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Multiple Scattering and Accidental Coincidences in the J-PET Detector Simulated Using GATE Package

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Novel positron emission tomography system, based on plastic scintillators, is developed by the J-PET collaboration. In order to optimize geometrical configuration of built device, advanced computer simulations are performed. Detailed study is presented of background given by accidental coincidences and multiple scattering of gamma quanta.

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1. Introduction

The GEANT4 application for tomographic emission [1] (GATE) represents one of the most advanced specialized software packages for simulations of PET scanners. Despite the complexity of the simulated system, GATE is easily configurable and facilitates convenient use of the powerful GEANT4 simulation toolkit.

Thanks to the fact that the software was widely verified, it may be used for simulations of such a prototype devices as Strip-PET scanner [2–4], build by the J-PET collaboration. The scanner is based on the plastic scintillators representing innovative approach in the field of PET tomography. Another important feature of the scanner is large axial field-of-view (AFOV). PET scanners with large AFOV are also developed by other collaborations [5–14].

2. Setting parameters of the simulations in the GATE software

Properties of the scintillating material and the detecting surface, were set using three GATE-specific files: GateMaterials.db, Materials.xml, and Surfaces.xml. Some of them, could be fixed using data from documentation prepared by the producers of the equipment. For example the properties of the scintillating material EJ230 [15] that is used by the collaboration in real-life experiments are

- scintillation yield 9700 1/MeV,
- refraction index -1.58,
- density 1.023 g/cm^3 ,
- emission spectrum Fig. 1; maximum of emission at 391 nm.

The only property of the detecting surface (which immitates the photomultiplier Hamamatsu R4998 [16]) that has to be set by the user is the dependence of quantum efficiency on the wavelength of optical photons [17] (Fig. 1).



Fig. 1. Emission spectrum of the EJ230 material [15] and quantum efficiency of the R4998 photomultiplier [17].

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Some important properties, however, are not given by the producer. One of them is the absorption length dependence on the light wavelength. Therefore, we adopted and tested this dependence from another similar material as described below.

2.1. Simulations of the single strip

The dependence of absorption length on light wavelength for plastic scintillator may be found in Ref. [18]. Similar borrowing has been applied by the authors simulating the NEMO detector [19]. The dependence taken from publication was read out from the picture, smoothed using line interpolation and implemented in GATE software. After that some simulations of the single strip were performed and their results were compared with the experiment.

In the experiment, the collimated source of gamma quanta (Na-22) was moved along the scintillator EJ230 (5 mm \times 19 mm \times 30 cm) with step 3 mm and the beam was directed perpendicularly into the scintillator. For each position of the beam, 1-dimensional histogram of the number of photoelectrons was created. The histogram was put into the single column of two-dimensional histogram presented in the background of Fig. 2b. In this figure, one can see the dependence between the number of photons detected by the photomultiplier and the position of the beam of gamma quanta. Experimental data are available for positions between -14.7 cm and 14.7 cm and the width of bins is 3 mm. In this figure results for R4998 photomultiplier attached to the scintillator at the end (position 15 cm) are shown.



Fig. 2. The left part of the figure presents the dependence of the absorption length on the light wavelength. Upper line shows result obtained for pure polystyrene (PST) [18] and the lower line is scaled by factor of 0.55. The right part of the figure shows the spectra of number of photoelectrons as a position of the beam of gamma quanta. Dashed line indicates maximum number of photoelectrons produced by 511 keV gamma quanta as a function of position of irradiation assuming absorption as measured for PST (dashed line) and PST absorption scaled by factor of 0.55 (solid line).

Figure 3 shows comparison of simulated and experimental distributions of number of photoelectrons for three exemplary positions. A good agreement was obtained when scaling the absorption length of pure polystyrene [18] by factor of 0.55 (Fig. 2). The scaling factor accounts effectively for the absorption due to the primary and secondary admixture in the scintillator material, imperfections of surfaces and reflectivity of the foil.



Fig. 3. Comparison of the simulated and experimental histograms of energy deposited by 511 keV gamma quanta (in number of photoelectrons) for the beam positions -12 cm (left), 0 cm (middle), 12 cm (right); experimental spectrum is suppressed at low values due to the triggering conditions [2].

Dashed and solid line in right part of Fig. 2 presents results of simulations performed for energy loss of 341 keV corresponding to the maximum energy of the electron scattered by the 511 keV gamma quantum via Compton effect. Dashed line was obtained assuming the absorption length as determined for the pure PST, whereas solid line shows result after scaling the absorption by a factor of 0.55. The scaling factor was optimised to the experimental results.

