass eigenstates \neq flavour eigenstates:

$$egin{aligned} |B_L
angle &= p \; |B_s^0
angle + q \; |\overline{B}_s^0
angle \ |B_H
angle &= p \; |B_s^0
angle - q \; |\overline{B}_s^0
angle \end{aligned}$$





Phenomenological mixing parameters:

- Lifetime difference: $\Delta \Gamma_s = \Gamma_L \Gamma_H$
- Mass difference: $\Delta m_s = m_H m_L$
- Mixing phase: $\phi_M = \arg(-M_{12}/\Gamma_{12})$

Three ways of CPV

- In mixing (indirect) $\Gamma(B^0 \to \overline{B}^0) \neq \Gamma(\overline{B}^0 \to B^0)$
- In decays (direct) $\Gamma(B^0 \to f) \neq \Gamma(\overline{B}^0 \to \overline{f})$
- In interference (indirect) between direct decays and decays with mixing $\Gamma(B^0 \to f_{CP}) \neq \Gamma(\overline{B}^0 \to f_{CP})$
 - $\,\circ\,$ Allows us to measure the value of ϕ_s

Phases

$$\phi_{S} = -2arg(-\frac{V_{ts}V_{tb}^{*}}{V_{cs}V_{cb}^{*}}) = -2\beta_{s}$$

$$\phi_{M} = 2arg(V_{ts}V_{tb}^{*})$$

$$2\phi_{D} = arg(V_{cs}V_{cb}^{*})$$



Three ways of CPV

- In mixing (indirect) $\Gamma(B^0 \to \overline{B}^0) \neq \Gamma(\overline{B}^0 \to B^0)$
- In decays (direct) $\Gamma(B^0 o f)
 eq \Gamma(\overline{B}^0 o \overline{f})$
- In interference (indirect) between direct decays and decays with mixing $\Gamma(B^0 \to f_{CP}) \neq \Gamma(\overline{B}^0 \to f_{CP})$
 - $^\circ\,$ Allows us to measure the value of ϕ_s

Why ϕ_s ?

- Very well predicted in the SM: $\phi_s^{SM} = -0.0368 \pm 0.0017 \, \mathrm{rad}$
- New particles can be exchanged in the box diagram and modify the value of $\phi_{\rm M}$



Analysis ingredients



Theoretical CP Asymmetry (for CP eigenstates):

$$A_{CP}(t) = \frac{\Gamma(\overline{B}_{s}^{0}(t) \to f_{CP}) - \Gamma(\overline{B}_{s}^{0}(t) \to f_{CP})}{\Gamma(\overline{B}_{s}^{0}(t) \to f_{CP}) + \Gamma(\overline{B}_{s}^{0}(t) \to f_{CP})} = -\eta_{CP} \cdot \sin(\varphi_{s}) \cdot \sin(\Delta m_{s} t)$$

Experimental CP Asymmetry from a flavour tagged time-dependent analysis:

$$A_{CP}(t) = - \eta_{CP} \cdot D_{tag}(\omega_{mistag}) \cdot D_{t_{res}}(\sigma_t) \cdot \sin(\phi_s) \cdot \sin(\Delta m_s t)$$

Essential ingredients to measure ϕ_s :

- CP eigenvalue of the final state: angular analysis needed, if not unique CP eigenstate
- · Probability of getting the initial flavour: good tagging performance and precise knowledge
- · Decay time resolution: good performance and precise knowledge
- Mixing frequency Δm_s : time dependent analysis 8 / 35



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• LHCb is a single-arm forward (2 $< \eta <$ 5) spectrometer at the LHC

- Precision beauty and charm physics: CP violation, rare decays, heavy flavour production
- High rate of $b\overline{b}$ pairs production at the LHC

 $~\circ~~\sigma_{b\overline{b}}\sim 300 \mu b \rightarrow$ more than $10^{13}~b\overline{b}$ pairs produced so far



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ightarrow {J/\psi} \pi^+ \pi^-$

- s quark in B⁰_s is produced with s
- $\sim 50 \%$ of \overline{s} forms a charged K
- charge of the K identifies flavour of B⁰_s

