

Studies on the Cherenkov Effect for Improved Time Resolution of TOF-PET using digital SiPM

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Outline

- **Motivation:** time-of-flight positron emission tomography
- **Fast photon detection:** digital **SiPM**
- Factors influencing the **time resolution of scintillators**
- Improving the time resolution of scintillators using the **Cherenkov effect**
 - **Simulation** investigations
 - **Proof of principle** measurements
 - Comparing Cherenkov radiators scintillators

Motivation

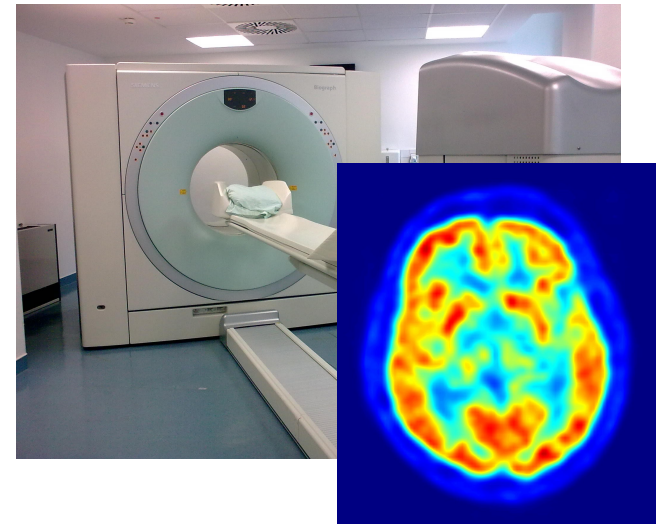
Fast particle/gamma detection is applied in many research fields:

- Material research (positron annihilation life time spectroscopy)
- Particle ID (time of flight detectors in high energy physics)
- ...

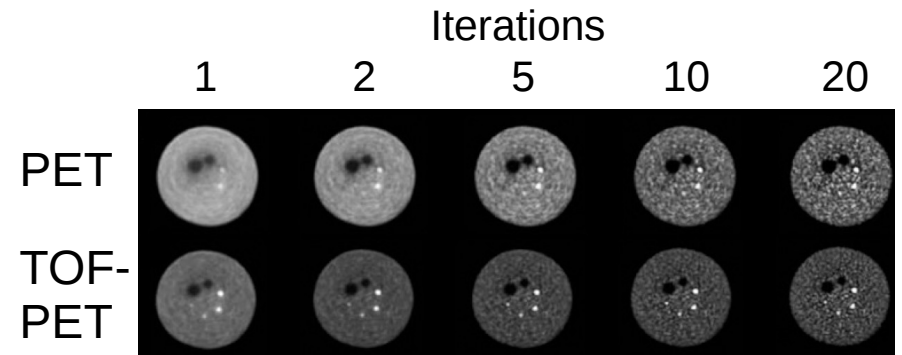
Main motivation:

Time-of-Flight Positron Emission Tomography (TOF-PET)

- TOF for PET allows to decrease the SNR of reconstructed PET pictures
- Dependent on the time resolution of the PET detectors



Ref. : <http://de.wikipedia.org/wiki/Positronen-Emissions-Tomographie>

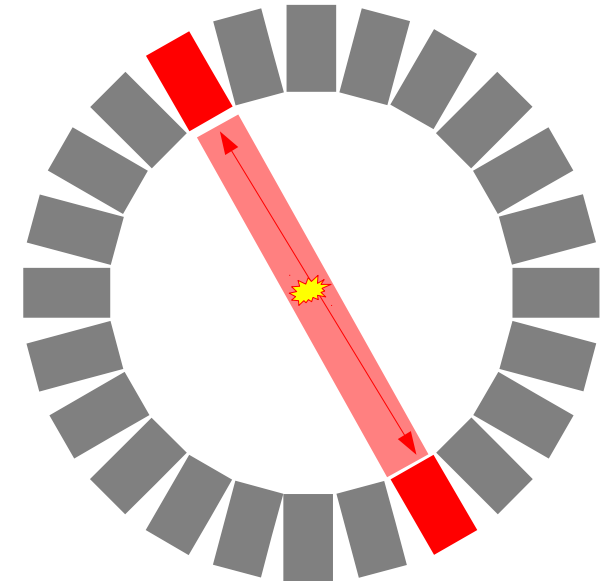
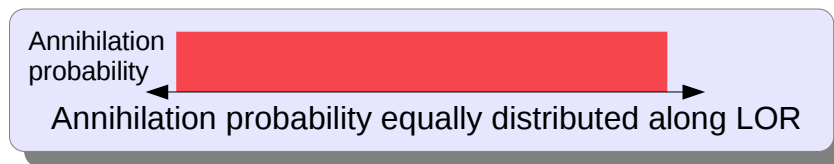


Karp et al., JNM, 49-3 (2008) pp.462-470

Positron Emission Tomography

PET

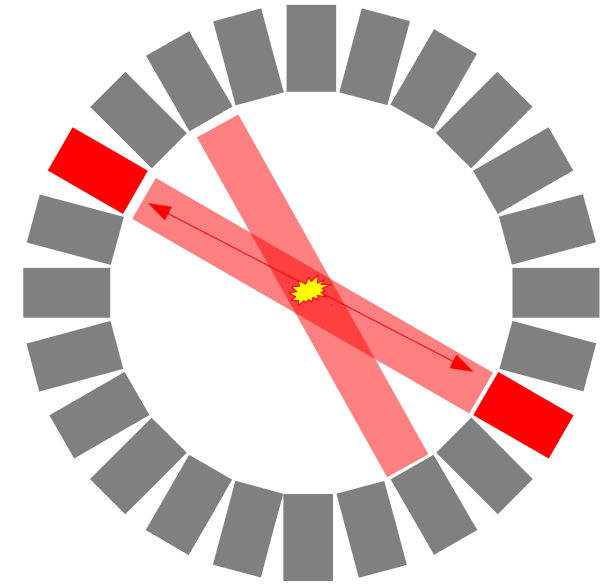
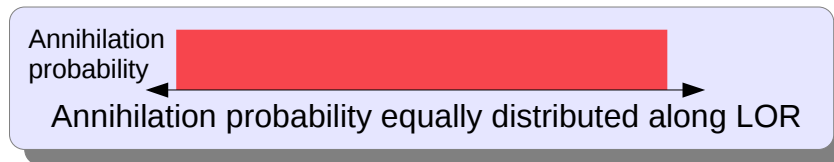
- Radiotracer (e.g. sugar + e^+ emitter) injected into patient
- Tracer accumulates at region of interest (e.g. metabolic tissue)
- e^+ annihilates with e^- of tissue
- Emission of two annihilation photon with 511keV at rel. angle of 180°
- The two photons are detected by a ring of detectors (within coinc. time window)
- A LOR is drawn between the responding detectors
- Statistics \rightarrow Image reconstruction



Positron Emission Tomography

PET

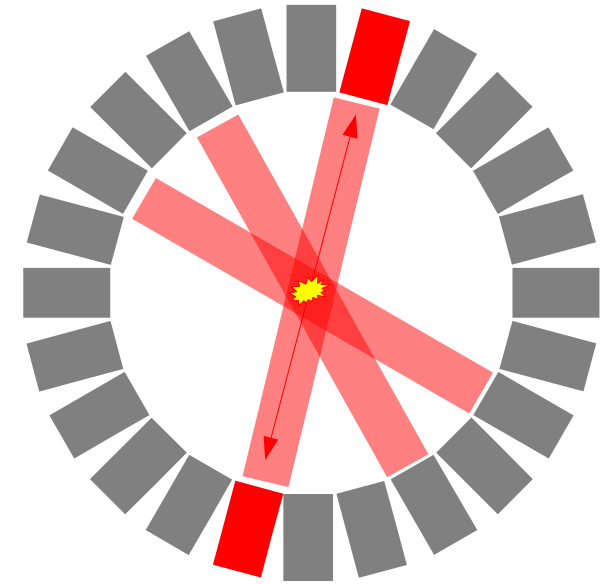
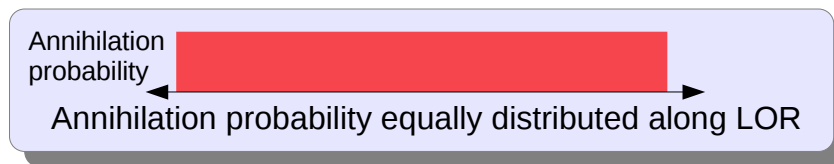
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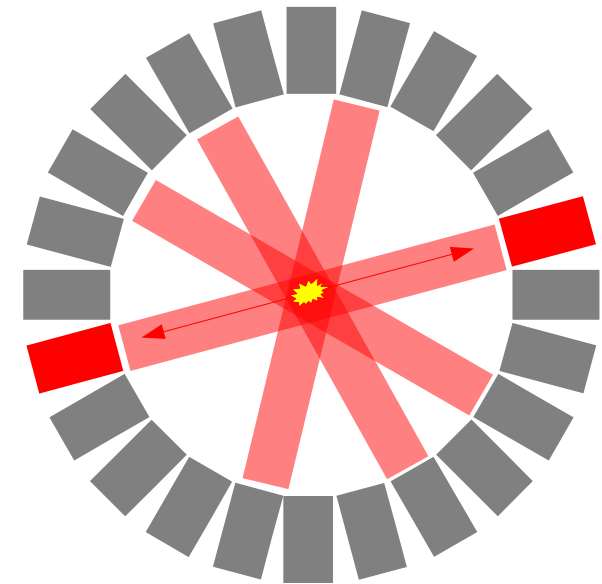
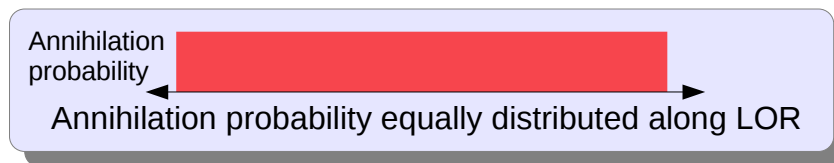
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Positron Emission Tomography

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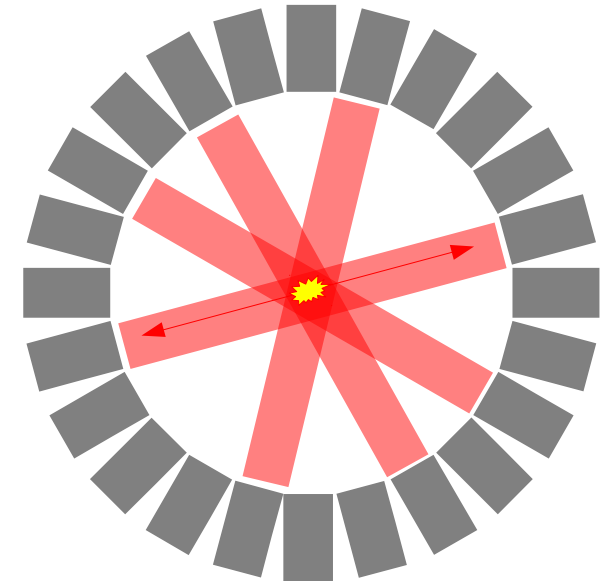
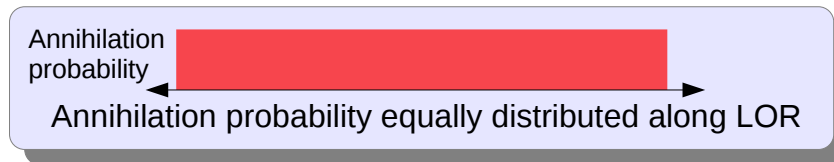
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Time-of-flight PET

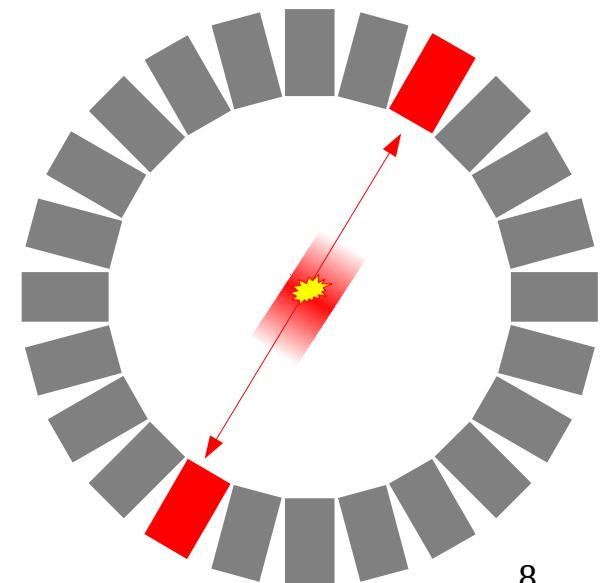
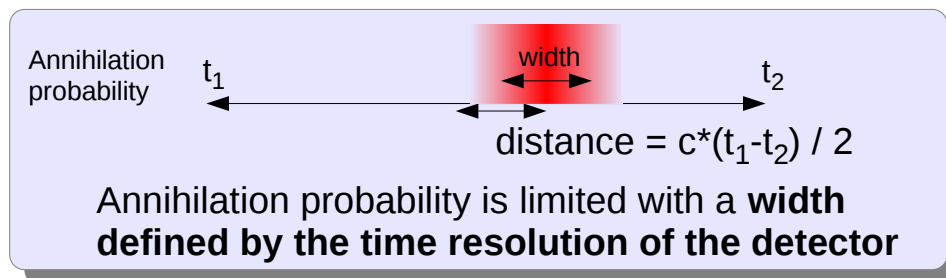
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TOF-PET

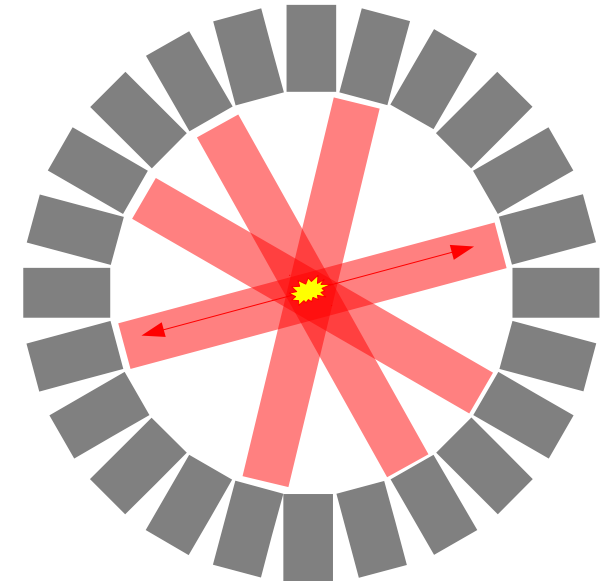
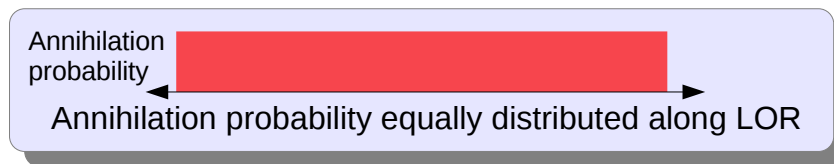
- arrival **time** of the 511keV photons is **measured**,
- LOR between responding detectors with a probability distribution
 - \rightarrow **Less artefacts**
 - \rightarrow **Improved SNR**



