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Master Thesis

Feasibility study of η-mesic nuclei production by means of the WASA-at-COSY and COSY-TOF facilities

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Abstract

Feasibility study of η -mesic nuclei production by means of WASA-at-COSY and COSY-TOF facilities

Despite the fact that existence of η -mesic nuclei in which the η meson might be bound with the light nucleus by means of the strong interaction was postulated already in 1986, it is still not experimentally confirmed. Discovering of this new kind of an exotic nuclear matter is very important as it might allow for better understanding of η meson structure and its interaction with nucleons.

The search of the η -helium bound states is carried out at the COSY accelerator in the Research Center Jülich in Germany, by means of the WASA detection system. The search are conducted with high statistic and high acceptance for the free production of the ⁴He- η bound states. It is also considered to search for η -tritium in quasi free reaction which might be realised with COSY-TOF facility.

In this thesis the results of the Monte Carlo simulations of the η -helium bound states and η -tritium bound state are presented and discussed. The acceptances of the WASA-at-COSY and COSY-TOF detectors for the free and quasi-free η -mesic nuclei production reactions were determined, respectively. Furthermore acceptances were compared for three different models of nucleon momentum distribution inside atomic nuclei and three different values of width of a considered bound states. In case of COSY-TOF detector it was established that the most effcient measurement of quasi-free $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ reaction can be done at beam momentum of $p_{beam}=3.1 \text{GeV/c}$.

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1 Introduction

The new kind of nuclear matter consisting of nucleus bound with η mesons via strong interaction was postulated by Haider and Liu over twenty years ago [1]. However, till now none of experiments confirmed empirically its existence. This exotic form of matter called η -mesic nucleus is schematically presented in Fig. 1.1.

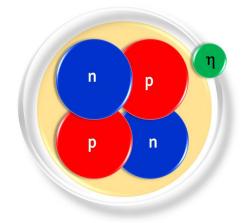


Figure 1.1: The scheme of η -mesic bound state.

Up to this time η -mesic nuclei have been searched via production of η meson in the vicinity of the heavy nuclei. It was considered that due to a huge number of nucleons, attraction of η meson could be high enough that allows to form a bound state. Nevertheless those experiments have not brought expected effect. Recent investigations indicate that interaction between η meson and nucleus is considerably stronger than it was predicted earlier. Therefore, according to the current theoretical considerations, it is possible that the bound states might be also formed for a light nuclei like helium, tritium [2, 3] and even deuteron [4].

The existence of η -mesic nuclei allows to investigate interaction of the η meson and the nucleons inside a nuclear matter. Moreover it would provide information about N*(1535) resonance [5] and about η meson properties in nuclear matter [6], as well as about contribution of the flavour singlet component of the quark-gluon wave function of η meson [7, 8].

The measurement of the ⁴He- η bound states is carried out with a unique accurance by means of WASA detector [9] installed at cooler synchrotron COSY in the Research Center Jülich. The η -mesic nuclei is searched there via studying of excitation function for the chosen decay channels of the ⁴He- η system formed in deuteron-deuteron collision [10]. The measurement is performed for the beam momentum varying continously around the threshold. The beam ramping technique allows to reduce the systematical uncertainities. The existence of the bound system should manifest itself as a resonancelike structure in the excitation curve of eg. $dd \rightarrow ({}^{4}\text{He}-\eta)_{bs} \rightarrow {}^{3}\text{He}p\pi^{-}$ reaction below the $dd \rightarrow {}^{4}\text{He}-\eta$ reaction threshold which allows to determine the binding energy and the width of such state.

Formation of the η -mesic nucleus might be also realized by means of the quasi-free reactions. In this case the scan of the energy can be achieved from the Fermi motion of nucleons inside the deuteron beam. Measurements of such reaction is available for the external COSY-TOF detector [11, 12, 13] where the search of η -mesic Tritium can be carried out by the measurement of the excitation function of the $nd \to (T-\eta)_{bs} \to$ $dp\pi^-$ reaction around the threshold of the $nd \to T-\eta$ production [10].

The main aim of this thesis is a determination of geometrical acceptance of WASA detector for four reactions in which η -mesic bound states might be formed via free production:

and geometrical acceptance of COSY-TOF detector setup for one quasi-free reaction of η -mesic nuclei production:

$$dd \to p_{sp}(T-\eta)_{bs} \to p_{sp}dp\pi^-$$

In each case Monte Carlo simulations of η -mesic nucleus production and decay process were carried out based on reaction kinematics. The simulations were realized with assumption that the bound state has a resonance structure given by the Breit-Wigner distribution with fixed binding energy B_s and a width Γ . Moreover, for reconstruction of events the spectator model was applied. The efficiency of the registration of each reactions was analysed with regard to different models describing Fermi momentum distributions of nucleons inside deuteron, helium and tritium nuclei. It was also compared for different values of B_s and Γ from range predicted by theory [14].

This thesis is divided into seven chapters. The second describes indirect and direct experimental indications for the existence of the η -mesic helium.

The Chapter 3 treats of nucleon momentum distributions inside the light nuclei such as ³He, ⁴He and T. The distributions are presented and compared for different models.

Description of the spectator model assumptions and its experimental confirmations are presented in Chapter 4.

The Chapter 5 is devoted to the kinematics of the free and quasi-free reactions in which η -mesic bound states are produced and decay.

The WASA-at-COSY and COSY-TOF detection systems emphasising their properties useful for the measurement of the η -mesic nuclei are presented in Chapter 6.

Simulation results of the bound states in free and quasi-free reactions are described in Chapter 7 and in Chapter 8 a summary and conclusions are presented.