Opposite side

- in pp collisions b produced mostly in bb pairs
- flavour determined by the charge of decay products of opposite B:
 - leptons
 - kaons
 - global charge of secondary vertex



LH

- Total effective tagging efficiency: $\epsilon(1-2\omega)^2$
- ϵ efficiency of tagging algorithm
- ω frequency of events with wrong tagging
- $Eff = (3.9 \pm 0.25)\%$

 $B_s^0 - \overline{B}_s^0$ oscillations



 Δm_s measured from 1fb $^{-1}$ $B^0_s o D^-_s \pi^+$ decays



- High statistics: N ~ 34000 signal candidates
- Self tagging channel
- Five different D_s^- decay modes: $(\phi \pi^-, K^* K^-, K^- K^+ \pi^-, K^- \pi^+ \pi^-, \pi^- \pi^+ \pi^-)$
- Very low background



 $\overline{B_s^0 - \overline{B}_s^0}$ oscillations



The measured oscillation frequency: $\Delta m_s = 17.768 \pm 0.023(stat) \pm 0.006(syst)\,\mathrm{ps}^{-1}$



[New J. Phys. 15 (2013) 053021]

Decay time resolution

- *інср*
- B_s^0 have fast oscillations: period $2\pi/\Delta m_s pprox$ 350 fs
- Decay time resolution σ_t will dilute the measured oscillation amplitude

• The dilution factor:
$$D(\sigma_t) = e^{-rac{(\sigma_t \Delta m_s)^2}{2}}$$



- Resolution measured from data
- Combinations of $\mu^+\mu^-K^+K^-$ events
- Same selection as for B⁰_s apart for decay time cuts
- Mostly prompt events with true decay time of zero
- Effective decay time resolution $\sigma_t = 45 \text{ fs}$

$$D(\sigma_t = 45 \, \mathrm{fs}) pprox 0.73$$

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 $B^0_s \rightarrow J/\psi(\mu\mu)K^+K^-$

[arXiv:1304.2600] LHCD

 $B_c^0 \rightarrow J/\psi(\mu\mu)K^+K^-$

- Mostly via $B_s^0 \rightarrow J/\psi \phi$, with $\phi \rightarrow K^+ K^-$ (the P-wave)
- Small non-resonant component with K^+K^- in S-wave

Sample

- Analysed $1 \, \text{fb}^{-1}$ LHCb data
- High statistics: $N \sim 27600$ events
- Low background
 - Narrow J/ψ resonance
 - Cuts on B_s^0 decay time

Decay dominated by tree level diagram:



[Phys. Rev. D 87, 112010]



Angular analysis

[arXiv:1304.2600]



$$B_{s}^{0} \rightarrow J/\psi(\rightarrow \mu^{+}\mu^{-})\phi(\rightarrow K^{+}K^{-})$$

Pseudoscalar to vector mesons $(J^{PC} = 1^{--})$ decay: final states *CP* odd and *CP* even.

L = 0, 2 CP =
$$(-1)^{L}$$
 = +1
L = 1 CP = $(-1)^{L}$ = -1

Three polarisation amplitudes and phases:

- $|A_0|^2$, $|A_{\parallel}|^2$, δ_0 , δ_{\parallel} (*CP*-even)
- $|A_{\perp}|^2$, δ_{\perp} (*CP*-odd)



Angular analysis in **helicity basis**: $\theta_{\kappa}, \theta_{\mu}, \phi_{h}$ to separate *CP*=±1 states and extract ϕ_{s} .

 s-wave component amplitude and phase included in the fit: | A_s |², δ_s (CP-odd)

 $\frac{\text{Angular analysis}}{\frac{d^4\Gamma(B^0_s \to J/\psi K^+ K^-)}{dtd\Omega} \propto \sum_{k=1}^{10} h_k(t) f_k(\Omega)}$

Time-dependent part

$$h_k(t) = N_k e^{-\Gamma_s t} \left[a_k \cosh(\frac{1}{2}\Delta\Gamma_s t) + b_k \sinh(\frac{1}{2}\Delta\Gamma_s t) + c_k \cos(\Delta m_s t) + d_k \sin(\Delta m_s t) \right]$$