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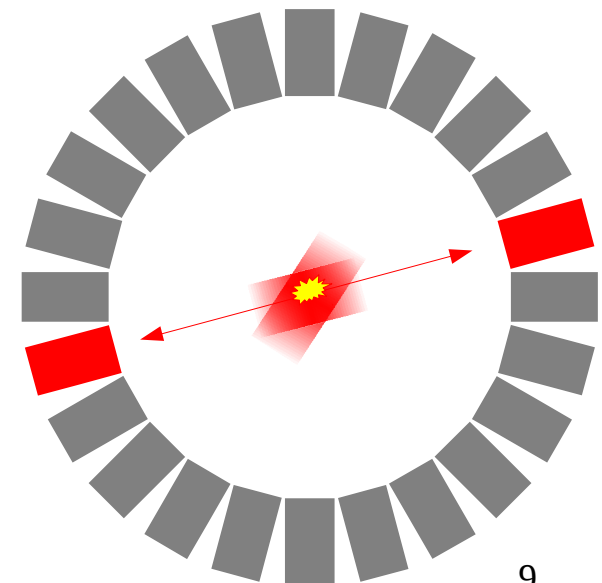
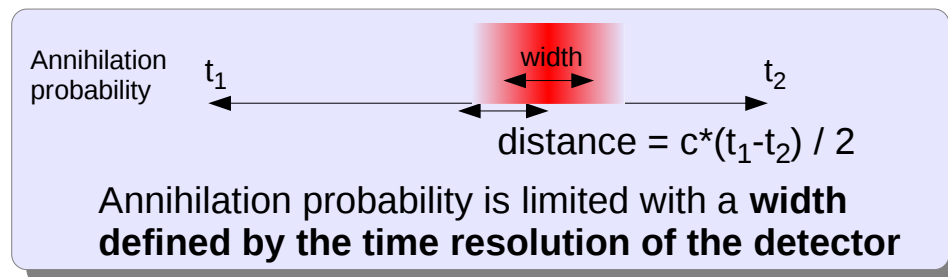
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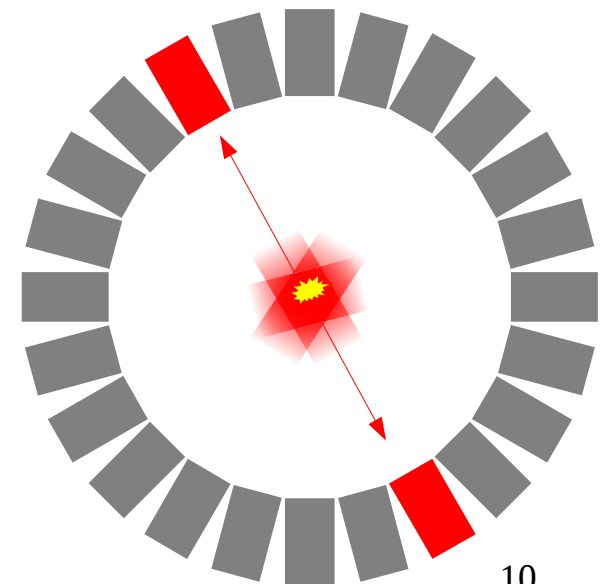
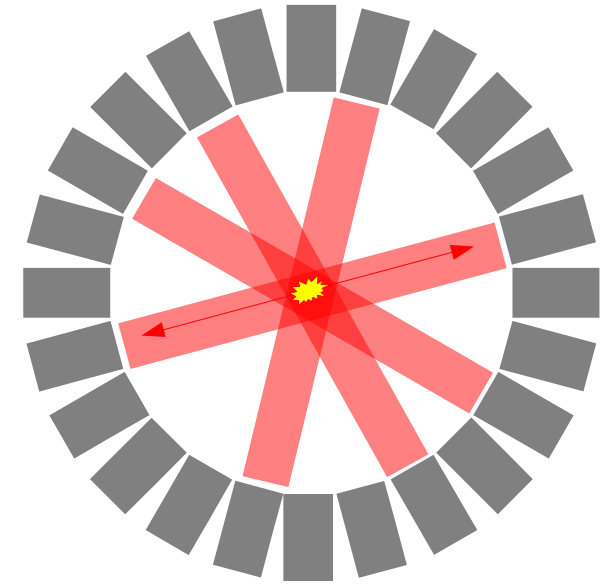
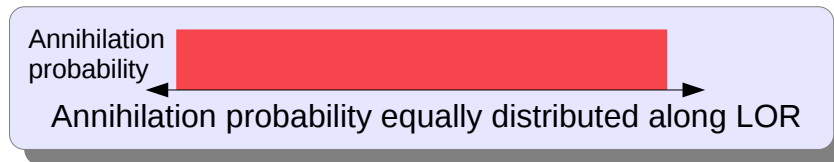
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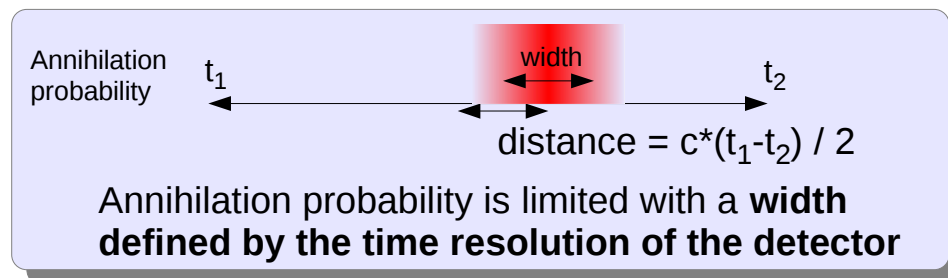
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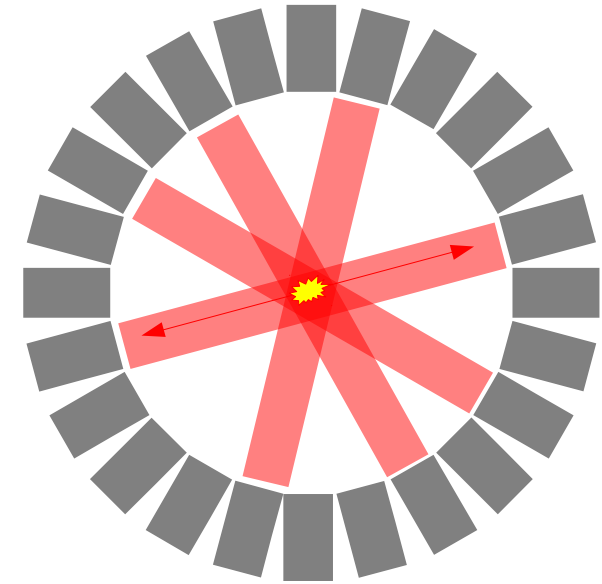
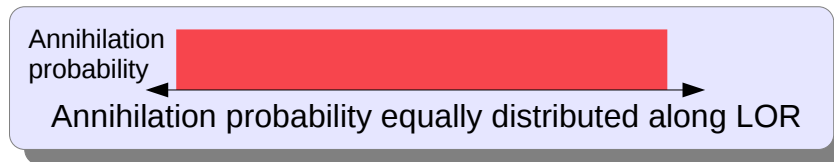
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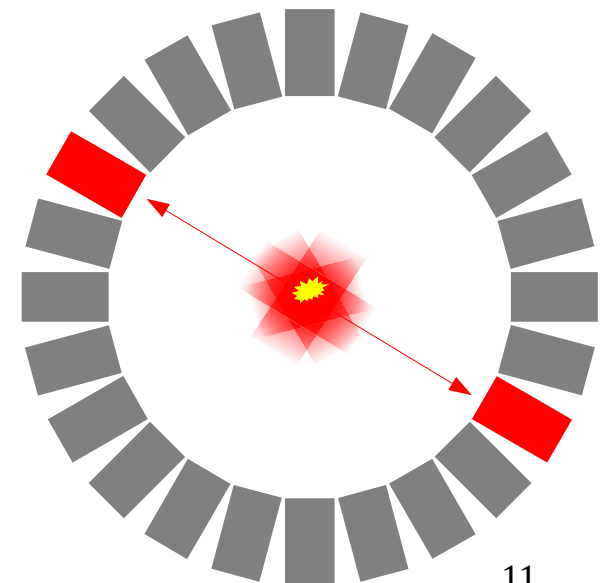
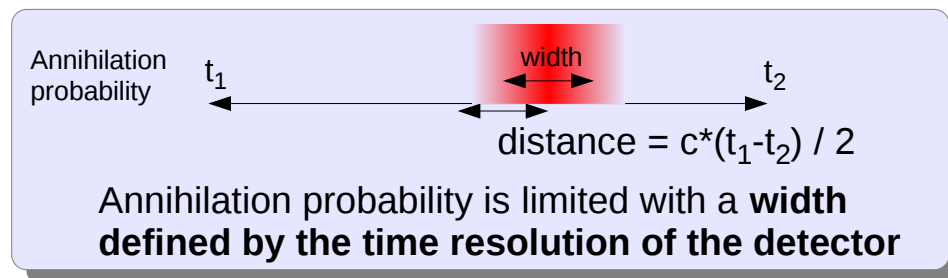
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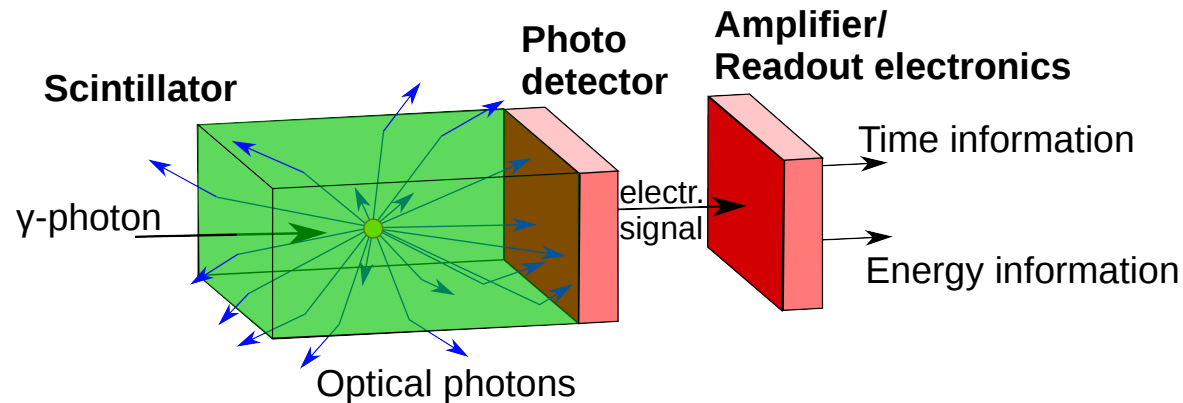
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Scintillation based gamma/particle detection

A scintillation detector consists of 3 major parts:

- **Scintillator:** Converting energy of particle/ γ -photon into optical photons
- **Photo detector:** Converts optical photons into electric signal
- **Amplifier/Readout electronics:** Amplifies the signal and digitizes it

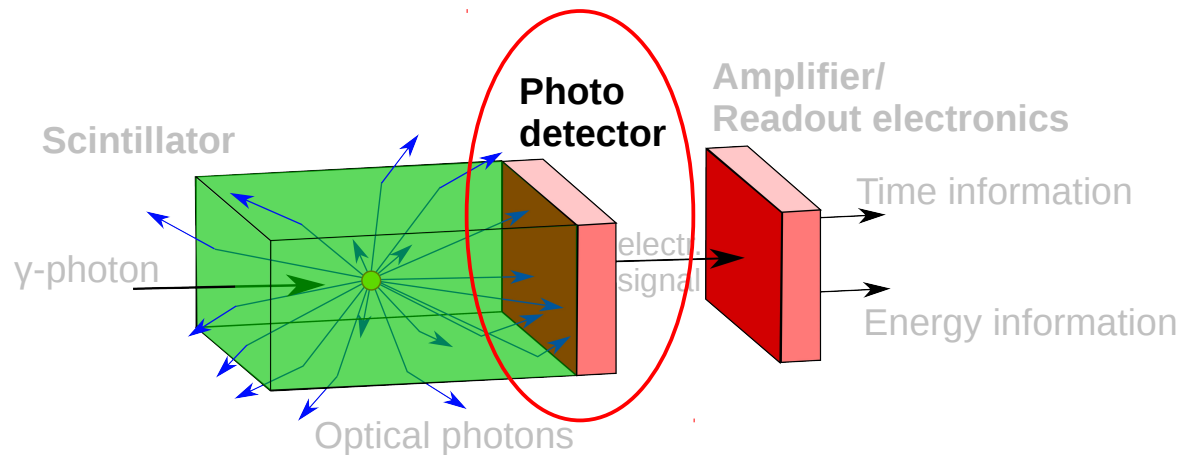


Every part is adding time spread to the total time resolution.

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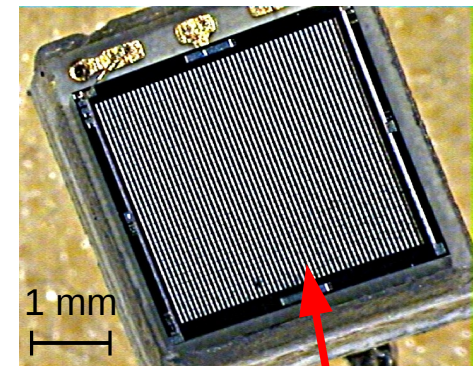
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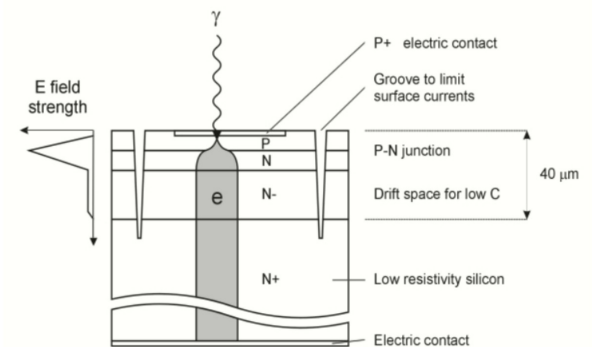
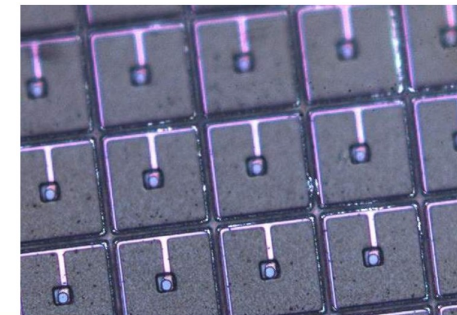
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The silicon photomultiplier

- Solid state detector based on silicon
- Array of miniature avalanche photo diodes driven in Geiger mode
- Sensitive area a few mm² (typically 3x3mm²)
- High gain ($\sim 10^6$) → detection of single photons
- Very fast, insensitive to magnetic fields, high PDE, compact, robust, cheap, low power consumption
- Well suited detectors for many kinds of detectors in HEP and nuclear imaging (PET)
- Drawbacks: high dark count rate (100 kHz/mm²), crosstalk, after pulses, temperature sensitivity



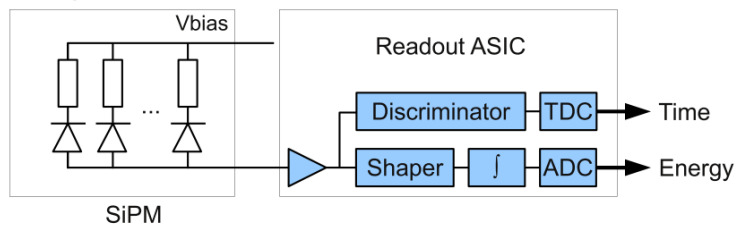
50 x 50 cells



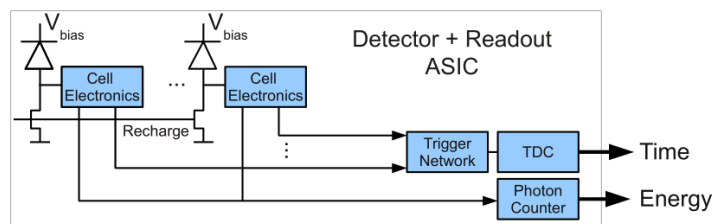
Ref: Renker et al., JINST 4 (2009) P04004

The analogue vs. the digital SiPM

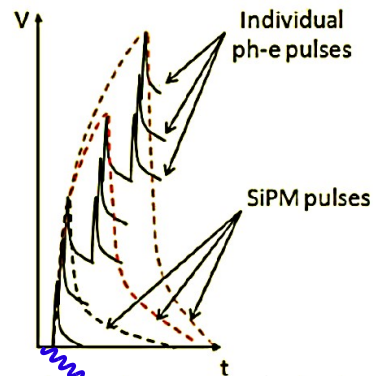
Analog Silicon Photomultiplier Detector



Digital Silicon Photomultiplier Detector



Ref.: Frach, JINST 7 (2012) C01112



0	1	0	0
0	0	0	1
1	0	0	0
0	0	1	0
0	0	0	0

Photon number
+ time of the first photon

- SiPM is an analogue device
- Provides quasi digital information about the number of detected photons

Analogue SiPM:

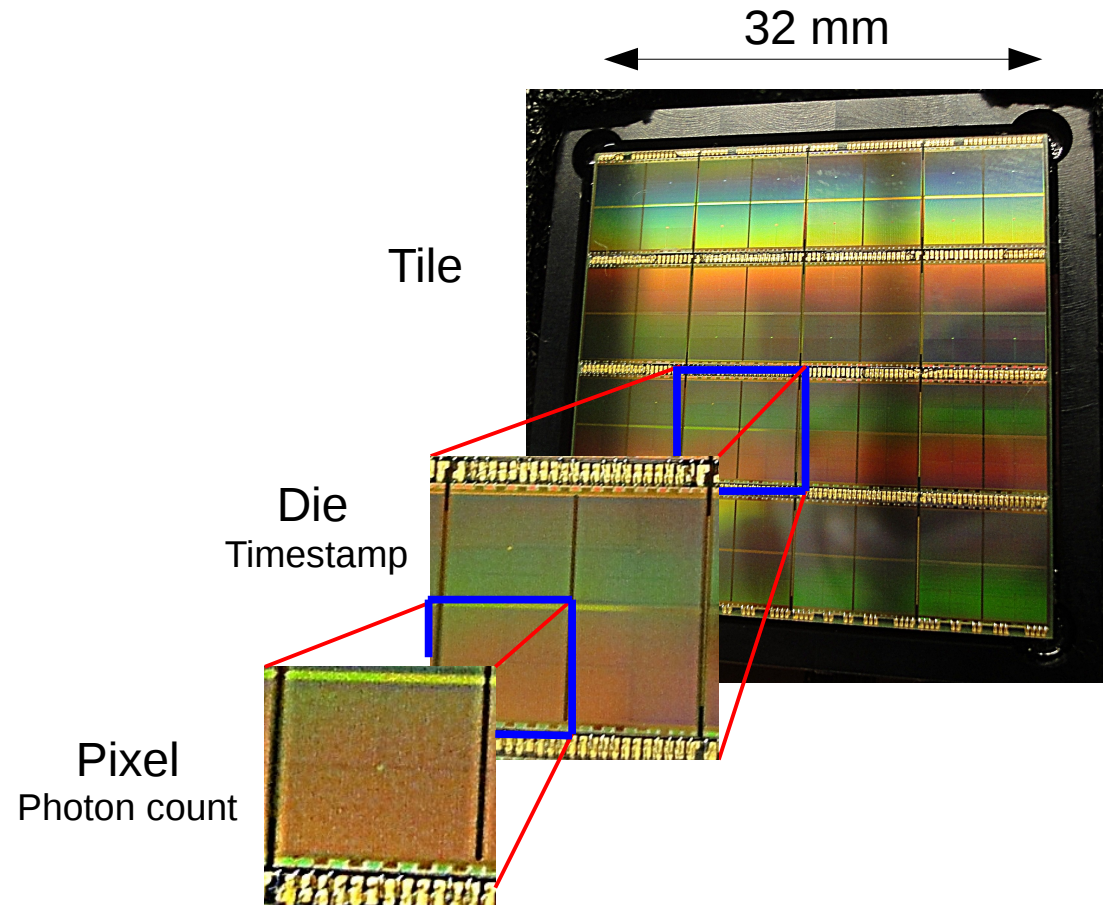
- Signal is the analogue sum of the single cells