2 Indications for the existence of η -mesic helium

2.1 Indirect

According to the theoretical considerations, the formation of the η -mesic nucleus can only take place if the real part of the η -nucleus scattering length is negative (attractive nature of the interaction), and the magnitude of the real part is greater than the magnitude of the imaginary part [15]:

$$|Re(a_{\eta-nucleus})| > |Im(a_{\eta-nucleus})|.$$

$$(2.1)$$

A wide range of possible values of the η N scattering lenght $a_{\eta N}$ calculated for hadronicand photoproduction of the η meson has not excluded the formation of η -nucleus bound states for a light nuclei as ^{3,4}He, T [2, 3] and even for deuteron [4]. Those bound states have been searched in many experiments. However, none of them gave empirical confirmation of their existence. There are only a signal which might be interpreted as an indications of the η -mesic nuclei.

Experimental observations which might suggest the possibility of the existence of the ³He- η bound system were found by SPES-4 [16], SPES-2 [17], ANKE [18] and COSY-11 [19] collaborations. In the experiments cross section of the $dp \rightarrow {}^{3}\text{He-}\eta$ reaction was measured. In this reaction with the real η meson in the final state, the bound state could not be produced and therefore obtained results might be treated as indirect indications of the η -mesic nuclei only.

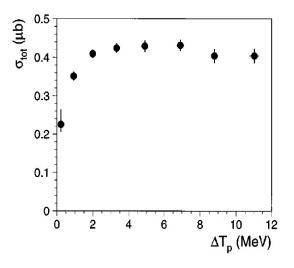


Figure 2.1: Total cross section for $pd \rightarrow {}^{3}\text{He-}\eta$ reaction measured for eight different proton energies above threshold from 0.2 to 11 MeV [17]. Total cross section rises from 0.25 to 0.40 µb rapidly in the range of 2 MeV.

The measurements on the SPES-4 spectrometer were realised using the deuteron beam accelerated in SATURNE synchrotron colliding with liquid-hydrogen target, while in case of SPES-2 the proton beam and liquid-deuterium target were used. The total cross section measured by the SPES-2 collaboration for the eight different beam energies are presented in Fig. 2.1. According to [2], the energy dependence of the cross section for the $dp \rightarrow {}^{3}\text{He}-\eta$ reaction is dominated by the strong interaction between η and ${}^{3}\text{He}$ originating from the strong η -nucleon interaction leading to the formation of the N*(1535) resonance. The data analysis of the close to threshold measurements of the total cross section led to the determination of the $\eta^{3}\text{He}$ scattering length. The negative sign of a real part of the $a_{\eta^{3}He}$ and its large value equal $a_{\eta^{3}He} = (-2.31 + 2.57i)$ fm [2] suggest a possible existence of the (${}^{3}\text{He}-\eta$)_{bs}, although the condition given by (2.1) is not fulfilled.

An indirect signature of the η -mesic nuclei were also searched at the cooler synchrotron COSY in Jülich by means of internal COSY-11 and COSY-ANKE detection setups with high precision and high statistics. In the experiments the momentum ramping technique of the deuteron beam was used that allows to reduce the systematic uncertainties. The beam was accelerated slowly and linearly in time, from excess energy of Q=-5.05 MeV up to Q=11.33 MeV in case of ANKE experiment [18], while during the COSY-11 experiment [19] the momentum was varied in the range corresponding to the excess energy from Q=-10 MeV to Q=9 MeV. Both collaborations performed the measurement of the excitation function and differential cross section of the $dp \rightarrow {}^{3}\text{He-}\eta$ reaction close to the kinematical threshold. The experimental excitation function parametrized with the s-wave formula of scattering length [18, 19] is presented in Fig. 2.2 (left panel). The fit to the COSY-11 data gave the value of the η^{3} He scattering length equal to $a_{\eta^3 He} = [\pm (2.9 \pm 0.6) + (3.2 \pm 0.4)i]$ fm [19]. Although this value is in agreement with formula (2.1), uncertainties of its real and imaginary part are too large to confirm the possible formation of $({}^{3}\text{He}-\eta)_{bs}$. The real part of scattering lenght of the $\eta^{3}\text{He}$ system derived by fitting the ANKE data for Q<4MeV equals $Re(a_{n^{3}He}) = (11.6 \pm 1.4)$ fm while imaginary part is equal $Im(a_{n^{3}He}) = (-4.1 \pm 7.0)$ fm [18]. Those large values implies the existence of a quasi-bound states very close to the reaction threshold, however the derived by ANKE and COSY-11 collaborations real parts of the scattering length are not consistent within the quoted errors.

The differential cross section measurement allows to calculate angular asymmetry parameter α , defined as:

$$\alpha = \frac{d}{d\cos\theta_{\eta}}\ln\frac{d\sigma}{d\Omega}.$$
(2.2)

The momentum dependence of parameter α can be described correctly with assumption that the phase is varying between S and P waves [21]. In another case the discrepancy between the experimental data and theoretical description are significant. The momentum dependence of α parameter is presented in Fig. 2.2 (right).