3. Simulations of the single layer J-PET scanner

A diagnostic chamber of the J-PET detector will form a cylinder which will be constructed from the plastic scintillator strips [20–22]. In this article we present simulations for the detector with the inner radius of R = 427.8 mm (radius similar to commercially available PET systems [23, 24]). We assume that the detector possesses one layer built out of 384 EJ230 scintillator strips with dimensions of 7 mm × 19 mm × L (L = 20, 50,100, or 200 cm). Geometry of the simulated scanner is visualised in Fig. 4.



Fig. 4. Visualisation of the geometry of the single-layer J-PET scanner with radius of the cylinder R and the length of the scintillators L.

3.1. Scattered coincidences

In order to estimate secondary scattering of gamma quanta in the detector material, we have simulated annihilations homogeneously in the 2 m long line placed along the central axis of the scanner. In the following, we consider few most probable responses of the detector system (see Fig. 5). In the most probable case both gamma quanta will escape detection and no signal will be observed ($N_{\rm strips} = 0$). The second frequent category corresponds to events when only one strip was hit ($N_{\rm strips} \geq 2$ we can distinguish different cases for the same value of $N_{\rm strips}$. Therefore for the univocal description we introduce one more parameter μ . Various possibilities which may occur are listed below and depicted in Fig. 5:

- $N_{\text{strips}} = 3$, $\mu = -3$ 3 quanta in 3 different strips with two secondary scatterings,
- $N_{\text{strips}} = 2, \ \mu = -2$ 2 quanta in 2 different strips with one secondary scattering,
- $N_{\text{strips}} = 0, \ \mu = 0$ no gamma quanta registered,
- $N_{\text{strips}} = 1, \ \mu = 1$ interaction in only one strip,
- $N_{\text{strips}} = 2, \ \mu = 2$ 2 interactions in 2 different strips,
- N_{strips} = 3, μ = 3
 3 scatterings in 3 different strips; 2 primary and 1 secondary scattering.

It is also possible that there are 4, 5 or even more scatterings, depending on the energy threshold applied to each hit.



Fig. 5. Pictorial definitions of the value of multiplicity μ used further in the following figures.

Histograms of the multiplicity for three different energy thresholds (0, 100, and 200 keV) and for four different lengths of scintillators (20, 50, 100, and 200 cm) are presented in Fig. 6. Results of the simulations show

that if energy threshold is set to 200 keV, there are no events where number of hits is bigger than 2. Most of scattered coincidences (with multiplicity -2) is also eliminated with this energy threshold. If the energy threshold is set to 100 keV, for lengths of scintillators 100 cm and 200 cm, there would be even events with four scatterings, which may negatively influence the quality of reconstructed images.



Fig. 6. Histogram of the multiplicity μ for different lengths L of the diagnostic chamber. Meanings of different values of the multiplicity μ are described in the text and defined in Fig. 5.

For $N_{\text{strips}} = 2$ and $N_{\text{strips}} = 3$ and length of scintillators equal to L = 50 cm, histograms of time differences between subsequent hits were calculated. These histograms are presented in Figs. 7-9. Right part of these figures shows distribution of difference between ID of hit modules (Δ ID) as a function of hit time difference[†]. The module ID increases monotonically with the growth of the azimuthal angle φ (see Fig. 4). Black lines in the two-dimensional histograms (Figs. 7–10) show the boundaries between events treated as useful coincidences and events treated as background coincidences due to the secondary scatterings. A positive value of μ (2 or 3) is assigned to events above the line, which are treated in further analysis as true coincidences. Whereas to events below the line a negative value of μ (-3 or -2) is assigned, these events include secondary scattering of gamma quanta. This boundary was used to separate events with different multiplicities for preparation of histograms presented in Fig. 6.

In Fig. 7, for energy thresholds 0 keV and 100 keV, in two-dimensional histograms there is longitudinal structure extending between points (0 ns, 0) and (3 ns, 192). These events correspond to difference between time of primary reaction of the gamma quantum in a given scintillator and a time of the secondary scattering. The larger is the angle of the primary scattered gamma quantum the

[†]If IDs of hit modules are ID₁ and ID₂ then Δ ID = min(|ID₁ - ID₂|, 384 - |ID₁ - ID₂|).

larger will be the Δ ID value and also a Δt . For example bin with coordinates (2.9 ns, 192) corresponds to the backscattering — primary particle is backscattered and it is registered in the strip on the opposite side of the scintillator (2.9 ns is the time needed by the gamma quanta to travel between opposite strips with speed of light).