Digital SiPM:

- Each SPAD connected to logic electronics
- Signal is the digital sum of fired SPADs
- **Advantages:** Electronics as close as possible at the SPADs (**fast, accurate**), control of single SPADs (**reduction of darkcounts**)

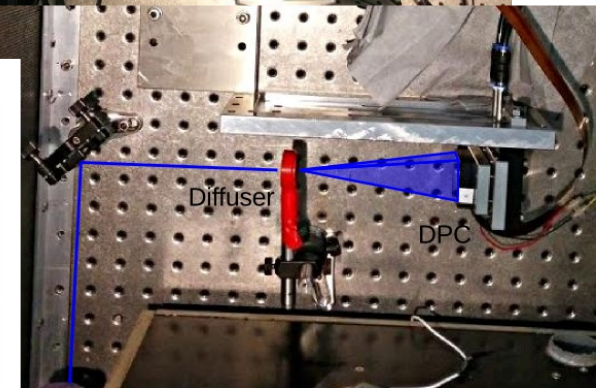
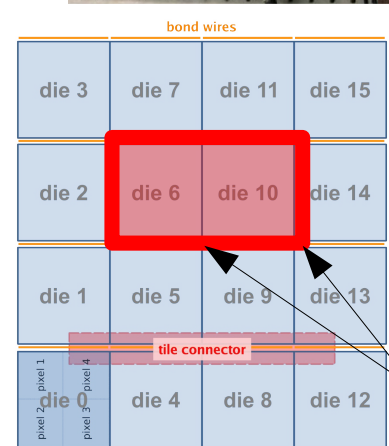
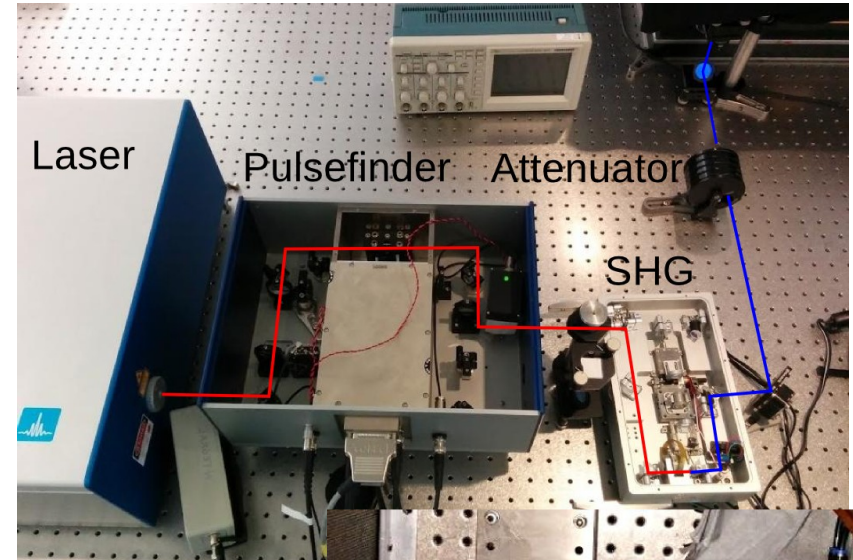
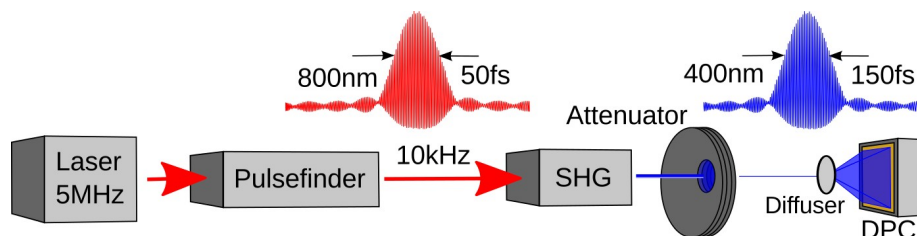
The Philips Digital Photon Counter (DPC)

- DPC consists of 16 dies ($\sim 3 \times 3 \text{ cm}^2$)
- Each die consists of 4 pixels
- Each pixel consists of 3200/6400 microcells
- Each cell can be turned on/off individually
- One time stamp per die
- One photon count per pixel
- 16 timestamps / 64 photon counts



Time resolution of the digital SiPM: setup

- Femtosecond laser
- Laser at detector: $\lambda = 400\text{nm}$, $\Delta t = 150\text{fs}$, rep. rate = 10kHz
- 1 DPC tile, two pixels/dies in coincidence
- Trigger level: 1 photon
- At low photon levels: no validation, no intergration
- Two dies or pixels activated, give timestamp t and number of triggers n
- The time resolution was determined by calculating the **standard deviation** of $t_1 - t_2$ dependent on n



Coincidence

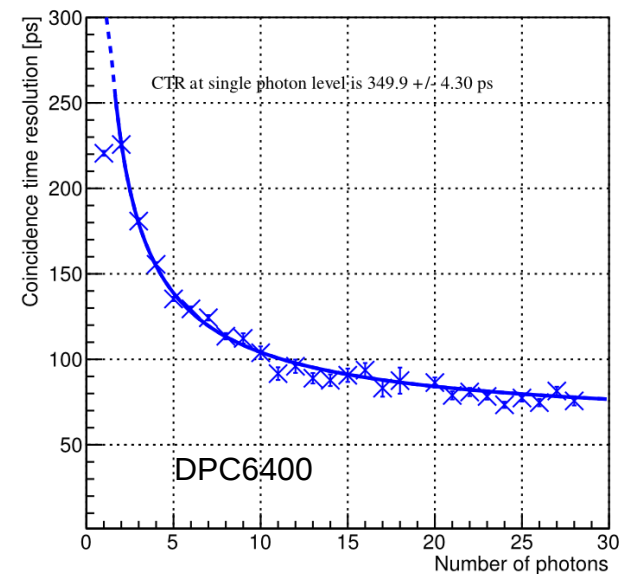
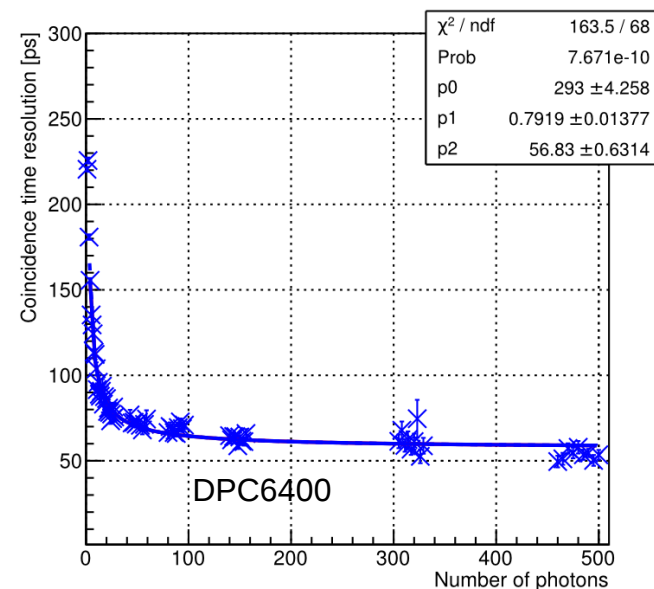
Time resolution of the digital SiPM: Results

Single photon **coincidence**
time resolution

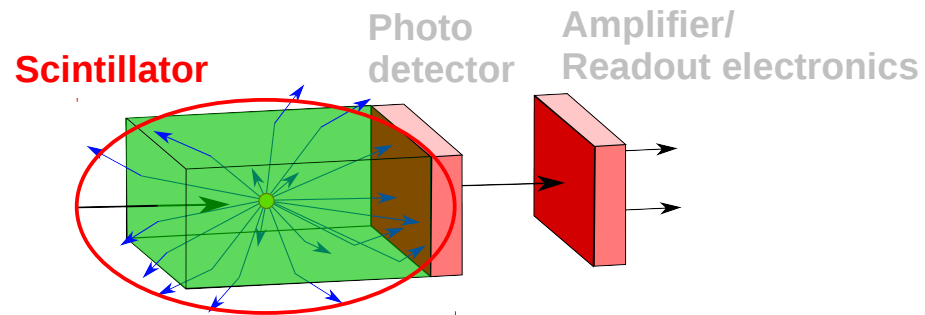
DPC	Active cells	T [°C]	Laser rate [kHz]	Inact. cells [%]	SPCTR [ps] FWHM	System (coinc.) [ps]
3200	die	0	10	0	265 ± 8.4	67 ± 2.7
3200	die	0	10	20	238 ± 4.3	60 ± 1.2
3200	die	0	10	50	216 ± 3.3	64 ± 0.8
3200	die	10	10	20	361 ± 17.7	66 ± 0.9
3200	pixel	10	10	20	143 ± 3.9	22 ± 3.4
3200	pixel	20	10	20	160 ± 4.9	20 ± 4.4
6400	die	0	10	20	350 ± 4.3	57 ± 0.6

Ref.: S.E. Brunner, PhD thesis, Vienna UT (2014)

Time resolution prop. $1/n^p$ (expected by simulation).
Drop of SPCTR when approaching single photon level.



Factors influencing the time resolution of scintillators & Improvement by the Cherenkov effect



The Cherenkov effect

- Dielectric material
- Charged particle ●
- Faster than the speed of light in the medium
- Constructive interference of electromagnetic pulses by polarisation of the atomic dipoles
- Cherenkov emission angle θ

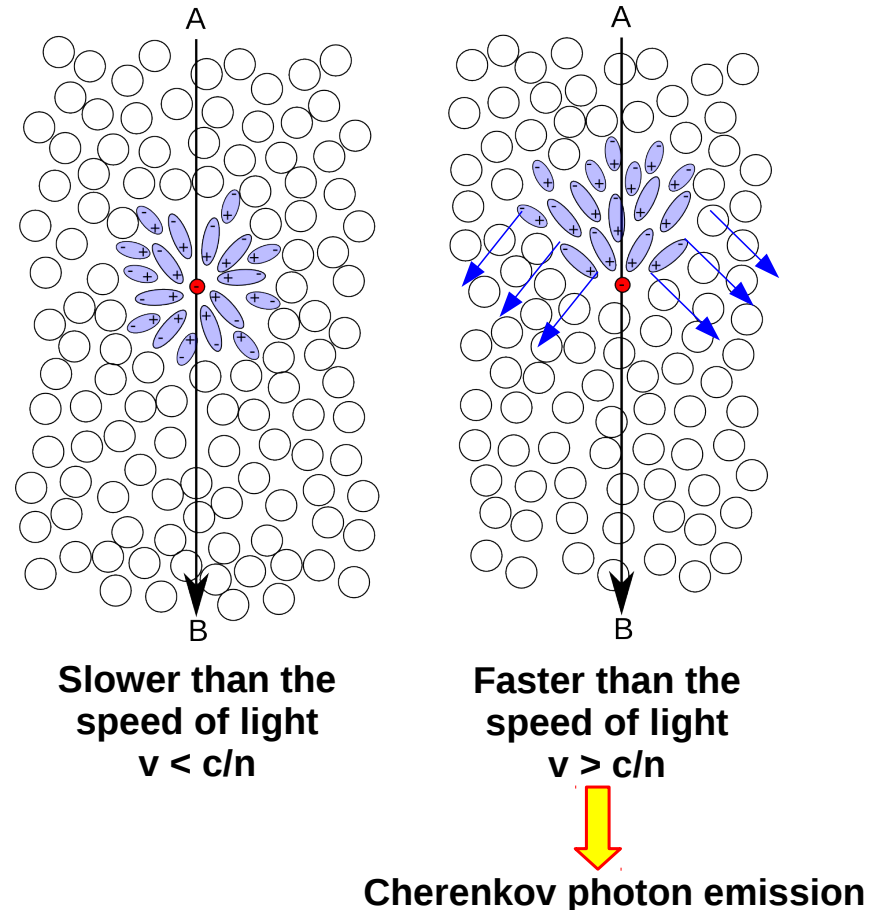
$$\cos \theta = \frac{1}{\beta n}$$

- Number of emitted Cherenkov photons

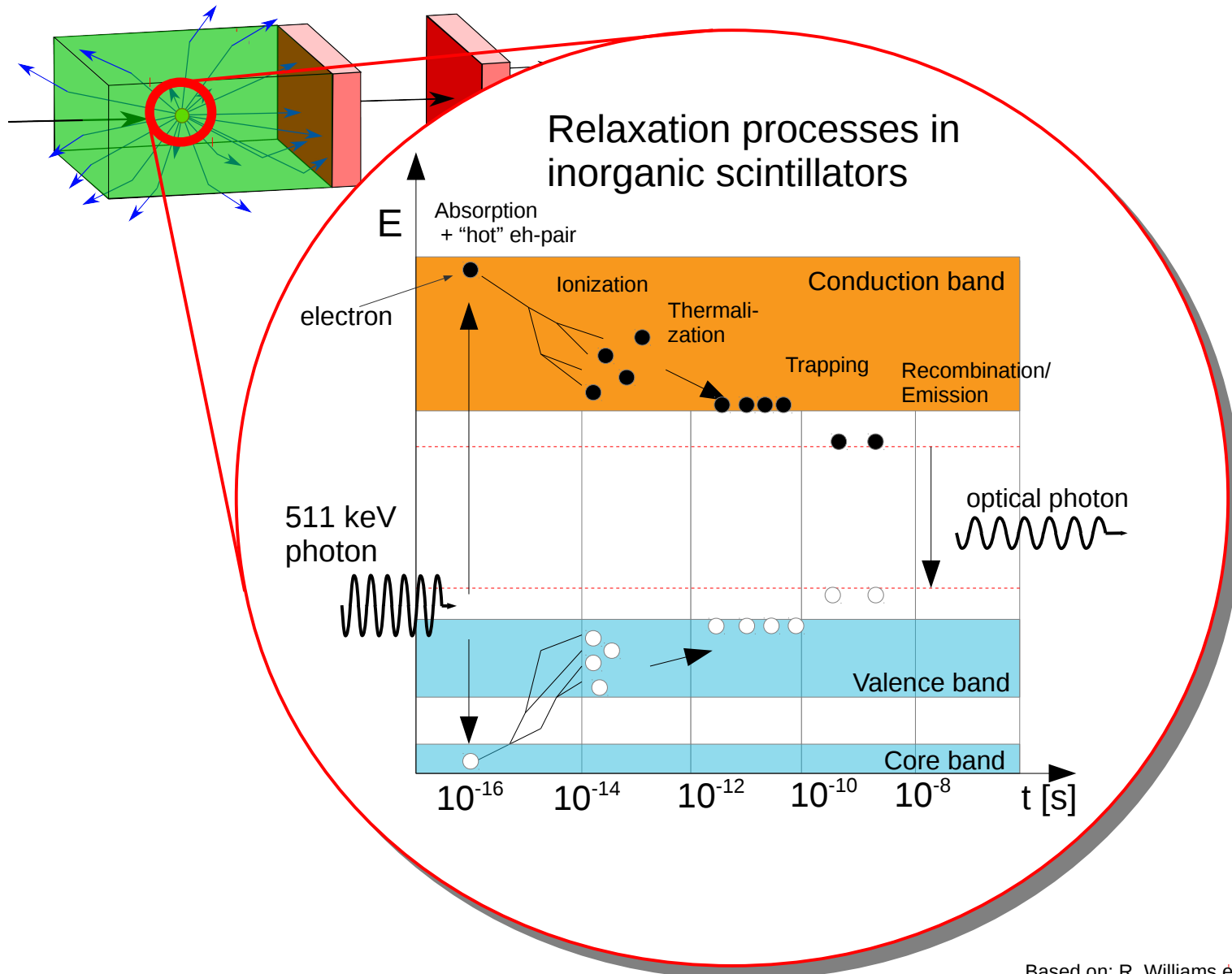
$$\frac{dN^2}{dx d\lambda} = \frac{2\pi z^2 \alpha}{\lambda^2} \cdot \left(1 - \frac{1}{\beta^2 n^2(\lambda)}\right)$$

- Emission spectrum (Frank-Tamm)