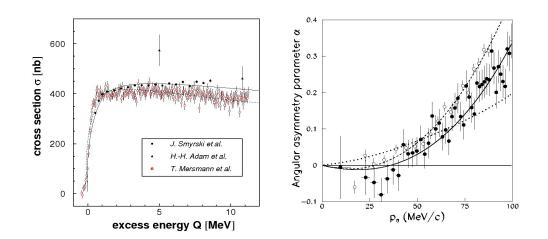


Figure 2.2: (left) Total cross section for the $dp \rightarrow {}^{3}\text{He-}\eta$ reaction measured with the COSY-ANKE (open circles) [18] and the COSY-11 facilities (closed circles) [19] and (triangles) [20]. Scattering length fit to the COSY-ANKE and COSY-11 data is represented with dashed and solid lines, respectively. (right) Angular asymmetry parameter α for the experimental data from COSY-ANKE (full dots) [18] and from COSY-11 (open circles) [19]. The dashed and solid lines are fitted (assuming the phase variation between S and P waves) to the COSY-11 and COSY-ANKE data, respectively [21]. The fit without the phase variation is denoted as the dotted line. The figure is adapted from [10].

2.2 Direct

The first direct experimental indications of a light η -nucleus bound states were observed in the reaction of the η photoproduction $\gamma^{3}\text{He} \rightarrow \pi^{0}pX$ which was investigated with the TAPS calorimeter at the electron accelerator facility Mainz Microtron (MAMI) [22]. Photons produced in a thin radiator foil and tagged using a special spectrometer hit the target filled with liquid ³He. There the measurements of the excitation functions of the π^0 -proton production for two ranges of the relative angle between those particles were carried out. It appeared that a difference between excitation curves for opening angles of $170^{\circ} - 180^{\circ}$ and $150^{\circ} - 170^{\circ}$ in the center-of-mass frame revealed an enhancement just below the threshold of the γ^{3} He \rightarrow ³He- η reaction which was interpreted as a possible signature of a ³He- η bound state where η meson captured by one of nucleons inside helium forms an intermediate $S_{11}(1535)$ resonance which decays into π^0 -p pair. A binding energy and width for the anticipated quasibound η -mesic state in ³He were deduced from the fit of the Breit-Wigner distribution function [22] to the experimental points and equal (-4.4 ± 4.2) MeV and (25.6 ± 6.1) MeV, respectively. Those values are consistent with expectations for η -mesic nuclei. Above cited excitation functions and the difference of them with a Breit-Wigner distribution and background fitted to the data are shown in Fig. 2.3.

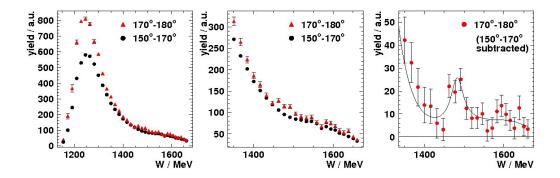


Figure 2.3: Excitation functions of the π^0 -proton production for relative angles of $170^0 - 180^0$ (red triangles) and $150^0 - 170^0$ (black circles) in the γ^3 He center-of-mass system are shown in the left and center panels. In the right panel the difference between both distributions with superimposed line denoting the results of the fit of the Breit-Wigner distribution plus background are presented. The figure is adapted from [22].

However, due to the low statistics of the measurement the results might be interpreted not as an indication of the bound state but rather as a virtual state what is in details described in Ref. [23]. The interpretation is still under discussion [24]. Moreover at the recent meeting it was shown that the result may be an artefact due to the strong influence of the resonances on the shape of the excitation function [25].

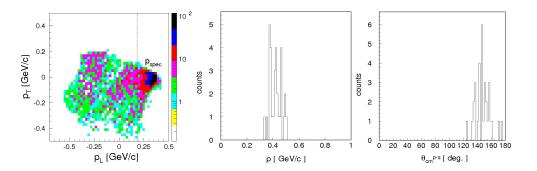


Figure 2.4: Experimental results of the COSY-11 collaboration for the $dp \rightarrow ppp\pi^-$ reaction: (left) Transversal vs. longitudinal momentum distributions of protons. The upper limit for the longituidal proton momenta is shown as dashed line and equals $p_L=0.18 \text{GeV/c}$. (middle) Pion momentum distribution in the center of mass system. (right) Relative angle between pion and proton direction in the c.m. The figure is adapted from [27].

The analysis carried out by COSY-11 group [26, 27, 28, 29] give an indication for the ³He- η bound state existence. The search for the η -mesic helium was carried out using a deuteron beam and internal hydrogen target. The beam momentum was ramped around the kinematical threshold for the η production in the $dp \rightarrow {}^{3}\text{He-}\eta$ reaction and the measurement of the $dp \rightarrow ppp\pi^{-}$ and $dp \rightarrow {}^{3}\text{He}\pi^{0}$ reactions was carried out. In the first case the momentum distribution of the π^{-} (middle panel in Fig. 2.4) and the relative angle distribution between pion and proton momentum vectors (right panel in Fig. 2.4) were determined after application of apropriate cuts on the momentum of the spectator protons (left panel in Fig. 2.4) and the rejection of the events corresponding to quasi-free π^- production. Obtained results are in agreement with theoretical expectations for particles originating from decay of the N*(1535) resonance which is created as a result of the absorption of the bound η meson in the neutron inside ³He. Based on the above results the upper limit of total cross section for the $dp \rightarrow ({}^{3}\text{He}-\eta)_{bs} \rightarrow ppp\pi^{-}$ reaction was estimated to the value of 270 nb. Similarly, investigation of the $dp \rightarrow ({}^{3}\text{He}-\eta)_{bs} \rightarrow {}^{3}\text{He}-\pi^{0}$ reaction equal to 70 nb.

3 Nucleon momentum distributions inside d, T, ³He and ⁴He nuclei

Due to the Fermi motion, nucleons inside atomic nuclei are not at rest but move with momenta which vary in a broad range. This variation influences kinematics of nuclear reactions.