- N_k amplitudes of the different polarisations and their interference
- a_k, b_k, c_k, d_k coefficients expressed in terms of CP violating observables C, D, S (depending on φ_s)

Angular part

- $\Omega = (\theta_{\mu}, \, \theta_{K}, \, \varphi_{h})$
- Various CP states differ by angular dependence

Angular analysis

[arXiv:1304.2600]





Result extracted using unbinned maximum likelihood fit

CP-even, CP-odd, S-wave, Total Fit



LHCb 2011 data corresponding to $\mathcal{L}=1 \text{fb}^{-1}$

$$\begin{split} \phi_s &= 0.07 \pm 0.09(stat) \pm 0.01(syst) \, \text{rad} \\ \Gamma_s &= 0.663 \pm 0.005(stat) \pm 0.006(syst) \, \text{ps}^{-1} \\ \Delta\Gamma_s &= 0.100 \pm 0.016(stat) \pm 0.003(syst) \, \text{ps}^{-1} \end{split}$$

Main systematic contributions: angular and decay time acceptances

 $B^0_s
ightarrow {\sf J}/\psi(ee) {\sf K}^+ {\sf K}^-$

- My area of interest
- Same BR for $J/\psi \rightarrow ee$ as for $\mu\mu$
- Electrons are harder to trigger on and to identify
- Smaller sample expected





LH

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 $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$

[arXiv:1405.4140]



- Predominantly via $B_s^0 \to J/\psi X$, with $X = f_0(980), f_2(1270), f_0(1370)$
- Decay mode determined to be > 97.7% CP-Odd [Phys. Rev. D 86, 052006]
- No need for angular analysis

Sample

- Analysed 3fb⁻¹of data from LHCb
- Signal events: $N\sim 27100$
- Γ_s and $\Delta\Gamma_s$ constrained to the values from $B^0_s
 ightarrow J/\psi\phi$





Summary

Results of LHCb ϕ_s measurements:

- $B^0_s \to J/\psi K^+ K^ (\mathcal{L} = 1 \mathrm{fb}^{-1})$ and $B^0_s \to J/\psi \pi^+ \pi^ (\mathcal{L} = 3 \mathrm{fb}^{-1})$
- Most precise measurement to date
 $\phi_s = 0.070 \pm 0.068 \pm 0.008 \, \text{rad}$

 So far compatible with SM
 $\Gamma_s = 0.663 \pm 0.005 \pm 0.006 \, \text{ps}^{-1}$
 $\Delta \Gamma_s = 0.100 \pm 0.016 \pm 0.003 \, \text{ps}^{-1}$

LHC

LHCb plans for the future:

- An update for $B_s^0 \rightarrow J/\psi K^+ K^-$ channel with a factor 2 more statistics in progress (expected $\delta \phi_s \approx 0.05 \text{ rad}$)
- Work is underway for inclusion of additional channels
- More data after LHCb upgrade (expected $\delta \phi_s \approx 0.008 \text{ rad}$)



Backup

$$B_s^0 - \overline{B}_s^0$$
 mixing



$$\begin{split} \Delta M &= M_{\rm H} - M_{\rm L} = 2|M_{12}| \left(1 - \frac{1}{8} \frac{|\Gamma_{12}|^2}{|M_{12}|^2} \sin^2 \phi_{12} + \dots \right), \\ \Delta \Gamma &= \Gamma_{\rm L} - \Gamma_{\rm H} = 2|\Gamma_{12}| \cos \phi_{12} \left(1 + \frac{1}{8} \frac{|\Gamma_{12}|^2}{|M_{12}|^2} \sin^2 \phi_{12} + \dots \right), \\ a_{\rm sl} &= \frac{\Gamma \left(\overline{B}(t) \to f \right) - \Gamma \left(B(t) \to \overline{f} \right)}{\Gamma \left(\overline{B}(t) \to f \right) + \Gamma \left(B(t) \to \overline{f} \right)} = \frac{\Delta \Gamma}{\Delta M} \tan \phi_{12}, \end{split}$$