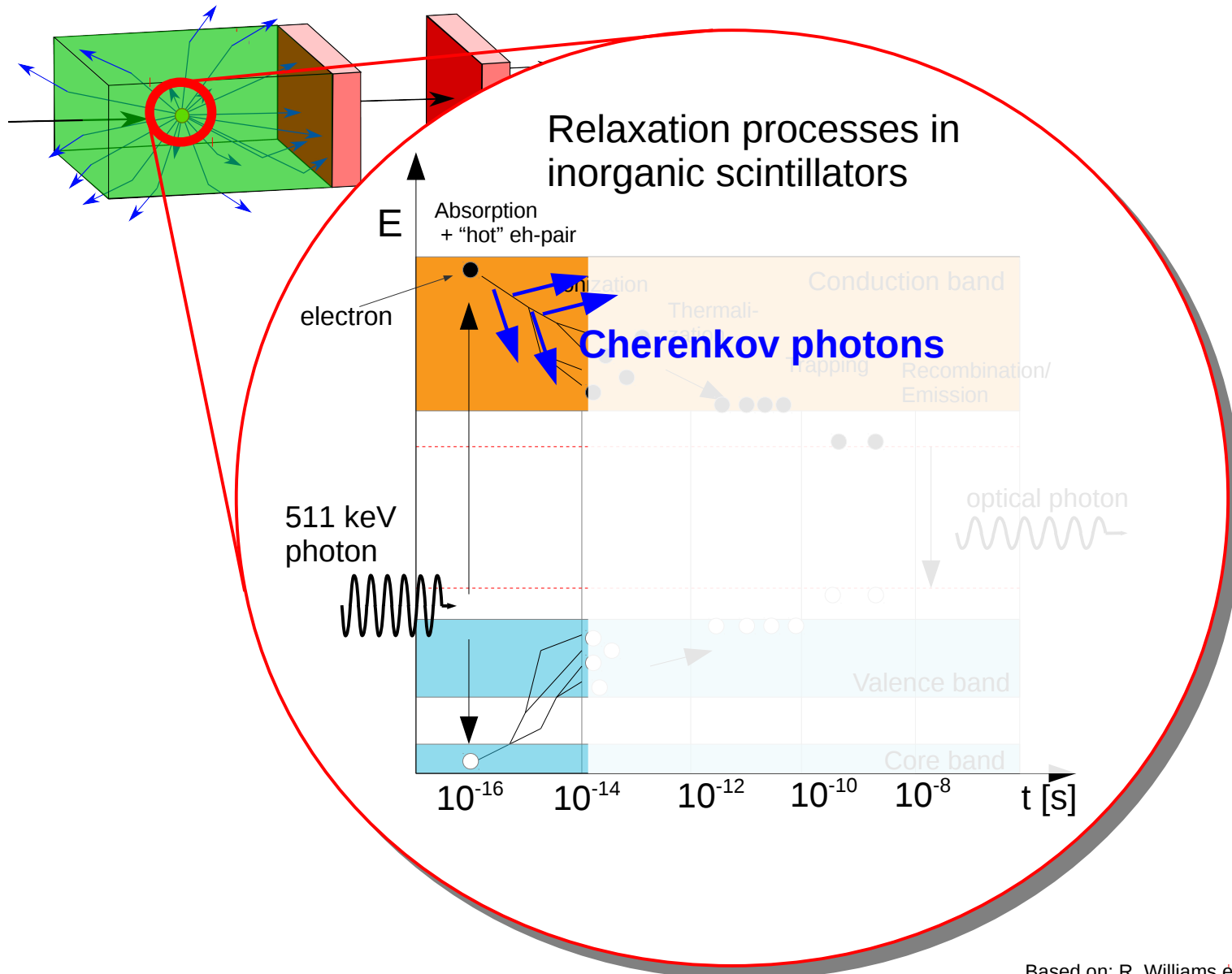
$$N(\lambda) \sim 1/\lambda^2$$



Gamma-photons and the Cherenkov effect

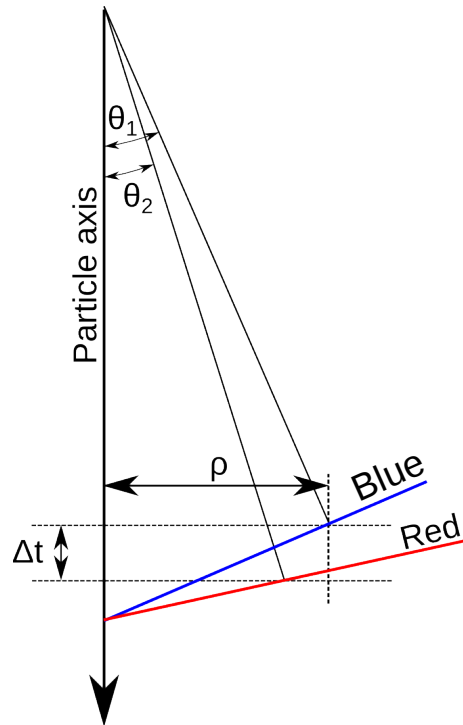


Gamma-photons and the Cherenkov effect

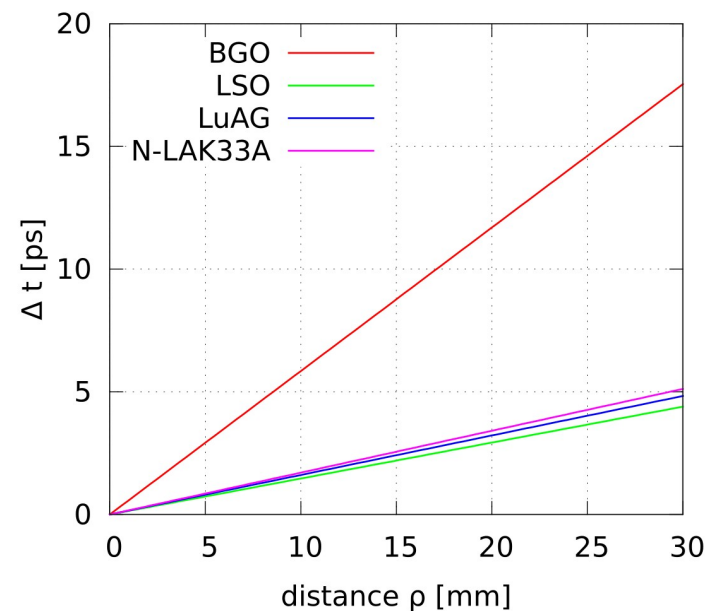


Time precision of the Cherenkov effect

Cherenkov photons are emitted almost instantaneously.



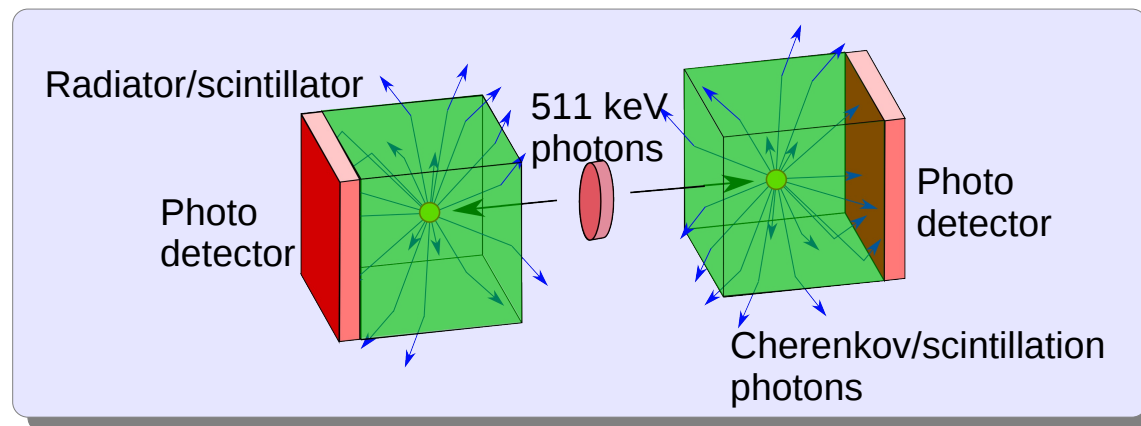
- Influence of **electron propagation** inside the material:
 - Electron range $\sim 200\text{-}300\mu\text{m}$, velocity $\geq \beta_t = 1/n$
 - time spread $\sim \mathbf{1\text{-}2\text{ ps}}$
- **Dispersion:** Angle of Cherenkov emission is dependent on the wavelength, $\cos \theta = 1/\beta n(\lambda)$



Ref.: S. E. Brunner, PhD thesis, Vienna UT (2014)

Investigating the Cherenkov effect for gamma detection: simulation environment

- Monte Carlo simulations using Geant4 (v9.4.p3, Livermore libraries)
- Basic setup: **scintillator** attached to a **generic photo detector** (TR=0, QE=1)
- Size scintillator: $3 \times 3 \times 3 \text{ mm}^3$, photo detector $3 \times 3 \text{ mm}^2$
- Perfectly polished surface, no wrapping, surrounded by air
- Comparing various materials (high density, high n):
 - **pure Cherenkov radiators:** N-LAK33A/B, N-FK5, N-LASF31A, P-SF68, LuAG
 - **hybrid materials:** LuAG:Ce, LSO:Ce, BGO, PWO



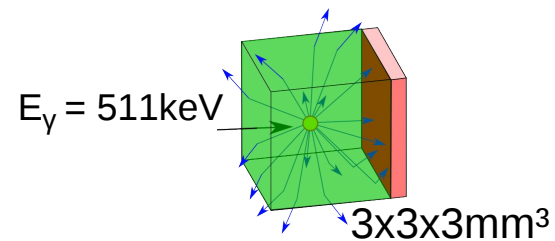
Cherenkov photon yield for 511keV annihilation photons (simulation)

Material	Luminescence type*	Density [g/cm ³]	n	Cutoff wavel. [nm]	Created photons (avrg.)	Detected photons (avrg.) [3x3x3mm ³]
N-LAK33A	Cherenkov	4.22	1.77	300	22.4	13.7
N-LAK33B	Cherenkov	4.22	1.77	280	24.9	14.5
N-FK5	Cherenkov	2.45	1.5	260	26.1	14.6
N-LASF31A	Cherenkov	5.51	1.91	310	19.6	12.1
P-SF68	Cherenkov	6.19	2.07	400	12.8	8.4
LuAG pure	Cherenkov	6.73	1.84	180	32	10.6
LuAG:Ce	hybrid	6.73	1.84	250	24.3	7.2
LSO:Ce	hybrid	7.4	1.82	390	13.8	1.1
BGO	hybrid	7.13	2.15	310	32.8	4.6
PWO	hybrid	8.28	2.2	340	22.6	3.8

Ref.: S. E. Brunner, PhD thesis, Vienna UT (2014)

*Cherenkov: photon emission via the Cherenkov effect

Hybrid: simultaneous photon emission via the Cherenkov effect and scintillation



Factors influencing the Cherenkov photon yield

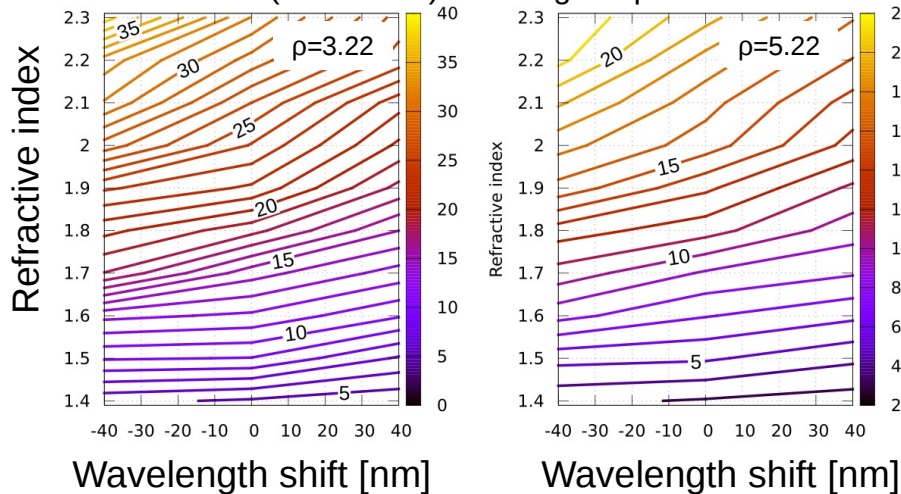
Cherenkov photon yield

$$\frac{dN^2}{dx d\lambda} = \frac{2\pi z^2 \alpha}{\lambda^2} \cdot \left(1 - \frac{1}{\beta^2 n^2(\lambda)}\right)$$

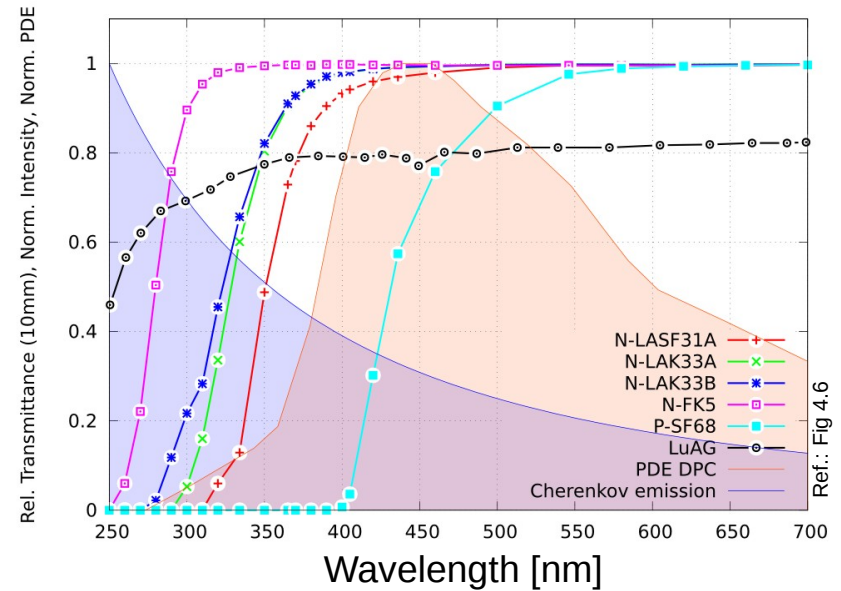
Dependent on

- Transmission
- Refractive index
- Density (electron range)

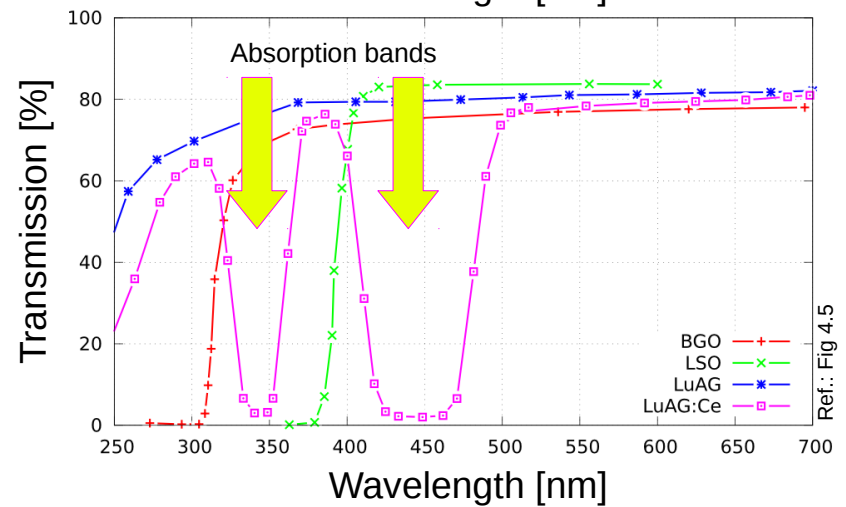
Simulated number of Cherenkov photons in N-LAK33A (3x3x3mm³) reaching the photo detector



Ref.: Fig 4.9



Ref.: Fig 4.6



Ref.: Fig 4.5

Ref.: S. E. Brunner, PhD thesis, Vienna UT (2014)

Comparing factors influencing the time resolution of scintillators and Cherenkov radiators

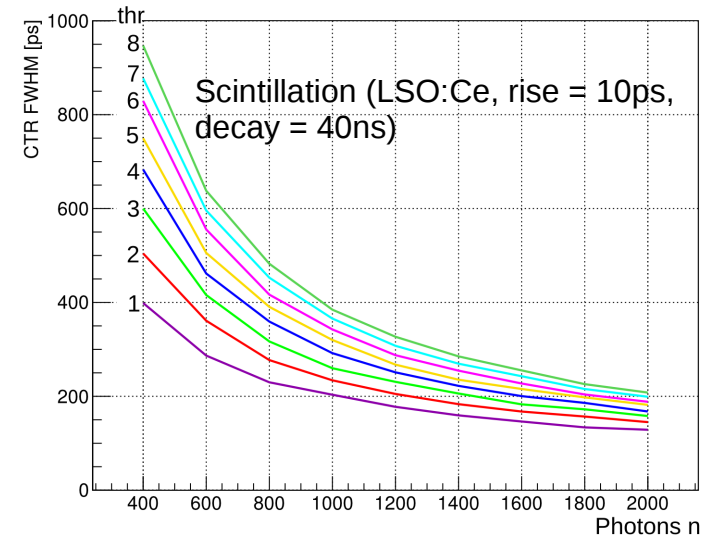
- **Photon statistics** (rise & decay time, light yield)
- **Depth of interaction** (crystal dimension, density)
- **Photon propagation** (crystal dimension, transmission)

Influence of photon statistics

- **Simulation** using a double exponential function for scintillation photon emission after gamma absorption at θ

$$f(x|\theta) = \begin{cases} \sum_i \frac{P_i}{\tau_{d,i} - \tau_{r,i}} \left[e^{-\frac{x-\theta}{\tau_{d,i}}} - e^{-\frac{x-\theta}{\tau_{r,i}}} \right], & \text{for } x \geq \theta \\ 0, & \text{else} \end{cases}$$

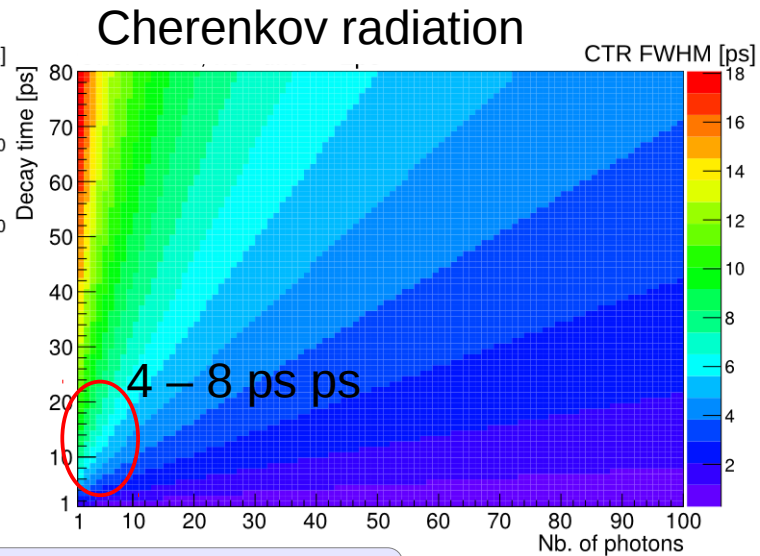
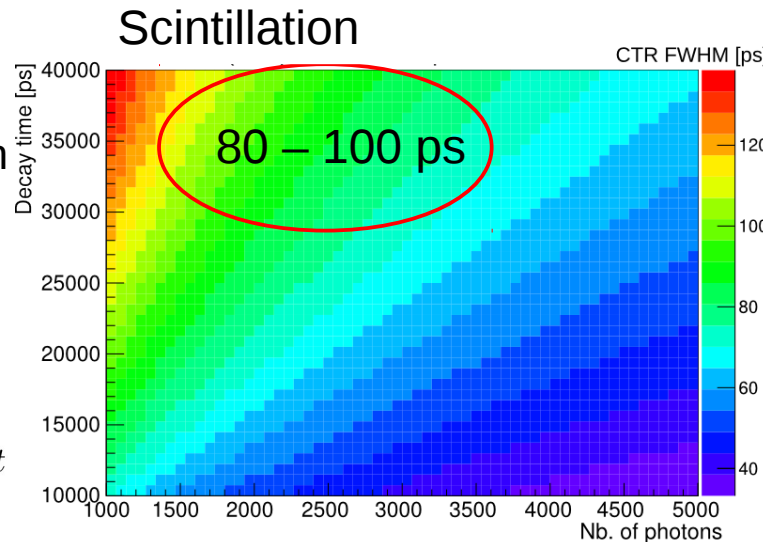
The time resolution improves with **increasing number of photons** and **decreasing threshold** (first photon provides the best time resolution if rise time is short)



- **Analytical approach:** improved version of estimation of approach by Post & Schiff, Lynch, Wright:

$$P(Q, t) = \frac{f(t)^Q e^{-f(t)}}{Q!}$$

$$W(Q, t) \cdot dt = P_{Q-1}(t) \cdot \frac{df}{dt} dt$$



The time resolution improves for **shorter rise- and decay times** and **increasing light yield**. Cherenkov emission provides much **better intrinsic time resolution** than fast state-of-the-art scintillators.