Fermi momentum distributions of proton and neutron bound inside a deuteron derived from two different potential models, namely PARIS [30] and CD-Bonn [31] are shown in Fig. 3.1. The normalized nucleon momentum distributions are calculated by means of the Fourier transformation of parametrized deuteron wave functions obtained from space representation. Respective parametrization coefficients found in the analitic representation of the deuteron wave function for both of above named nucleon-nucleon interaction models are given in [30, 31, 32]. The momentum distributions deduced from Paris and CD-Bonn potentials are peaked at about 40 MeV/c and differ no more than 5% [32].

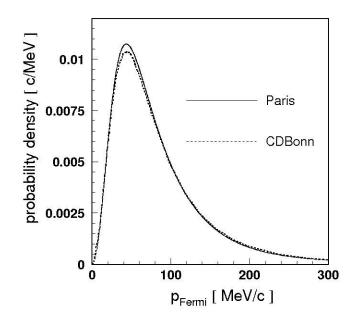


Figure 3.1: Fermi momentum distribution of nucleons inside the deuteron for PARIS (full line) and CD-Bonn (dashed line) potentials. The distributions were normalized to unity in the momentum range from 0 to 300 MeV/c.

In case of three-nucleon bound states like ³He and T, Fermi momentum distributions of nucleons are presented in Fig. 3.2 for three different models. Thick solid line depicts

proton momentum distribution inside ³He and neutron momentum distribution inside T as given by analytic formula (3.1) which results from the fit to the experimental data on $p({}^{3}\text{He}, 2p) d$ and p(T, pn) d reactions [33]:

$$f(p) = p^{2}[exp(-263p^{2}) + 0.177exp(-69.2p^{2})]$$
(3.1)

This momentum distribution is in a good agreement with the one calculated with realistic potential in the frame of the model of the composite quark bags [34].

The distributions of protons and neutrons momentum inside ³He and T are also estimated based on the AV18 and the CDB-2000 nucleon-nucleon interaction models in conjunction with Urbana IX (UIX) and Tucson-Melbourne (TM) three nucleon interactions (TNI), respectively [35, 36]. They are presented in Fig. 3.2 for protons inside ³He (left) and neutrons inside T (right) and ticked as a dashed and dotted lines. Similar results can be obtained for neutron inside helium and proton inside tritium. The difference between those two distributions are small and results from different interaction Hamiltonian forms defined for above-cited models.

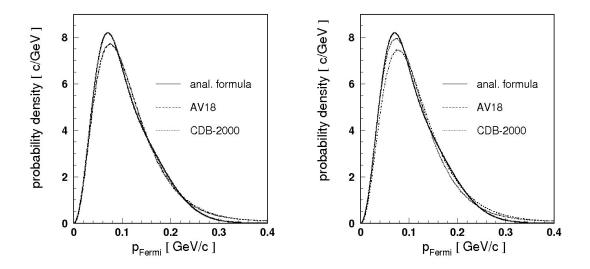


Figure 3.2: Fermi momentum distribution for protons inside ³He (left) and neutrons inside T (right) given by analytic formula (thick line) and estimated for the AV18 NN (dashed line) and the CDB-2000 NN (dotted line). The distributions were normalized to unity in the momentum range from 0 to 0.4 GeV/c.

Estimation based upon the formula (3.1) is consistent with the one derived from AV18 NN and CDB-2000 NN models with an accurancy better than 9% for protons inside ³He and 11% for neutrons inside T.

For nucleons inside ⁴He Fermi momentum distributions predicted by three independent models are shown in Fig. 3.3. The distribution represented by a thick line is calculated from helium wave function derived based on Fermi three parameter charge distribution of nucleus [37]. The momentum distribution is described by formula (3.2):

$$f(p) = \frac{p^2}{a \cdot b} exp\left(\frac{-p^2}{a \cdot c}\right),\tag{3.2}$$

where a = 0.03892719, b = 0.05511, c = 0.7352. Fermi momentum is given in units of GeV/c.

The dashed and dotted lines depict distributions obtained, similarly as in case of three nucleon systems, from AV18 and the CDB-2000 potential models with the inclusion of three nucleon interaction contributions [36]. Due to the fact that ⁴He is symmetrical, proton and neutron momentum distributions are in good approximation equal.

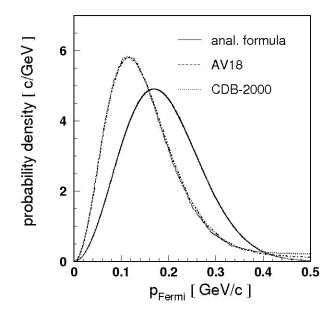


Figure 3.3: Fermi momentum distribution of nucleons inside ⁴He given by analytic formula (thick solid) and estimated for the AV18 NN (dashed) and the CDB-2000 NN (dotted). The distributions were normalized to unity in the momentum range from 0 to 0.5 GeV/c.

The difference between the distributions derived from AV18 and CDB-2000 models and given by analytic formula is significant and equals up to about 40%, and in addition the maxima of these distributions are shifted by about 45 MeV/c. The discrepancy results from the fact that the formula (3.2) was derived from nucleus charge distribution smeared out by the charge distribution of protons, whereas the AV18 and the CDB-2000 models allow for the finite size of nucleus charge distributions and are related to the momentum of the point like protons in the alpha particle [38]. Therefore, as more realistic in further considerations the momentum distributions of nucleons inside ⁴He calculated from AV18 and the CDB-2000 potentials will be taken into account.

The numerical data describing above cited momentum distributions are given in Appendix A.

The presented distributions estimated based on various models will be used to calculate the systematical uncertainty in the determination of the excitation curves used to search for η -mesic bound states. Respective results are presented in Chapter 7.