Angular analysis



$$\begin{array}{rcl} \lambda_i &=& \frac{q}{p} \frac{A_i}{A_i} \\ \phi_s &=& -\arg(\lambda) \\ C &=& \frac{1-|\lambda|^2}{1+|\lambda|^2} \\ S &=& -\frac{2|\lambda|\sin\phi_s}{1+|\lambda|^2} \\ D &=& -\frac{2|\lambda|\cos\phi_s}{1+|\lambda|^2} \end{array}$$

TABLE II. Definition of angular and time-dependent functions.

k	$f_k(\theta_{\mu}, \theta_K, \varphi_h)$	N_k	a_k	b_k	c_k	d_k
1	$2\cos^2\theta_K \sin^2\theta_\mu$	$ A_0 ^2$	1	D	С	-S
2	$\sin^2\theta_K(1-\sin^2\theta_\mu\cos^2\varphi_h)$	$ A_{ } ^2$	1	D	С	-S
3	$\sin^2\theta_K(1-\sin^2\theta_\mu\sin^2\varphi_h)$	$ A_{\perp} ^{2}$	1	-D	С	S
4	$\sin^2\theta_K \sin^2\theta_\mu \sin 2\varphi_h$	$ A_{\parallel}A_{\perp} $	$C\sin(\delta_{\perp} - \delta_{\parallel})$	$S\cos(\delta_{\perp} - \delta_{\parallel})$	$\sin \left(\delta_{\perp} - \delta_{\parallel} \right)$	$D\cos(\delta_{\perp} - \delta_{\parallel})$
5	$\frac{1}{2}\sqrt{2}\sin 2\theta_K\sin 2\theta_\mu\cos\varphi_h$	$ A_0A_{\parallel} $	$\cos{(\delta_{\parallel} - \delta_0)}$	$D\cos(\delta_{\parallel} - \delta_0)$	$C\cos(\delta_{\parallel}-\delta_{0})$	$-S\cos(\delta_{\parallel}-\delta_{0})$
6	$-\frac{1}{2}\sqrt{2}\sin 2\theta_K\sin 2\theta_\mu\sin \varphi_h$	$ A_0A_\perp $	$C\sin(\delta_{\perp}-\delta_0)$	$S\cos\left(\delta_{\perp}-\delta_{0} ight)$	$\sin(\delta_{\perp} - \delta_0)$	$D\cos\left(\delta_{\perp}-\delta_{0} ight)$
7	$\frac{2}{3}\sin^2\theta_{\mu}$	$ A_{\rm S} ^2$	1	-D	С	S
8	$\frac{1}{3}\sqrt{6}\sin\theta_K\sin2\theta_\mu\cos\varphi_h$	$ A_{\rm S}A_{\parallel} $	$C\cos\left(\delta_{\parallel}-\delta_{\rm S}\right)$	$S \sin (\delta_{\parallel} - \delta_{S})$	$\cos{(\delta_{\parallel} - \delta_{\rm S})}$	$D\sin(\delta_{\parallel} - \delta_{\rm S})$
9	$-\frac{1}{3}\sqrt{6}\sin\theta_{K}\sin2\theta_{\mu}\sin\varphi_{h}$	$ A_{\rm S}A_{\perp} $	$\sin (\delta_{\perp} - \delta_{S})$	$-D\sin(\delta_{\perp} - \delta_{\rm S})$	$C\sin(\delta_{\perp} - \delta_{\rm S})$	$S \sin (\delta_{\perp} - \delta_{S})$
10	$\frac{4}{\beta}\sqrt{3}\cos\theta_K\sin^2\theta_\mu$	$ A_{\rm S}A_0 $	$C\cos\left(\delta_0-\delta_{\rm S}\right)$	$S\sin(\delta_0 - \delta_S)$	$\cos\left(\delta_0 - \delta_S\right)$	$D\sin(\delta_0 - \delta_S)$

Pure penguin decays

 Decays forbiden at tree level. New Physics (NP) can enter in decay through loop diagrams (or penguin diagrams)



LH

• $B_s^0 \rightarrow \phi \overline{K}^{*0}$ and $B_s^0 \rightarrow K^{*0} \overline{K}^{*0}$ are pure penguin decays. No tree amplitude contribution