Influence of DOI and photon propagation

- Simulation, LSO:Ce 3x3x30mm³
Compare **photon arrival times at detector** of scintillation and Cherenkov emission

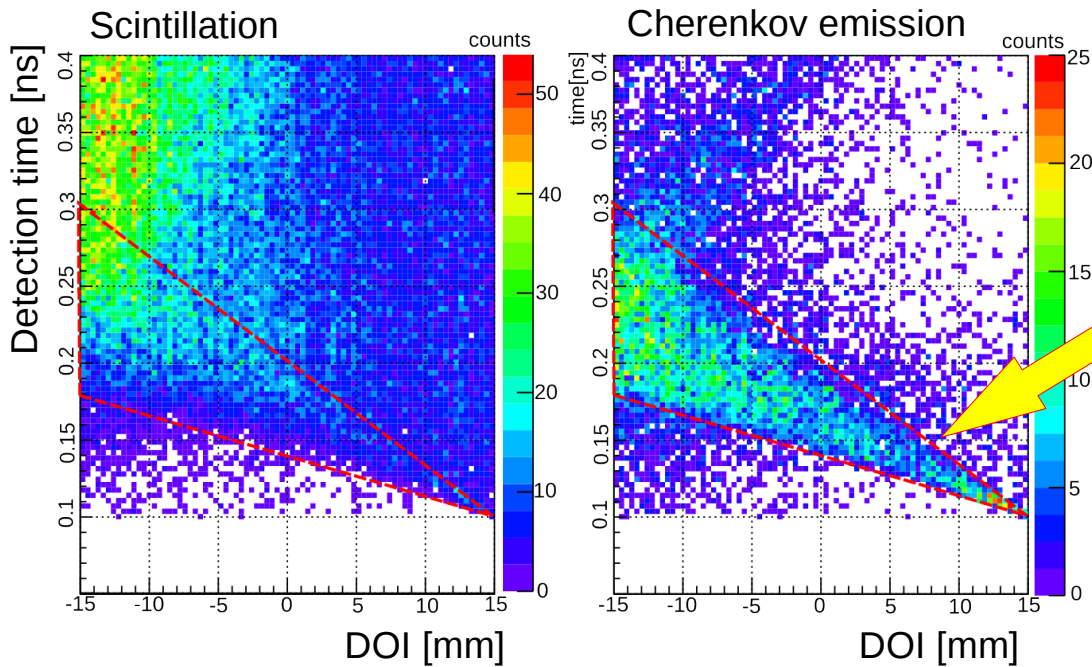
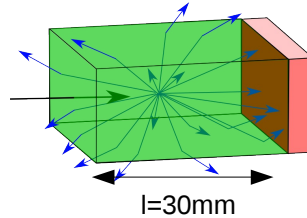
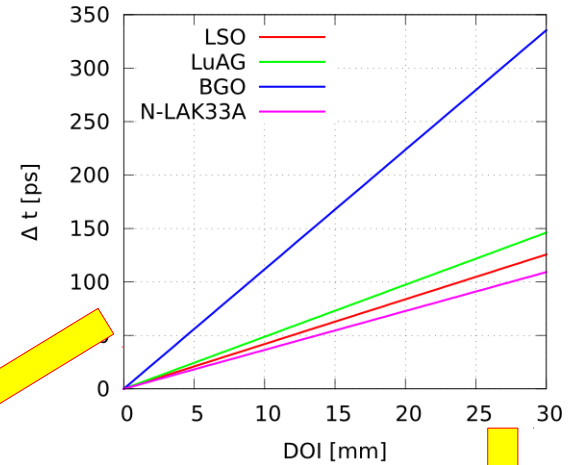


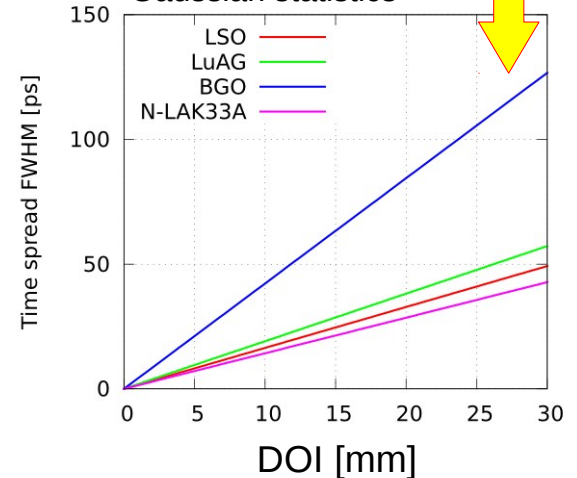
Figure 4.20

Maximum possible time spread

$$\Delta t = t_{\max} - t_{\min} = DOI \cdot \frac{n_{\text{cr}}}{c} \left(\frac{n_{\text{cr}}^2}{n_{\text{det}}^2} - 1 \right)$$



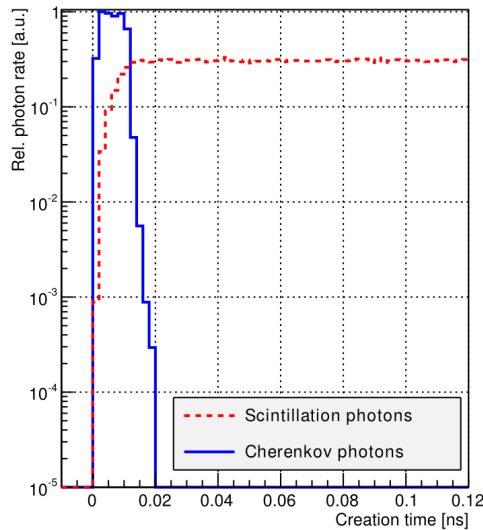
Time spread assuming Gaussian statistics



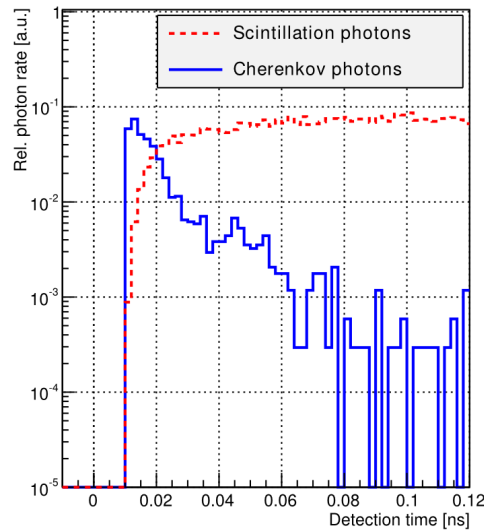
Influence of DOI and photon propagation can be reduced by shortening the crystals (efficiency for γ -detection decreases).

Comparing creation and arrival times of scintillation and Cherenkov photons

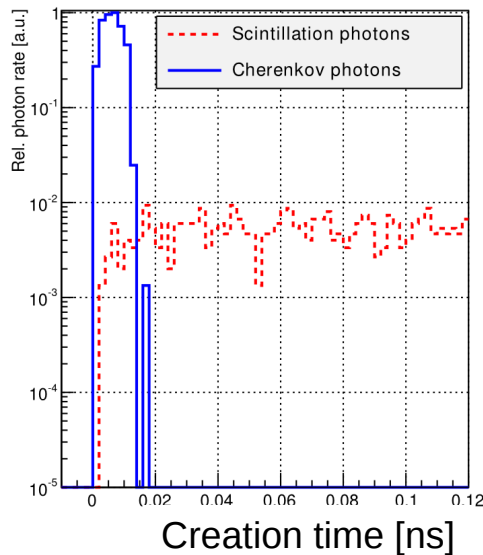
LSO:Ce Photon creation



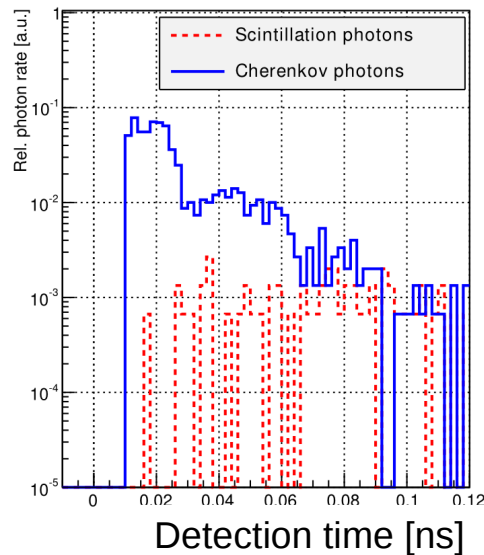
Photon detection



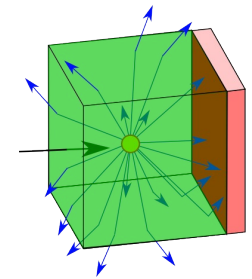
PWO Photon creation



Photon detection



- Cube with 3x3x3mm³



- Calculating “yield ratio” within time window

$$\text{Yield ratio} = \frac{n_{\text{Cherenkov}}}{n_{\text{scintillation}}}$$

- Yield ratio = $\frac{n_{\text{Cherenkov}}}{n_{\text{scintillation}}}$

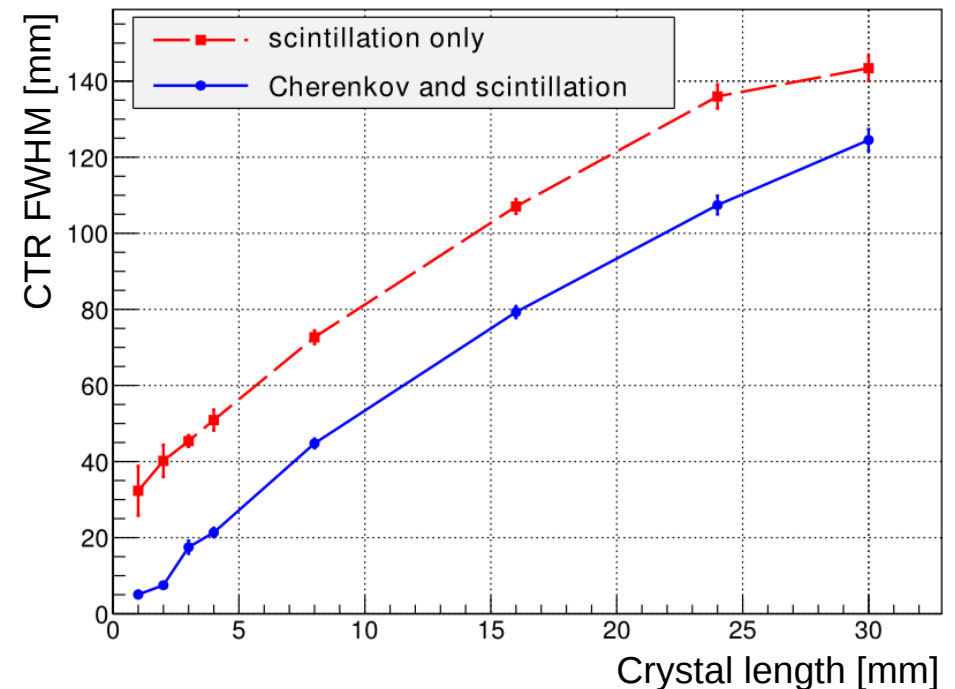
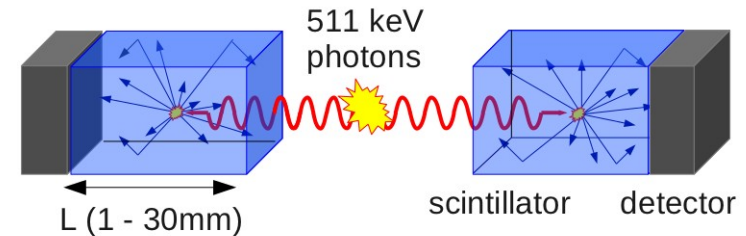
	created		detected	
	<25ps	<100ps	<25ps	<100ps
LSO:Ce	1.77	0.34	1.78	0.16
LuAG:Ce	11.5	2.1	41.5	3.4
BGO	122	24.2	364	28
PWO	86	16.6	134	21

Ref.: Brunner et al., IEEE Trans. Nucl. Sci. 61 (2014) p. 443

Impact of the Cherenkov effect on the coincidence time resolution

- Simulation of a coincidence setup
- LSO:Ce, length $l = 1-30\text{mm}$
- Determination of the coincidence time resolution with and without the Cherenkov effect
- On average 1-2 Cherenkov photons were detected in each crystal per event
- Cherenkov photons clearly **improve** the **CTR** for all crystal lengths
- Influence of **crystal length** (DOI + photon propagation) on the CTR is visible

Improvement of the CTR due to Cherenkov emission \leftrightarrow **fast time constants**.
Improvement of the CTR with decreasing crystal length \leftrightarrow **DOI & photon propagation**.



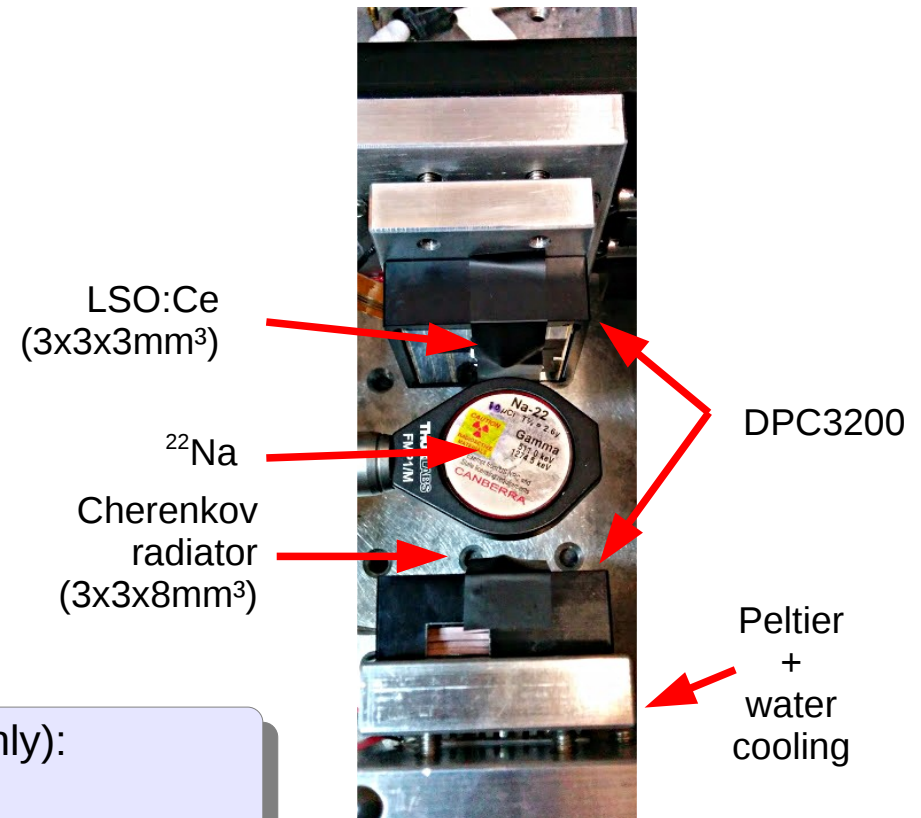
Improving the time resolution of scintillators using the Cherenkov effect: proof of principle measurements