4 Spectator model

4.1 The main assumption of the spectator model

The production and decay of η -mesic bound states investigated in this thesis might be schematically depicted as:

a)
$$dd \rightarrow ({}^{4}\text{He-}\eta)_{bs} \rightarrow \begin{cases} {}^{3}\text{He}_{sp} \ p \ \pi^{-} \\ p_{sp} \ d_{sp} \ p \ \pi^{-} \end{cases}$$

b) $pd \rightarrow ({}^{3}\text{He-}\eta)_{bs} \rightarrow \begin{cases} p_{sp} \ p_{sp} \ p \ \pi^{-} \\ d_{sp} \ p \ \pi^{0} \end{cases}$

c)
$$dd \to p_{sp}nd \to p_{sp}(\mathrm{T} \cdot \eta)_{bs} \to p_{sp} \ d_{sp} \ p \ \pi^-$$

The a) and b) schemes include free and c) one describes quasi-free production of the bound states. Subscript bs denotes 'bound state' whereas sp stands for the 'spectator'.

'Spectators' are particles which do not take part in reactions [39, 40] but hit the detectors with the Fermi momentum transformed into laboratory system. Fermi momentum distributions of nucleons inside the light nuclei are presented in previous chapter. In the framework of the spectator model due to the relatively small binding energy of the nuclei, spectators are considered as a real particles registered in the experiments and in the analysis it is assumed that they are on their mass-shell during the reaction [39, 40]:

$$|\mathbb{P}_{sp}|^2 = m_{sp}^2. \tag{4.1}$$

The \mathbb{P}_{sp} and m_{sp} are the four-momentum vector of spectator and the spectator mass, respectively.

In the free reactions the beam and target nuclei collide and form η -mesic bound state which decays into proton, pion and spectator/spectators which energies and momenta are measured in experiment. One of those reactions is schematically shown in Fig. 4.1.

In case of quasi-free reaction presented in Fig. 4.2, the deuteron from the beam is considered as a system consisting of proton and neutron moving with the Fermi motions. For the deuteron beam we have:

$$\mathbb{P}_d = \mathbb{P}_n^b + \mathbb{P}_{p_{sp}} \tag{4.2}$$

$$\left|\mathbb{P}_{p_{sp}} + \mathbb{P}_n^b\right|^2 = m_d^2,\tag{4.3}$$

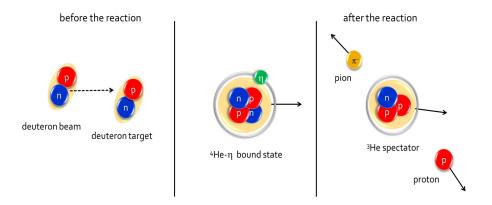


Figure 4.1: Schematic picture of the $dd \rightarrow ({}^{4}\text{He}-\eta)_{bs} \rightarrow {}^{3}\text{He}p\pi^{-}$ reaction. Red and blue circles represent protons and neutrons respectively, whereas π^{-} meson is depicted as yellow circle. The beam momentum is presented by the dashed arrow.

where m_d denotes the deuteron mass equal to 1875.6 MeV/c² [41] while $\mathbb{P}_{p_{sp}}$ and \mathbb{P}_n^b are the four-momentum vectors of the proton spectator and the beam neutron, respectively.

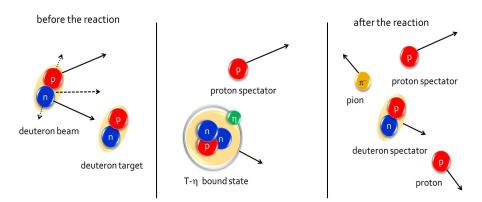


Figure 4.2: Schematic picture of the quasi-free $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ reaction. Red and blue circles represent protons and neutrons respectively, whereas η meson is depicted as green circle. The Fermi momentum of the nucleons inside the deuteron is presented by the dotted arrows and the beam momentum by the dashed one.

According to the spectator model, proton from the beam does not take part in the reaction and is registered as a real particle whereas neutron being off the mass-shell hits the target deuteron. From the conservations of momentum and energy and the assumption that proton is on its mass-shell we obtain in the deuteron beam rest frame:

$$\vec{p_n^*} = -\vec{p_{sp}^*},$$
 (4.4)

$$E_n^* = m_d - E_{p_{sp}}^*, (4.5)$$

Based on above-mentioned relationship we can deduce the neutron four-momentum vector from the spectator momentum which is fundamental in the analysis of reaction kinematics. The close description of free and quasi-free reactions processes is described in Chapter 5.

4.2 Experimental proofs of spectator model

The validity of spectator model assumptions was confirmed by measurements performed by collaborations WASA/PROMICE [42], TRIUMF [43], COSY-TOF [44], COSY-11 [45] and HADES [46]. The WASA/PROMICE collaboration [42] has compared free and quasi-free production cross sections for the $pp \rightarrow pp\eta$ reaction. As a result it was presented that within the statistical errors there is no difference between the total cross section of the free and quasi-free process. The experimental data are shown in Fig. 4.3.

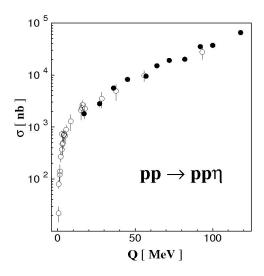


Figure 4.3: Total cross section for the $pp \rightarrow pp\eta$ reaction as a function of the excess energy for free (open circles) and quasi-free proton scattering (full circles). Figure is adapted from [47]. The data are taken from references [48, 49, 50, 51, 52, 53, 54].