Fig. 7. Distributions of differences of hit times; $N_{\rm strips} = 2$, $\mu = -2$ or $\mu = 2$; black line in the twodimensional histogram shows the boundary between events treated as originating from primary interactions only (above the line) and events including secondary interactions (below the line). Figure presents results of simulations for L = 50 cm. The time differences are calculated only for interactions originating from the same annihilation process.

If the energy threshold is set to 200 keV, nearly all scattered coincidences are eliminated. In the lower part of this figure there are results for this threshold. In ideal situation, time difference for this simulation for true coincidences would be always 0 and we would have only one bin for 0 ns. Because of the fact that gamma quanta interact with matter in different depths (depth of interaction), time difference is changing from 0 to about 80 ps. This picture shows what is the time limit for time-of-flight determination with scintillator strips of 19 mm thickness.

In Fig. 8, for energy thresholds 0 keV and 100 keV, in two-dimensional histograms there is symmetrical butterfly-shape structure extending between points (0 ns, 0) and (3 ns, 192) and between points (3 ns, 0) and (0 ns, 192). Each event with three hits and deposited energy above the energy threshold, gives two inputs to these histograms. An additional structure (for $N_{\text{strips}} = 3$) which is spanned between points (3 ns, 0) and (0 ns, 192) originates from the time differences between the primary interaction of one of the gamma quantum and a secondary interaction of the other or from the time difference between two secondary interactions. Pictorial definitions of these situations are presented in Fig. 5. If only the first time difference is taken into account, histograms for 3 hits (Fig. 9) look like histograms for 2 hits (Fig. 7).



Fig. 8. Distributions of differences of hit times; $N_{\rm strips} = 3$, $\mu = -3$ or $\mu = 3$, both time differences are taken into account. Figure presents results of simulations for L = 50 cm. The time differences are calculated only for interactions originating from the same annihilation process. Figure is described with details in the text.



Fig. 9. Distributions of differences of hit times; $N_{\rm strips} = 3$, $\mu = -3$ or $\mu = 3$, only first time difference is taken into account. Figure presents results of simulations for L = 50 cm. The time differences are calculated only for interactions originating from the same annihilation process. Figure is described with details in the text.

Response of the detector to the annihilations in the 2 m long line placed along the detector axis was simulated also for other lengths of scintillators L = 20, 100, and 200 cm. Results of these simulations for two energy thresholds (0 keV and 200 keV) are presented in Fig. 10. One can see that the longer the scintillators, the wider the longitudinal structure described above. It is caused by the fact that the longer the scintillators, the longer the possible distance between places of the primary and secondary interactions. For the scanner with 20 cm scintillators, the longest possible path along the

diagonal of the longitudinal cross-section of the scanner has length of 88 cm (~ 2.9 ns) and for the scanner with 200 cm scintillators, the longest possible path is equal to 218 cm (7.3 ns).



Fig. 10. Distributions of differences of hit times (Δt) as a function of ID difference between hit modules (ΔID) . The length L of the detector is 20 cm (1st row), 50 cm (2nd row), 100 cm (3rd row), 200 cm (4th row). Right part of the figure shows results for energy threshold of $E_{\rm th} = 200$ keV whereas results in the left figure were obtained for $E_{\rm th} = 0$. Only interactions originating from the same annihilation process are taken into account.

3.2. Accidental coincidences

An accidental coincidence is the coincidence, in which two events occur simultaneously in a fixed time window but in fact they are independent, they come from different annihilations. Because of that, number of accidental coincidences depends on the width of the time window, the size of the detector and in contrast to the secondary scattering, the accidental coincidences depend on the activity of the source.

3.2.1. Accidental coincidences as a function of the source activity

Simulations described in this section were performed for other activities of the source: 5, 10, 20, 30, 50, 100, 150, 200, 250, 300, 350, and 400 MBq. For each of these activities 10^8 annihilations were simulated. Results of simulations for the smallest (5 MBq) and the largest (400 MBq) activity are presented in Figs. 11 and 12.

In Fig. 11 histograms contain all time differences both for hits from the same event and for hits from different events (there is no time window). One can see that the first bin is higher than expected from the general exponential dependence. This is because this bin contains both true and accidental coincidences. The structure is better visible in Fig. 12. In the upper part of this figure, histograms contain time differences between hits from the same and from different annihilations. If time differences from the same annihilations were omitted, there would be only accidental coincidences, as it is presented in the bottom part of the figure.