The Cherenkov effect for annihilation photon detection: setup

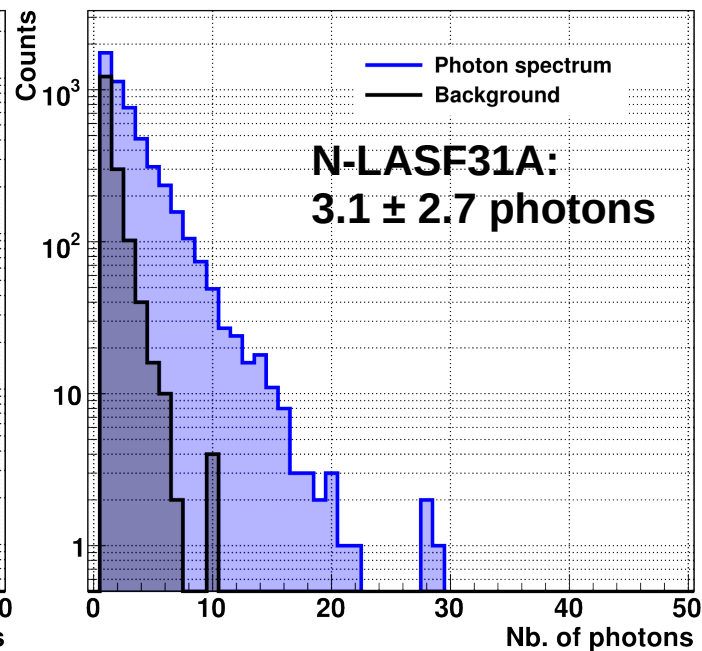
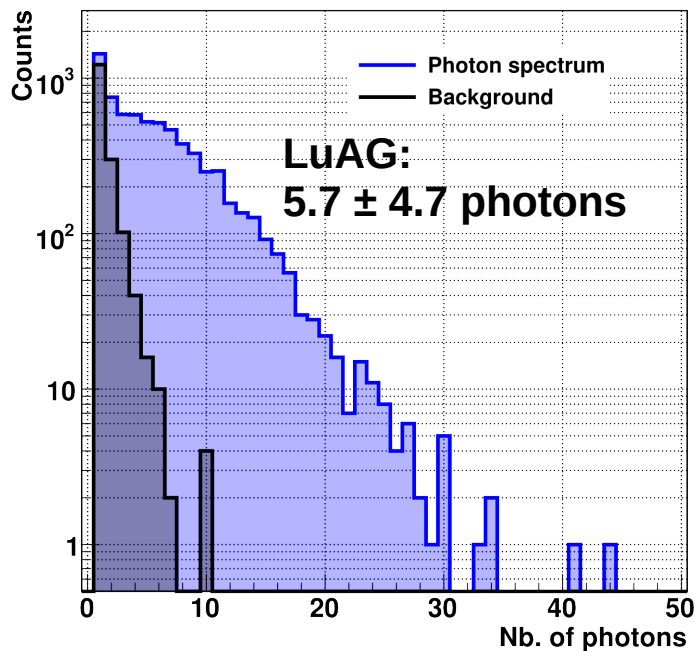
- Coincidence setup using ^{22}Na
- Photo detectors: Philips DPC3200
- Temp.: -18°C , 10% cells off
- **LSO:Ce** ($3\times 3\times 3\text{mm}^3$) as **reference** detector
- **Cherenkov radiator** ($3\times 3\times 8\text{mm}^3$) for investigations
- Surface: polished, no wrapping

Materials

- ◆ **Pure** Cherenkov radiators (Cherenkov emission only):
LuAG, N-LASF31A
- ◆ **Hybrid** materials (Cherenkov emission and scintillation occur):
LuAG:Ce, BGO

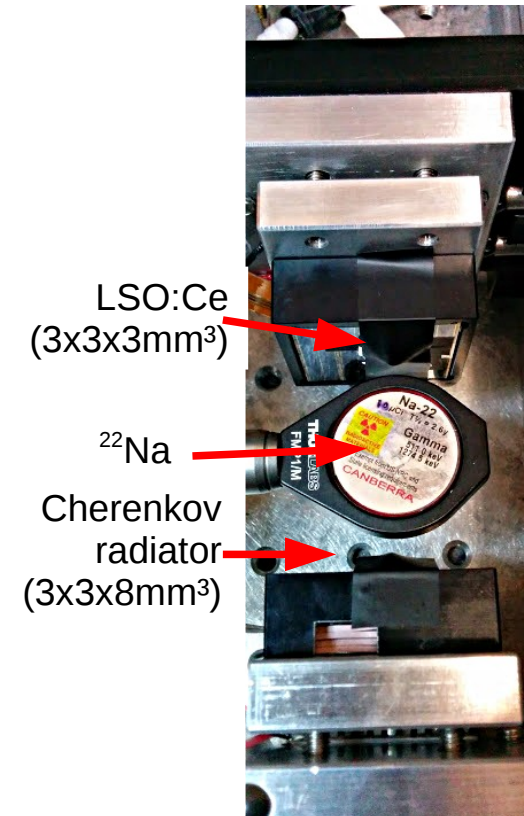


Proof of principle measurement: Cherenkov photon yield

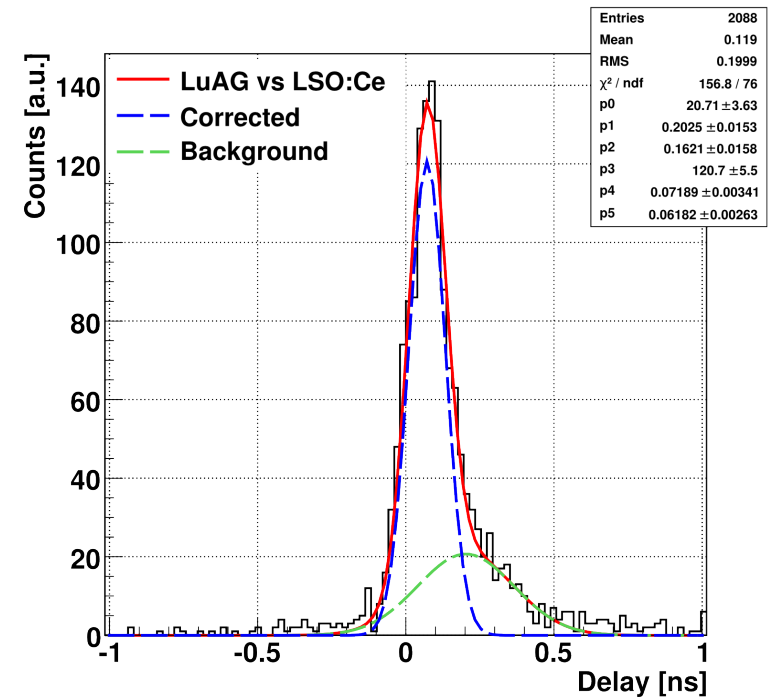


Ref.: S. E. Brunner, PhD thesis, Vienna UT (2014)

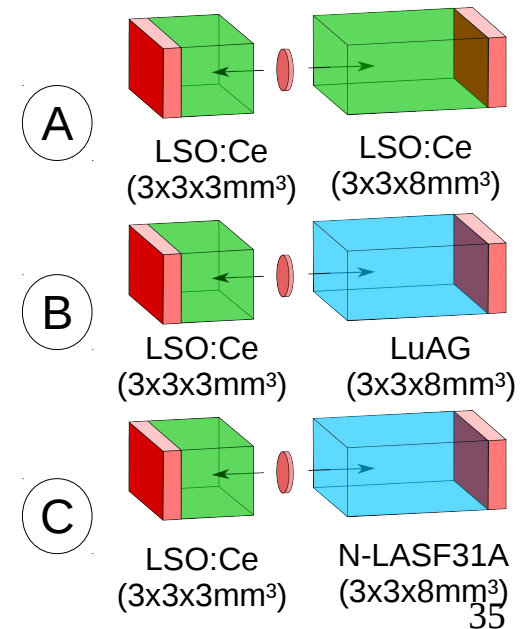
- Temp. -18°C, inhibited cells 10%
- Crystal sizes: 3x3x8mm³, polished, no wrapping
- Cut on photoelectric absorption of annihilation photons at reference detector



Proof of principle measurements: Time resolution with pure Cherenkov radiators

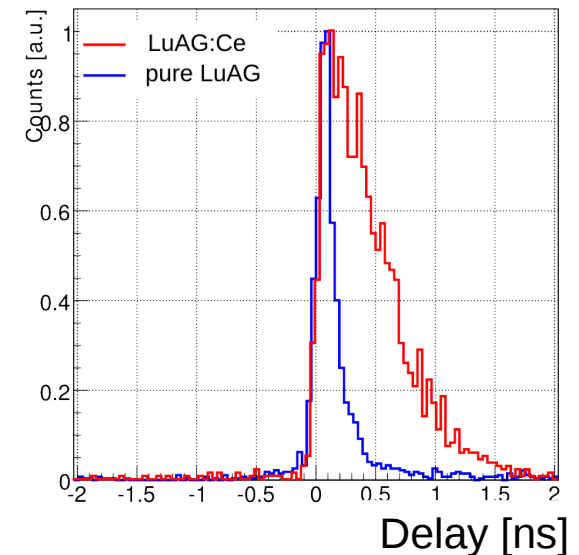
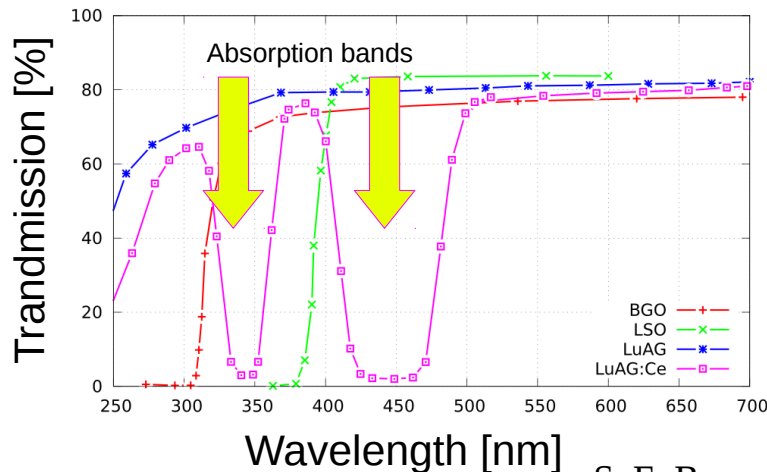
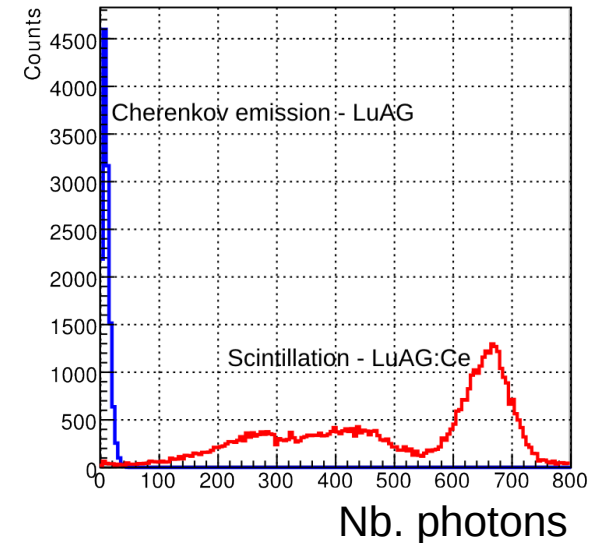


Crystal 1	Crystal 2	Length 1 [mm]	Length 2 [mm]	Thr 2 [photons]	Setup	CTR [ps]
LSO:Ce	LSO:Ce	3	8	photo-p.	(A)	192 ± 4
LSO:Ce	LuAG	3	8	6	(B)	146 ± 16
LSO:Ce	LuAG	3	8	4-6	(B)	145 ± 6
LSO:Ce	N-LASF31A	3	6	(C)	178 ± 16	



Time resolution with hybrid scintillators

- Undoped LuAG shows only Cherenkov emission
- Ce doped LuAG shows **Cherenkov emission and scintillation**
- Cherenkov emission is fast → **good time resolution**
- Scintillation provides high light output → **good energy resolution** (necessary for rejecting scattered events in PET)
- A **hybrid material** offers **both** advantages
- **Challenge:** in undoped LuAG Cherenkov photons can be detected in doped LuAG:Ce many Cherenkov photons get absorbed → better material: **BGO**



Time resolution using hybrid Cherenkov radiators

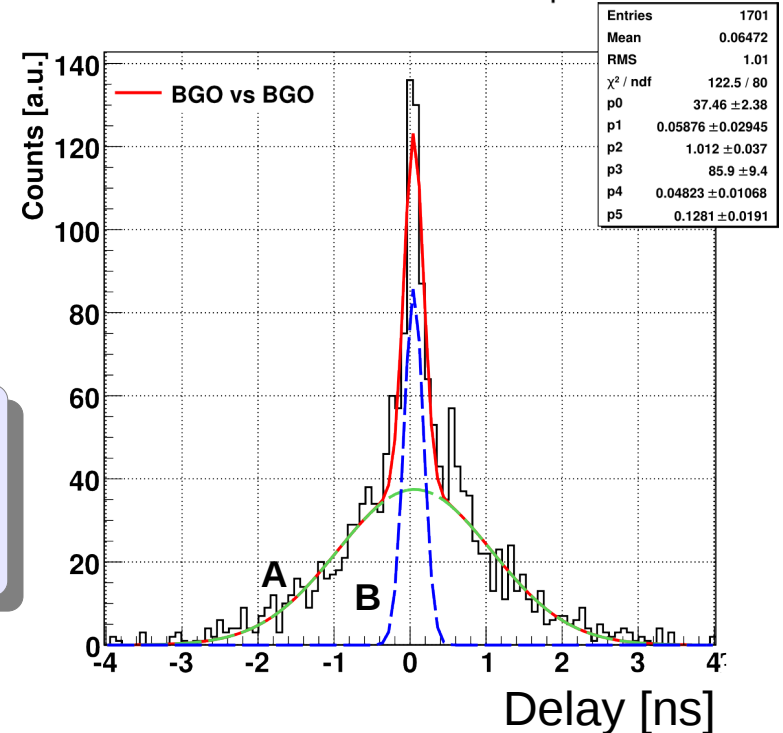
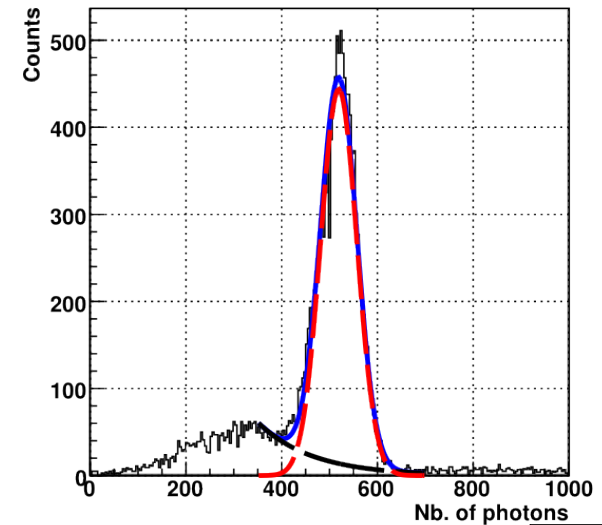
- Two BGO crystals $3 \times 3 \times 8 \text{mm}^3$ in coincidence
- Philips DPC3200
- Surfaces polished, wrapped in Teflon,
- Trigger on first arriving photon
- Two components visible:

Component A (76%): CTR = 2.38ns FWHM

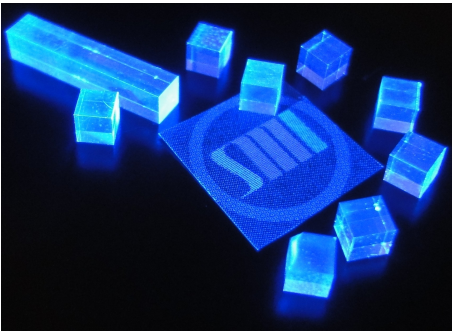
Component B (24%): **CTR = 301ps FWHM**

- Best ever measured CTR with BGO
(according to *Moses, NIM A 580 (2007) p.919*)
- LSO:Ce with the same size: 240ps FWHM

Cherenkov emission improves the CTR also in scintillators. The **DPC** is the **optimum detector** for Cherenkov photon detection in hybrid materials, because it allows to trigger on the first arriving photon.