Investigation of pion production at the TRIUMF [43] facility in quasi-free $pp \to d\pi^+$ reaction extracted from the $pd \to d\pi^+ n$ reaction has proven that the spectator momentum distribution determined from the experimental data agrees with expectations based on spectator model. Moreover, it was shown that the magnitude of the differential cross sections for the quasi-free and for the free reactions are consistent on the few per cent level.

The spectator assumption was also confirmed by the COSY-TOF group [44]. The momentum distribution of the spectator as well as the shape of the angular distribution for the quasi-free $np \rightarrow pp\pi^-$ and $pn \rightarrow pn$ reactions have been measured. The experimental data are consistent with calculations based upon the hypothesis of spectator

model with an accurancy better than 4% up to 150 MeV/c of the Fermi momentum and with about 25% up to a momentum of 300 MeV/c.

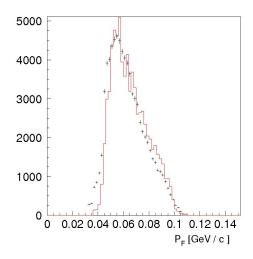


Figure 4.4: Proton spectator momentum distribution reconstructed in COSY-11 experiment (points) in comparison with simulation taking into account Fermi momentum distribution of nucleons inside deuteron, the acceptance and the efficiency of the detector system (solid histogram). The figure is adapted from [45].

In case of quasi-free $pn \rightarrow pn\eta'$ reaction studied at COSY-11 facility [45] it is shown that the measured proton spectator momentum distribution is in good agreement with the theoretical assumptions of spectator model. The comparison of the experimental data and simulation result is shown in Fig. 4.4.

Recently, the validity of the spectator model was proven also by HADES collaboration [46] during the measurement of the quasi-free $np \rightarrow e^+e^-pX$ reaction realised with a deuteron beam and proton target. The angular distribution of proton spectator outgoing from deuteron beam and its momentum distribution agrees with assumptions of spectator model up to 200-300 MeV/c. Momentum distributions in deuteron CM frame are presented in Fig. 4.5. Experimental data are ticked as a red points, while simulations results based on the spectator model as a black points.

The above-cited results confirmed the spectator model and thus allow to use it in the analysis of the reactions kinematics.

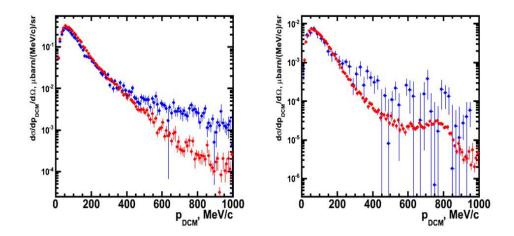


Figure 4.5: Momentum distribution of proton spectator measured in HADES experiment (red points) and calculated based upon the hypothesis of spectator model (blue points) for $M_{e^+e^-} < 140 \text{MeV/c}^2$ (left) and for $M_{e^+e^-} > 140 \text{MeV/c}^2$ (right). Picture courtesy of [46].

5 Kinematics of the η -mesic bound states production and decays

In this thesis four reactions of free and one of quasi-free η -mesic bound states production are considered [55]:

- 1. $dd \rightarrow ({}^{4}\text{He-}\eta)_{bs} \rightarrow {}^{3}\text{He}p\pi^{-}$
- 2. $dd \rightarrow ({}^{4}\text{He-}\eta)_{bs} \rightarrow dpp\pi^{-}$
- 3. $pd \rightarrow ({}^{3}\text{He-}\eta)_{bs} \rightarrow dp\pi^{0} \rightarrow dp\gamma\gamma$
- 4. $pd \to ({}^{3}\text{He-}\eta)_{bs} \to ppp\pi^{-}$
- 5. $nd \to (T-\eta)_{bs} \to dp\pi^-$

In case of free reactions (1)-(4), ⁴He- η and ³He- η bound states are produced in deuteron-deuteron and proton-deuteron fusion, respectively [56]. The mechanism of the reactions is presented schematically in the example of the (⁴He- η)_{bs} production in Fig. 5.1. Describing the kinematics of the reaction following notations will be used:

$$\begin{split} \mathbb{P}_{d}^{b} &= (E_{d}^{b}, \vec{p}_{b}) \text{-four-momentum vector of the beam deuteron} \\ \mathbb{P}_{d}^{t} &= (m_{d}, 0) \text{-four-momentum vector of the target deuteron} \\ \mathbb{P}_{3He}^{a} &= (E_{3He}, \vec{p}_{3He}) \text{-four-momentum vector of the outgoing }^{3}\text{He} \\ \mathbb{P}_{p}^{a} &= (E_{p}, \vec{p}_{p}) \text{-four-momentum vector of the outgoing proton} \\ \mathbb{P}_{\pi^{-}}^{a} &= (E_{\pi^{-}}, \vec{p}_{\pi^{-}}) \text{-four-momentum vector of the outgoing pion} \end{split}$$

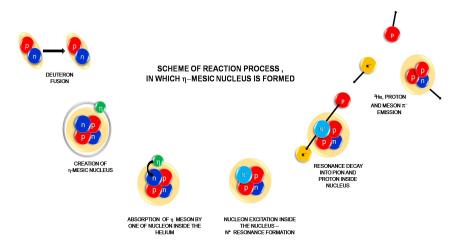


Figure 5.1: Reaction process of the $({}^{4}\text{He}-\eta)_{bs}$ production and decay.