- Very good framework to find New Physics (NP) contributions, since new heavy particles can enter in loops
- They are $B \rightarrow V_1 V_2$ (V_i vector mesons). Angular analysis is necessary
- $B_{s}^{0} \rightarrow \phi \ \overline{K}^{*0}$ and $B_{s}^{0} \rightarrow K^{*0} \ \overline{K}^{*0}$ are studied. First observation of decays and measurement of longitudinal polarization fraction was performed

LHCb in numbers

- Vertex Finder
 - IP resolution≈ 20*mm*
 - $^\circ\,$ Decay time resolution pprox 45fs
- Tracking
 - $\circ \ \ \delta p/p = 0.4\% \ {\rm at} \ {\rm 5GeV} \ {\rm up} \ {\rm to} \ 0.6\% \ {\rm at} \ {\rm 100GeV}$



- Particle ID
 - RICH:
 - $\varepsilon_{PID}(K) \approx 95\%$
 - $MisID(K \rightarrow \pi) \approx 5\%$
 - Electromagnetic Calorimeter:
 - Resolution $\approx 1\% + 10\%/\sqrt{E}$ (GeV)
 - Muon ID:
 - $\varepsilon_{PID}(\mu)pprox 97\%$
 - MisID(μ) $\approx 1-3\%$



LHCb running conditions





- LHCb designed to run at lower luminosity than ATLAS/CMS
 - Tracking, PID sensitive to pile-up
 - $\circ~$ Mean number of interactions/bunch crossing ~ 2
- pp beams displaced to reduce instantaneous luminosity
- For $\mathcal{L} = 1 \text{fb}^{-1}$ about $3 \cdot 10^{11} b\overline{b}$ produced

LHCb upgrade

- Take quark flavour physics to the precision and very high precision regime
 - Towards experimental sensitivities matching theoretical uncertainties
- Upgrade detector and trigger system
 - Full readout at 40 MHz and availability of full event info from first-stage software trigger

Installation in 2018-19

- \Rightarrow ready for data taking in 2020
- □ Collect ~ 50 fb⁻¹
- Gain in collected yields from
 - (1) increased luminosity and (2) trigger
 - Trigger efficiencies for hadronic decays saturate with present trigger system
 - Inst. lumi: 4×10³² cm⁻² s⁻¹ → 2×10³³ cm⁻² s⁻¹



* Integrated luminosity always include lumi. from previous runs

Eduardo Rodrigues

CKM 2014, Vienna, Austria, 11 Sep. 2014

Observable	LHC run I	LHC run II	LHC run III	
$\phi_s(B^0_s o J/\psi \phi) \text{ [rad]}$	0.050	0.025	0.009	
$\phi_s(B^0_s \to J/\psi f_0) \text{ [rad]}$	0.068	0.035	0.012	



$\Delta\Gamma_S$ sign ambiguity

There are two possible fit solutions: $\Delta \Gamma_s$, ϕ_s and $-\Delta \Gamma_s$, $\pi - \phi_s$

- For physical solution:
 - P-wave phase (δ_{\perp}) increases rapidly across $\phi(1020)$ mass resonance
 - S-wave phase (δ_s) varies slowly
- Measuring $\delta_s \delta_{\perp}$ in bins of $M(K^+K^-)$ resolves the ambiguity
- LHCb results using $\mathcal{L} = 1 \text{fb}^{-1}$ in 6 bins of $M(K^+K^-)$



LHC





The **physical solution** has to decrease in bins of $M(K^+K^-)$



 B^0_{s}

[arXiv:1407.2222]



$B_s^0 o \phi \phi$

- Similar CKM phases as for $B_s^0 \rightarrow J/\psi K^+ K^-$
- Mixture of CP eigenstates, 2 CP-even and 3 CP-odd
- Angular analysis needed

Sample

- Analysed 3 fb⁻¹ LHCb data
- Clean signal in purely hadronic channel: $N \sim 4000$ events
- Selection based on Boosted Decision Tree
- Similar resolution and effective tagging power

Decay dominated by penguin diagram:



[to appear in Phys. Rev. D, arXiv:1407.2222]



0

cosθ

-0.5

0

0.5

 $\cos\theta$.

-0.5 0.5 Φ[rad] 35 / 35