Fig. 11. Histograms of numbers of all differences of hit times for length of scintillators equal to 50 cm, activities of 5 MBq (left) and 400 MBq (right) and for two different energy thresholds as indicated in the legends.



Fig. 12. Distributions of time differences between hits in the detector originating from the same and from different annihilations (top part) and from the different annihilations only (bottom part). Shown are results of simulations for activities of 5 MBq (left) and 400 MBq (right) and for two different energy thresholds as indicated in the figures.

3.2.2. Accidental coincidences for time windows 3 ns and 5 ns $\,$

For simulations described in this article with the virtual linear source of annihilations placed along the main axis of the scanner, true coincidences are defined as two hits from the same annihilation having Δ ID vs. Δt above the black lines shown in Figs. 7–10. Figure 13 presents rate of such defined true coincidences as a function of annihilation source activity, time window, energy threshold, and detector length L.



Fig. 13. Simulated rate of true coincidences as a function of time window, activity and detector length. The sequence of curves in the figure is the same as in the legend (from top to bottom); bottom pictures present the same data as the top ones but in logarithmic scale. Results for the time window of 3 ns (solid lines) are indistinguishable from the results for time window of 5 ns (dashed lines); $N_{\rm strips} = 2$, $\mu = 2$. Right part of the figure shows results for energy threshold of $E_{\rm th} = 200$ keV whereas results in left figure were obtained for $E_{\rm th} = 0$.

Accidental coincidences for time windows 3 ns and 5 ns and for four lengths of the scintillators are presented in Fig. 14. One can see that if the energy threshold is 200 keV (right column of the figure), a rate of accidental coincidences is reduced by the factor of about 7 in comparison to situation when there is no energy threshold (left column of the figure).



Fig. 14. Accidental coincidences for time windows 3 ns (solid lines) and 5 ns (dashed lines) for different lengths of the scintillators (as indicated in the legend); the sequence of curves in the figure is the same as in the legend (from top to bottom); bottom pictures present the same data as the top ones but in logarithmic scale; $\Delta ID_{th} = 0$, $N_{strips} = 2$. Right part of the figure shows results for energy threshold of $E_{th} = 200$ keV whereas results in left figure were obtained for $E_{th} = 0$.

Figure 15 shows rate of accidental coincidences under condition that difference Δ ID is larger than 96, which means that interactions of gamma quanta occur in two different quarters of the cylinder (consisting of 384 scintillator strips). Such condition decreases the field of view of the detector to the cylinder with radius of 30 cm, however this additional condition reduces the number of accidental coincidences by the factor of 2.



Fig. 15. Accidental coincidences for time windows 3 ns (solid lines) and 5 ns (dashed lines) for different lengths of the scintillators (as indicated in the legend); minimum difference between IDs of the strips is equal to $\Delta ID_{th} = 96$; $N_{strips} = 2$; the sequence of curves in the figure is the same as in the legend (from top to bottom); bottom pictures present the same data as the top ones but in logarithmic scale. Right part of the figure shows results for energy threshold of $E_{th} = 200$ keV whereas results in left figure were obtained for $E_{th} = 0$.



Fig. 16. Ratios between true and accidental coincidences for time window 3 ns and minimum difference between IDs of the hit scintillator strips ΔID_{th} is equal to 96; $N_{strips} = 2$. Right part of the figure shows results for energy threshold of $E_{th} = 200$ keV whereas results in the left figure were obtained for $E_{th} = 0$.

In Fig. 16 rates of true and accidental coincidences are presented. The ratio is larger for longer scintillators. It is caused by the fact that for short scintillators there are additional accidental coincidences caused by the gamma quanta from outside of the tomograph.

4. Summary

Physical properties of the scintillating material and the photomultiplier used in the J-PET detector were implemented in the GATE software. The simulations procedures were validated by the comparison of simulated and experimental results for the number of photoelectron spectra. In previous research, studies of simplified Strip-PET scanner were presented [25]. Map of efficiency of 2strip scanner was calculated and compared with the geometrical efficiency of such a device. In present studies, background given by accidental coincidences and multiple scattering of gamma quanta was investigated for single-layer 384-strip J-PET scanner.

In presented simulations, the source of annihilations was assumed to be a 2 m long line placed along the main axis of the scanner. In order to compare precisely obtained results with results for another devices, in the future the source will be simulated in accordance with NEMA-NU-2 standard [26]. Even so, it is possible to compare orders of magnitudes of calculated parameters. For example, results obtained for 2 m long J-PET scanner for activity of 200 MBq are similar to these simulated for the same length RPC-PET [27–29].

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