According to the scheme shown in Fig. 5.1, the deuteron from the beam hits the deuteron in the target with a momentum of \vec{p}_b . The collision may lead to the creation of ⁴He nucleus bound with the η meson via strong interaction. The mass of a bound state is a sum of η and ⁴He masses reduced by binding energy (B_s):

$$m_{bs} = m_{\eta} + m_{^4He} - B_s. \tag{5.1}$$

The η -mesic nucleus moves in laboratory frame with velocity:

$$\vec{\beta}_{cm} = \frac{\vec{p}_b}{m_d + E_d^{\ b}} = \frac{2\,\vec{p}_b\,m_d}{s_{dd}},\tag{5.2}$$

where s_{dd} is the square of invariant mass of the colliding deuterons:

$$s_{dd} = |\mathbb{P}_d^b + \mathbb{P}_d^t|^2 = 2m_d \left(m_d + \sqrt{m_d^2 + |\vec{p_b}|^2} \right).$$
(5.3)

The η meson might be absorbed by one of the nucleons inside helium and may propagate in the nucleus via consecutive excitation of nucleons to the N^{*}(1525) state [57] until the resonance decays into the pion-proton pair outgoing from the nucleus [10, 56, 58]. Before the decay, it is assumed that N^{*} resonance moves with a Fermi momentum \vec{p}_F^* inside ⁴He. From the momentum conservation in the ⁴He frame and the assumption of spectator model, momentum and energy of ³He may be expressed as:

$$\vec{p}_{3He}^* = -\vec{p}_F^* \tag{5.4}$$

$$E_{^{3}He}^{*} = \sqrt{m_{^{3}He}^{2} + |\vec{p}_{F}^{*}|^{2}}.$$
(5.5)

The momentum and energy are transformed into the laboratory frame by means of Lorentz transformation:

$$\vec{p}_{^{3}He} = \vec{p}_{^{3}He}^{*} + \vec{\beta}_{cm}\gamma_{cm}(\gamma_{cm}/(\gamma_{cm}+1)\vec{\beta}_{cm}\cdot\vec{p}_{^{3}He}^{*} + E_{^{3}He}^{*})$$
(5.6)

$$E_{^{3}He} = \gamma_{cm} (E_{^{3}He}^{*} + \vec{\beta}_{cm} \cdot \vec{p}_{^{3}He}^{*}), \qquad (5.7)$$

where $\gamma_{cm} = 1/\sqrt{1 - |\vec{\beta}_{cm}|^2}$.

The angle between outgoing ³He and the beam direction is given by:

$$\theta_{^{3}He} = \arccos\left(\frac{\vec{p}_{^{3}He} \cdot \vec{p}_{b}}{|\vec{p}_{^{3}He}| \cdot |\vec{p}_{b}|}\right).$$
(5.8)

The relative angle between the outgoing nucleon-pion pair is equal to 180° in the N^{*} reference frame. In the following the variables in the N^{*} reference frame will be denoted by '**'. Both particles move with a momentum $|p_{p,\pi^-}|$ which is related to the resonance mass:

$$m_{N^*} = \left(s_{dd} + m_{^{3}He}^2 - 2\sqrt{s_{dd}}\sqrt{m_{^{3}He}^2 + |\vec{p}_F^*|^2}\right)^{\frac{1}{2}},$$
(5.9)

and is given by:

$$|\vec{p}_{p,\pi^{-}}^{**}| = \frac{\lambda(m_{N^{*}}^{2}, m_{\pi^{-}}^{2}, m_{p}^{2})}{2m_{N^{*}}},$$
(5.10)

where $\lambda(x, y, z) = (x - y - z)^2 - 4yz$ [59].

The pion and proton four-momentum vectors in the laboratory frame are calculated using the Lorentz transformation, first from N^* to the bound state frame:

$$\vec{p}_{p,\pi^{-}}^{*} = \vec{p}_{p,\pi^{-}}^{**} + \vec{\beta}_{N^{*}} \gamma_{N^{*}} (\gamma_{N^{*}} / (\gamma_{N^{*}} + 1) \vec{\beta}_{N^{*}} \cdot \vec{p}_{p,\pi^{-}}^{**} + E_{p,\pi^{-}}^{**})$$
(5.11)

$$E_{p,\pi^{-}}^{*} = \gamma_{N^{*}} (E_{p,\pi^{-}}^{**} + \vec{\beta}_{N^{*}} \cdot \vec{p}_{p,\pi^{-}}^{**}), \qquad (5.12)$$

and further to the laboratory frame:

$$\vec{p}_{p,\pi^{-}} = \vec{p}_{p,\pi^{-}}^{*} + \vec{\beta}_{cm}\gamma_{cm}(\gamma_{cm}/(\gamma_{cm}+1)\vec{\beta}_{cm}\cdot\vec{p}_{p,\pi^{-}}^{*} + E_{p,\pi^{-}}^{*})$$
(5.13)

$$E_{p,\pi^{-}} = \gamma_{cm} (E_{p,\pi^{-}}^{*} + \vec{\beta}_{cm} \cdot \vec{p}_{p,\pi^{-}}^{*}), \qquad (5.14)$$

where $\gamma_{N^*} = 1/\sqrt{1 - |\vec{\beta}_{N^*}|^2}$ is a velocity of the resonance N^{*} in the bound state frame. The angles of outgoing proton and pion in LAB system equals:

$$\theta_{p,\pi^-} = \arccos\left(\frac{\vec{p}_{p,\pi^-} \cdot \vec{p}_b}{|\vec{p}_{p,\pi^-}| \cdot |\vec{p}_b|}\right).$$
(5.15)