The Cherenkov effect for gamma detection: potential and outlook

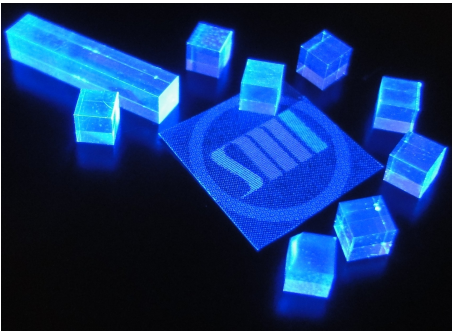


- **Cherenkov photons** were **detected** for γ -photons with 511keV in Cherenkov radiators and hybrid scintillators using digital SiPM
- The **time resolution** could be **improved** when compared with a fast scintillator (LSO:Ce)
- **Detecting Cherenkov photons in hybrid** scintillators could solve problem of energy determination while improving the TR
- **Challenge:** Cherenkov photon yield is very low

Outlook

- Detection of Cherenkov radiation with two (pure) Cherenkov radiators in **coincidence** (first tests are promising)
- Investigations of **new materials** for increasing the Cherenkov photon yield

The Cherenkov effect for gamma detection: potential and outlook



- **Cherenkov photons** were **detected** for γ -photons with 511keV in Cherenkov radiators and hybrid scintillators using digital SiPM
- The **time resolution** could be **improved** when compared with a fast scintillator (LSO:Ce)
- **Detecting Cherenkov photons in hybrid** scintillators could solve problem of energy determination while improving the TR
- **Challenge:** Cherenkov photon yield is very low

Outlook

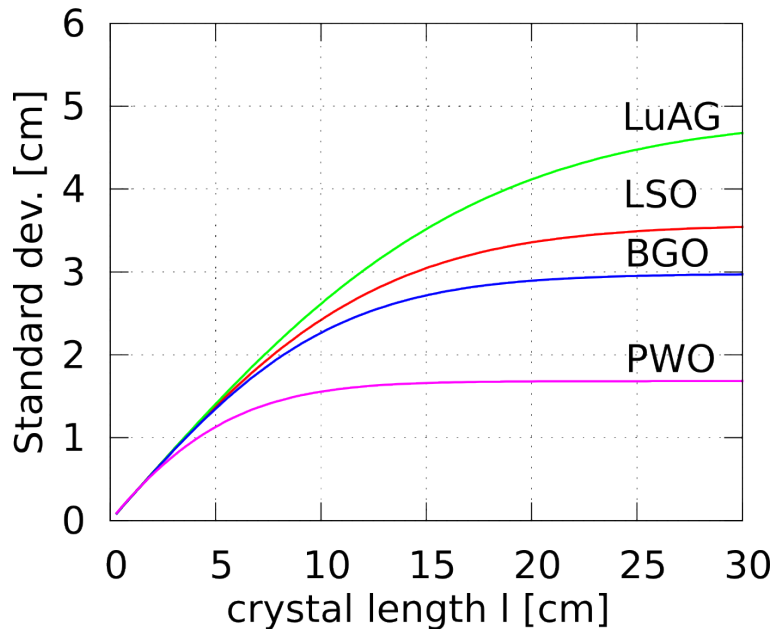
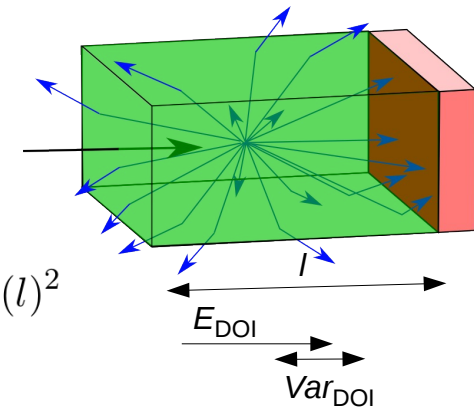
- Detection of Cherenkov radiation with two (pure) Cherenkov radiators in **coincidence** (first tests are promising)
- Investigations of **new materials** for increasing the Cherenkov photon yield

Thank you!

Influence of the DOI

- Analytical approach
- Calculating expectation value of γ -interaction inside a scintillator with a length l

$$E_{\text{DOI}} = \frac{N(l)}{\mu} \left(1 - e^{-\mu l} (1 + \mu l) \right) \quad \text{Var}_{\text{DOI}} = \frac{1}{\mu} \left(2E(l) - l^2 e^{-\mu l} \right) - E(l)^2$$



$\sigma(t=xn/c)$

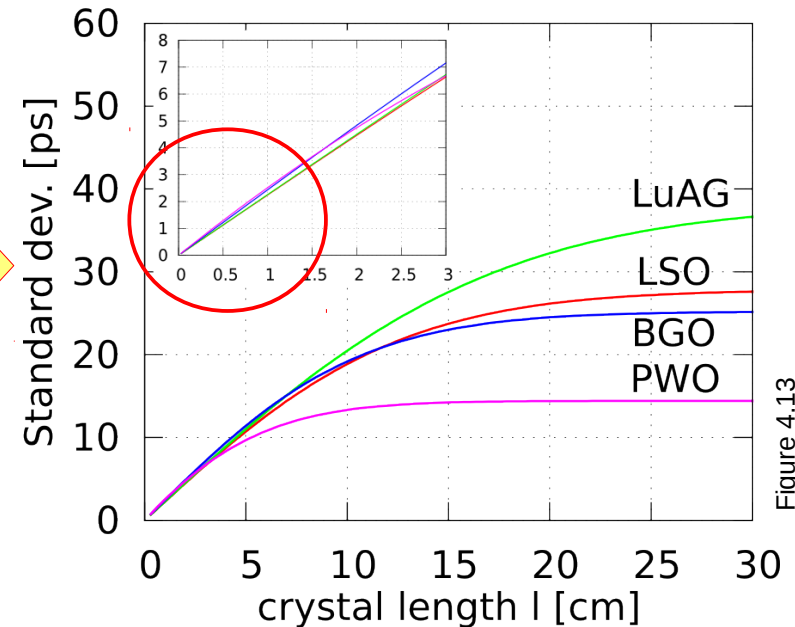
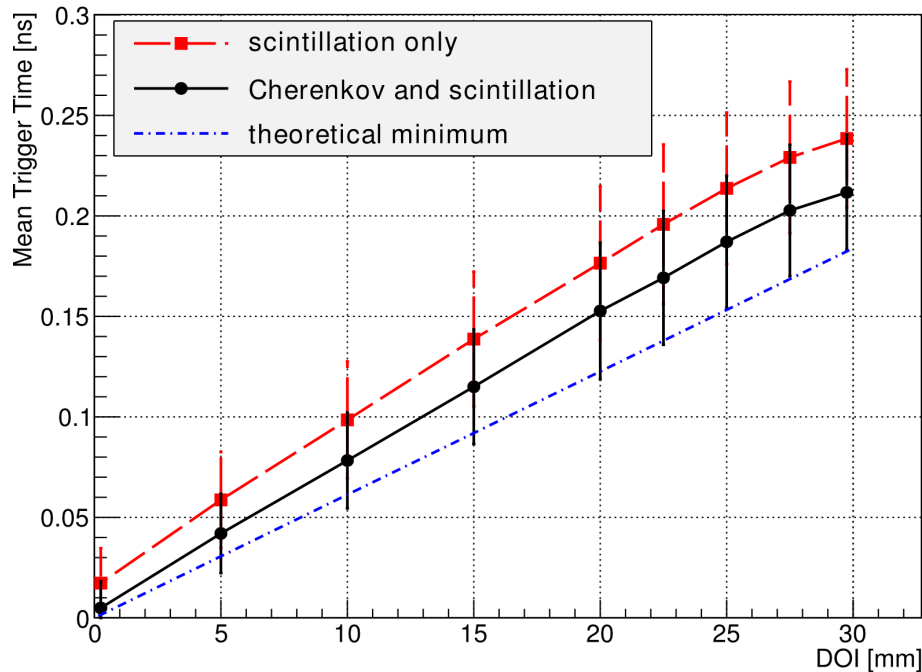
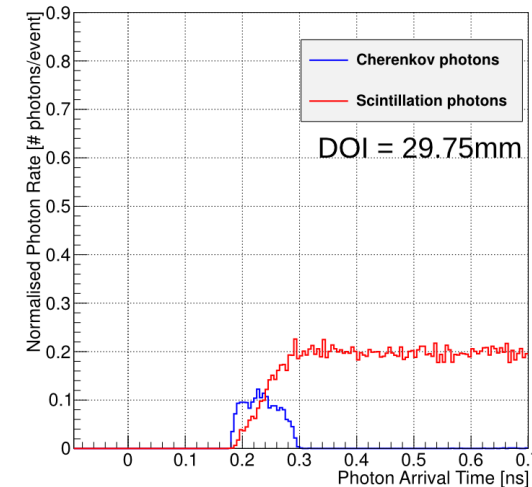
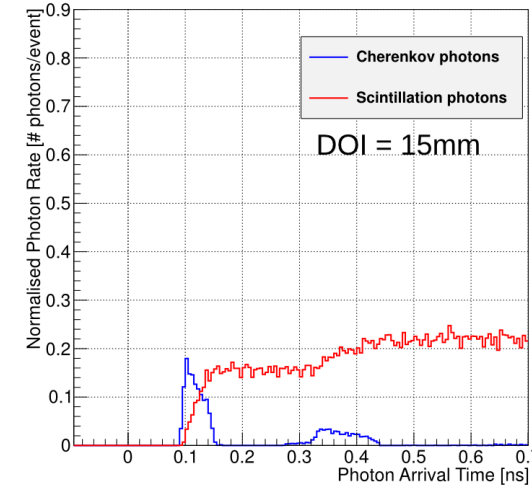
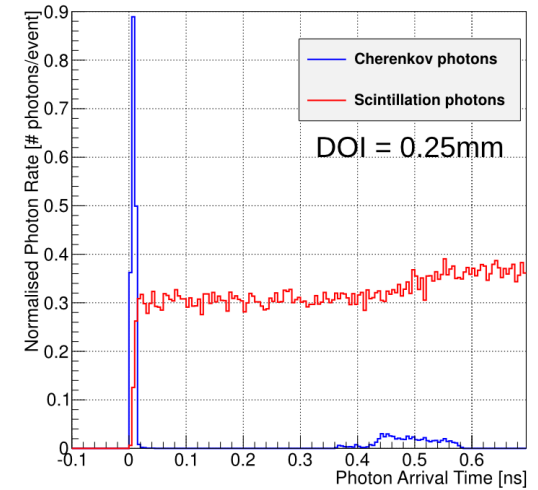
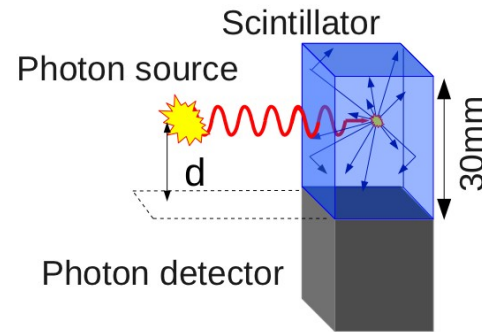


Figure 4.13

Photon detection times

- Simulating photon arrival times at photo detector for LSO:Ce (3x3x30mm³)
- Shoot γ -source from the side
- Varying distance of γ -source relative to photo detector



S. E. Brunner et al. NIM A 732 (2013) p. 560

S. E. Brunner

S. E. Brunner et al. NIM A 732 (2013) p. 560

Time resolution of the digital SiPM: simulation

- MC simulation using ROOT
- Structure based on the Philips DPC
- Two arrays representing the SPADs of two pixels/dies
- Laserpulse is triggering cells
- The arrays give back the time of the first trigger and the number of triggers per array
 - **time resolution**

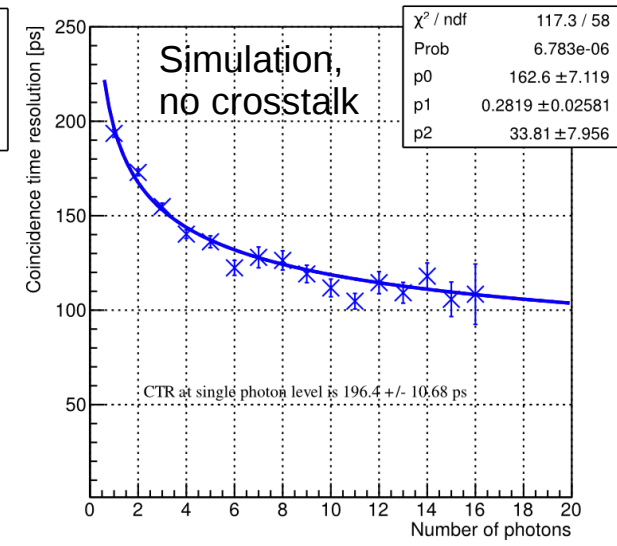
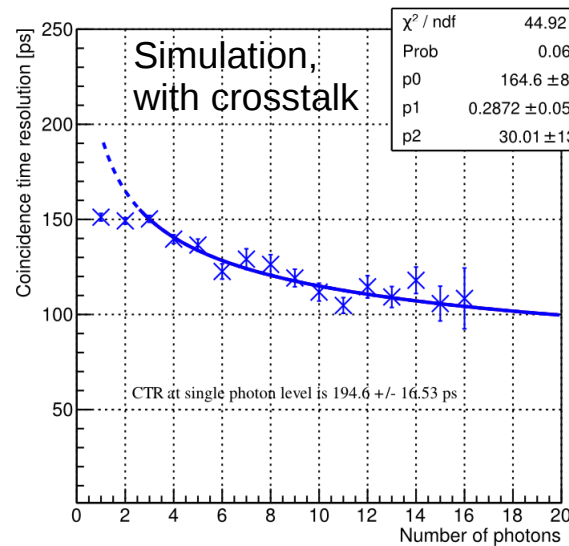
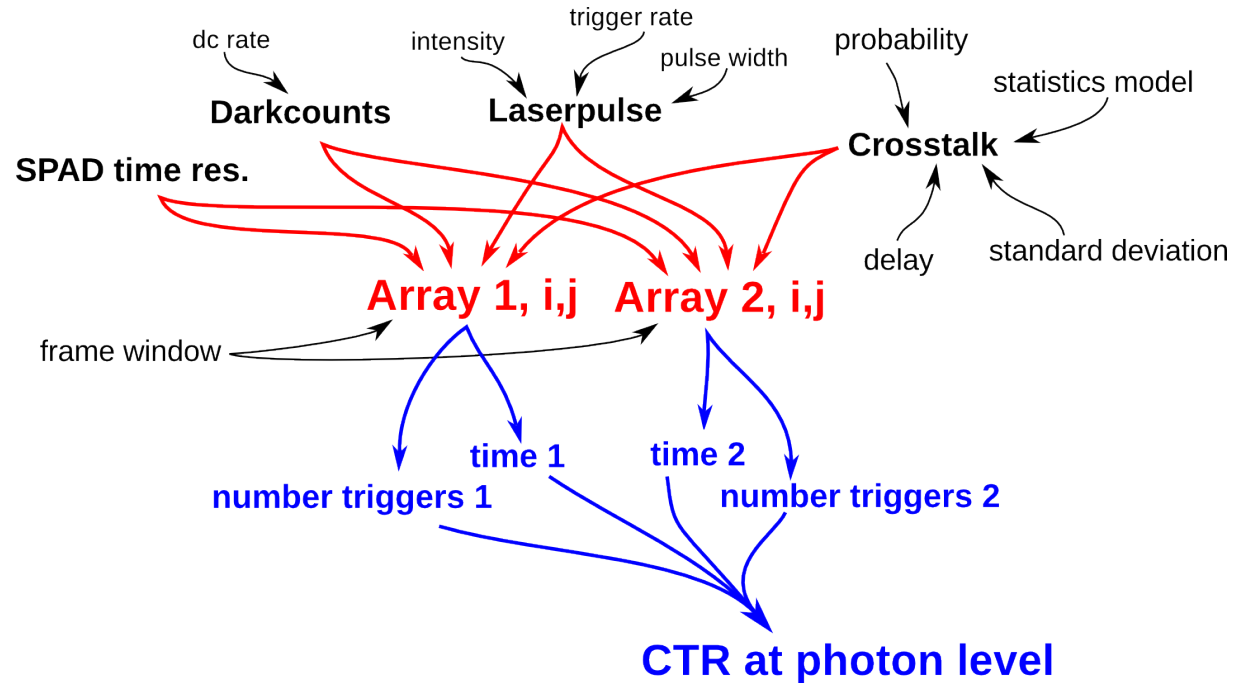
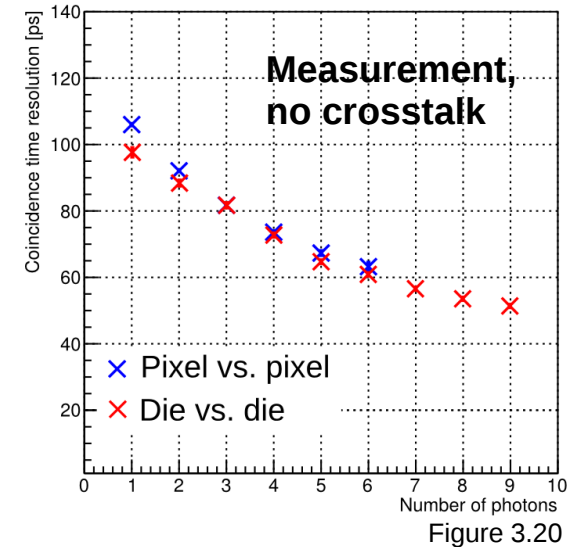
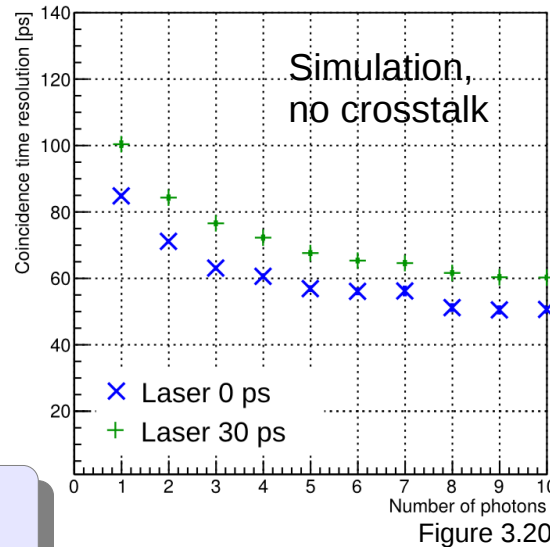
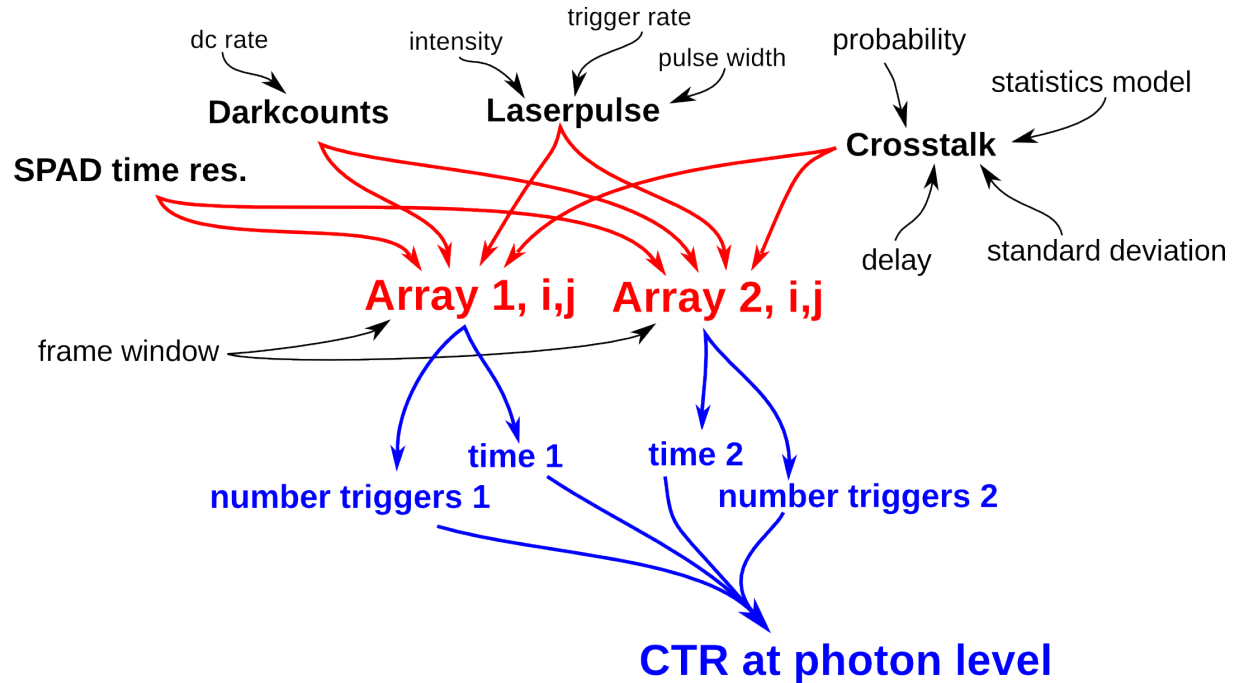


Figure 3.21

Time resolution of the digital SiPM: simulation

- MC simulation using ROOT
- Structure based on the Philips DPC
- Two arrays representing the SPADs of two pixels/dies
- Laserpulse is triggering cells
- The arrays give back the time of the first trigger and the number of triggers per array
 - **time resolution**



Setup was adjusted according to outcomes of the simulation. Artefacts at low photon levels vanished.

Time resolution of the digital SiPM: simulation

- Correlated triggers cause artefact → opt. cross talk
- Experimental validation:

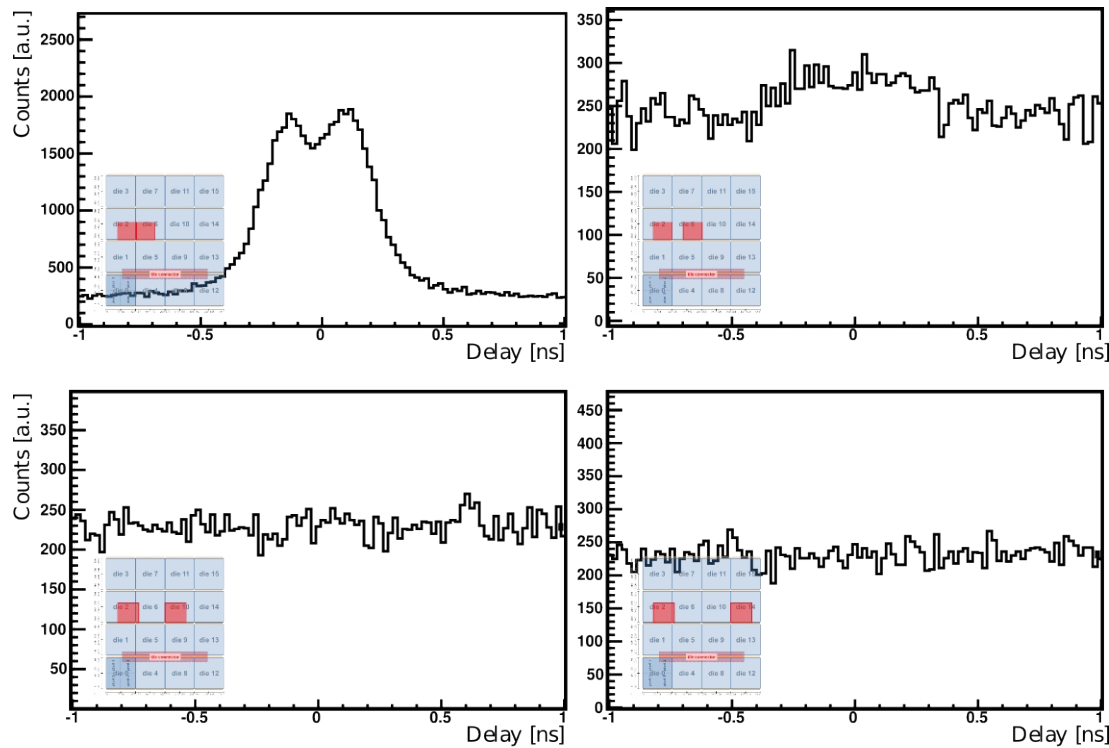


Figure 3.19

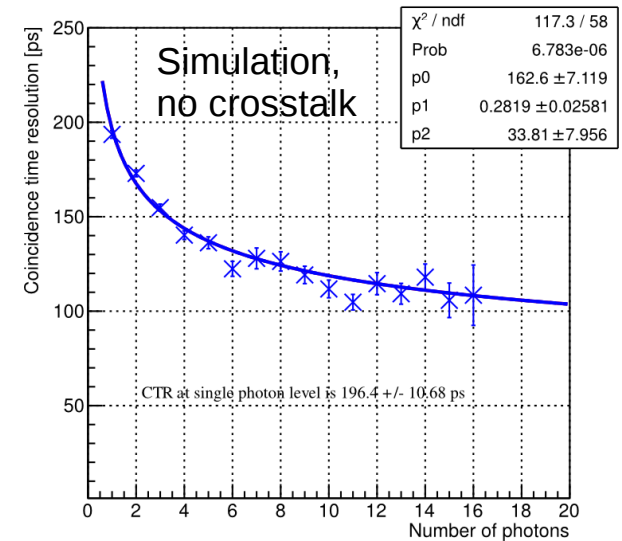
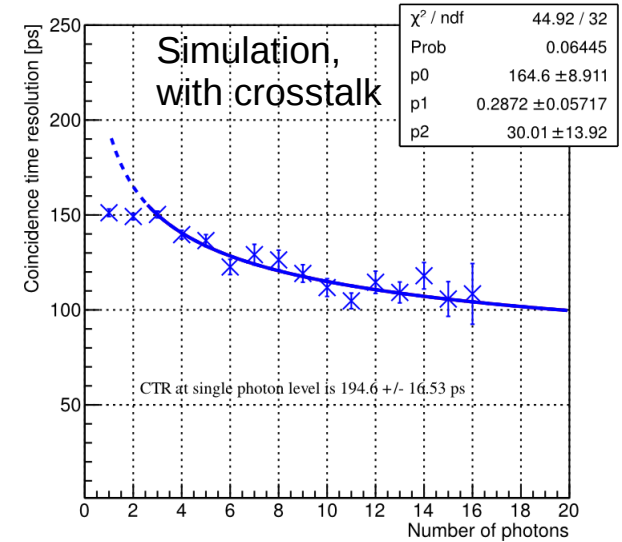
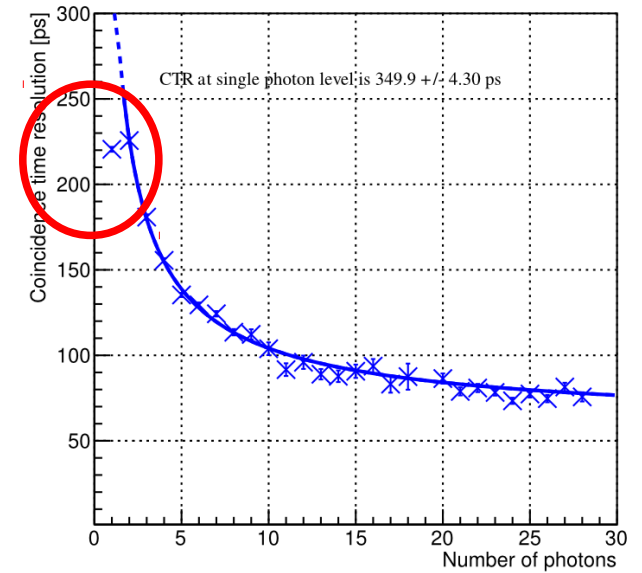
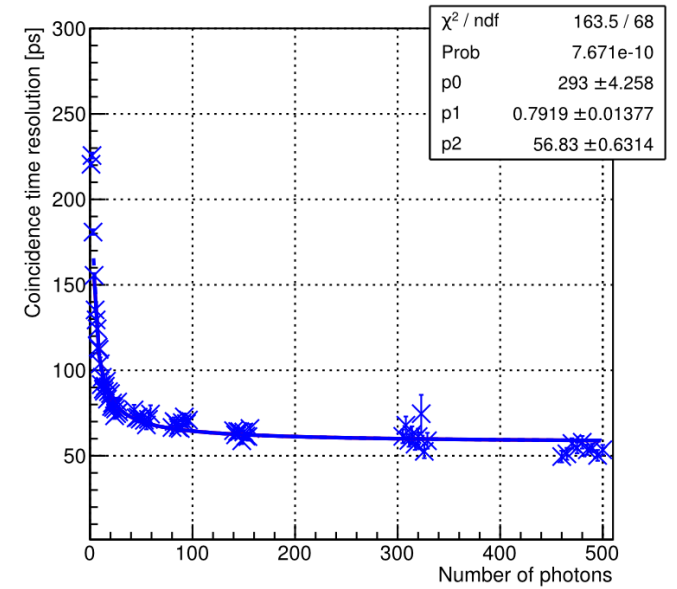
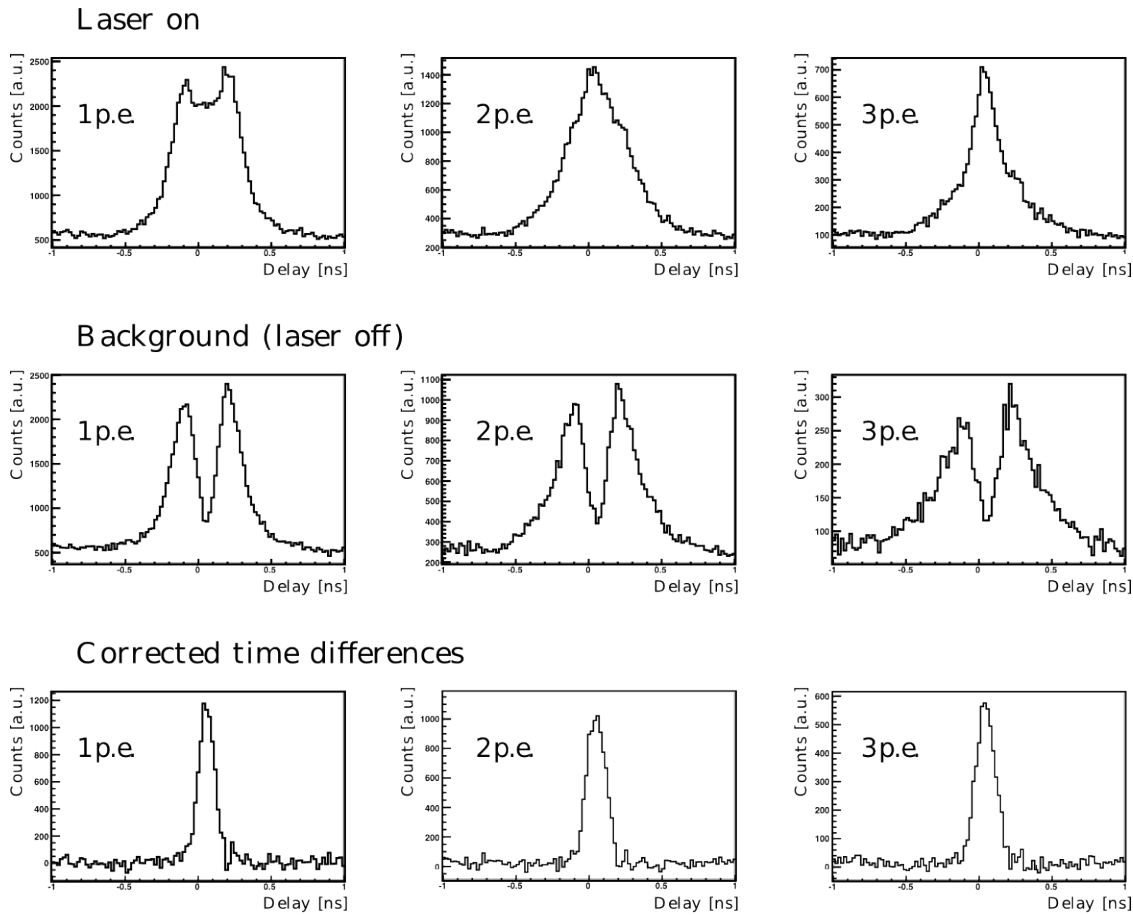


Figure 3.21

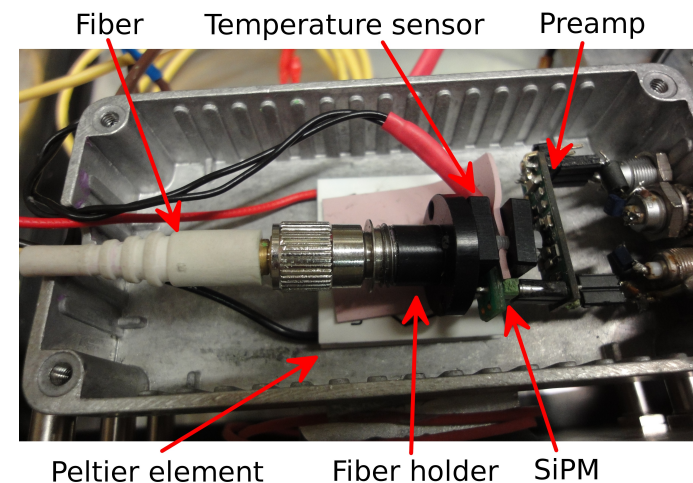
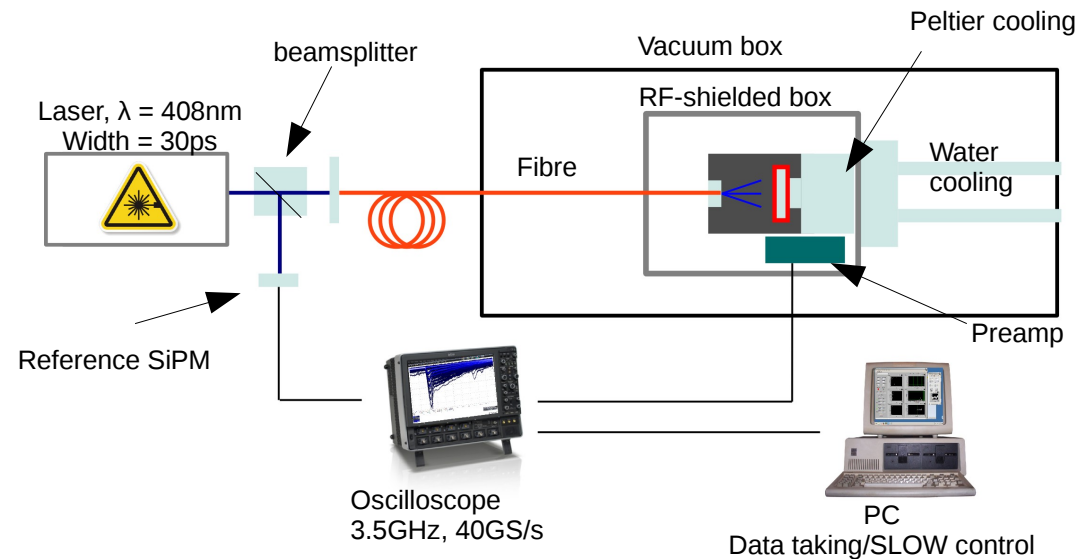
Time resolution of the digital SiPM: Results



Ref.: figure 3.14 & 3.15

Single photon time resolution of SiPM

- Figure of merit: single photon time resolution
- Semi-automatic test stand
- PC (LabView) controls: bias, cooling, oscilloscope
- PC records: bias, current, temperature, signal (amplitude, area, risetime), time difference to trigger
- Offline data analysis, including automatic determination of the breakdown voltage



→ time resolution as function of number of photons, bias, temperature

Single photon time resolution of SiPM

Manufact.	AdvanSiD	Hamamatsu	Ketek	Ketek	Ketek
Type	SiPM3S P-50	S10931- 100P	PM3375- B72	PM3360- A2*	PM3350- B63
Size [mm ²]	3x3	3x3	3x3	3x3	3x3
SPAD size [μm]	50	100	75	60	50
Breakdown v. [V]	~35	~70	~23	~23	~23
DC-rate [MHz]	<45	<12	<4.5	<4.5	<4.5
Gain [x10 ⁶]	2.5	2.4	14	9	6
PDE [%]	22	70	62	39	50
Cell cap. [fF]	-	2800	650	380	270
SPTR** [ps]	200	200	160	200	140

*prototype
** best value

Best time resolution by sensors with the smallest cell capacitance (Ketek).
Large contribution of the system to the time resolution!