The quasi-free reaction kinematics was partially characterized in Chapter 4 by the way of the spectator model description. Neutron bound inside the deuteron hits the deuteron target forming the $(T-\eta)_{bs}$, while proton does not take part in reaction and is considered as a real particle:

$$|\mathbb{P}_{p_{sp}}|^2 = m_{p_{sp}}^2. \tag{5.16}$$

The square of invariant mass of neutron-deuteron system (s_{nd}) depends on the neutron Fermi momentum \vec{p}_n^* (5.1.3) inside the beam deuteron and taking into account that target deuteron is at rest in the laboratory s_{nd} equals:

$$s_{nd} = (E_n + m_d)^2 - |\vec{p}_n|^2, \qquad (5.17)$$

where \vec{p}_n and E_n are neutron momentum and energy in laboratory frame which may be obtained applying the Lorentz transformation according to the following formulas:

$$\vec{p}_n = \vec{p}_n^* + \vec{\beta}_d \gamma_d (\gamma_d / (\gamma_d + 1)\vec{\beta}_d \cdot \vec{p}_n^* + E_n^*)$$
(5.18)

$$E_n = \gamma_d (E_n^* + \vec{\beta}_d \cdot \vec{p}_n^*), \qquad (5.19)$$

where $\vec{\beta}_d$ denotes velocity of the beam deuteron in the laboratory frame, and \vec{p}_n^* denotes neutron momentum in the deuteron center of mass, and $E_n^* = m_d - \sqrt{m_p^2 + |p_n^*|^2}$.

The process of T- η bound state decay is analogous like in case of the free reaction which kinematics was described before. The deuteron spectator escapes with the Fermi momentum and energy, which in the frame of the bound state is equal to:

$$\vec{p}_d^* = -\vec{p}_F^* \tag{5.20}$$

$$E_d^* = \sqrt{m_d^2 + |\vec{p}_F^*|^2},\tag{5.21}$$

After the transformation into laboratory system we have:

$$\vec{p}_d = \vec{p}_d^* + \vec{\beta}_{cm'} \gamma_{cm'} (\gamma_{cm'} / (\gamma_{cm'} + 1) \vec{\beta}_{cm'} \cdot \vec{p}_d^* + E_d^*)$$
(5.22)

$$E_d = \gamma_{cm'} (E_d^* + \vec{\beta}_{cm'} \cdot \vec{p}_d^*), \qquad (5.23)$$

where $\vec{\beta}_{cm'} = \frac{\vec{p}_n}{m_d + E_n}$ denotes velocity of the center of mass for the quasi-free $nd \to (T - \eta)_{bs} \to dp\pi^-$ reaction in the laboratory frame.

The outgoing proton-pion pair originates from the decay of the resonance created via absorption of the η meson on a nucleon in the tritium nucleus. The four-momenta

of those particles are described in resonace frame by equations analogous to (5.11) and (5.12), and in laboratory frame by formulas (5.13) and (5.14) while proton and pion angles with relation to the beam direction are given by (5.15).

6 Experimental setup

6.1 WASA-at-COSY facility

The search for η -mesic helium in free production reactions with high statistic and acceptance is carried out at the WASA facility [9], an internal detection system installed at the cooler synchrotron COSY in the Research Center Jülich. The WASA detector vertical cross section is schematically presented in Fig. 6.1. All setup components and the method of measurement are described in detail in reference [9]. Thus, in this chapter the experimental technique will be only shortly presented.

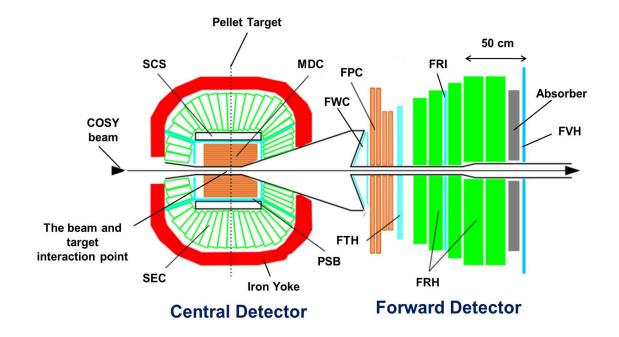


Figure 6.1: Scheme of WASA-at-COSY detection system. Gamma quanta, electrons and charged pions being products of mesons decays are registered in the Central Detector. Scattered projectiles and charged recoil particles like ³He, deuterons and protons are registered in the Forward Detector. The abbreviations of the detectors names are explained in the text.

In the COSY synchrotron protons and deuterons might be accelerated in the momentum range between 0.3 GeV/c and 3.7 GeV/c [9]. The ring can be filled with up to 10^{11} particles leading to luminosities of 10^{31} cm⁻²s⁻¹ in case of internal cluster target [60] and 10^{32} cm⁻²s⁻¹ in case of pellet target [9]. Beams are cooled by means of electron cooling as well as stochastic cooling at injection and high energies, respectively.

The internal hydrogen (H₂) or deuteron (D₂) target of the pellet-type is installed in the central part of the WASA-at-COSY detector and its position is marked in Fig. 6.1 as a dotted line. The central detector is built around the interaction point and designed for measurements of π^0 and η mesons decay products like photons, electrons and charged pions. The charged particles momenta and reaction vertex are determined by means of Mini Drift Chamber (MDC) which covers angles from 24^{0} to 159^{0} . Charged particles are here bending in the magnetic field provided by sourrounding Superconducting Solenoid (SCS). First their trajectories are reconstructed, and then knowing the magnetic field, the momentum vector is reconstructed. For identification of charged particles the ΔE -p and ΔE -E methods are used based on ΔE signals in Plastic Scintillator Barrel (PSB). The photons, electrons and positrons are registered in Scintillator Electromagnetic Calorimeter (SEC) via production of electromagnetic cascades. The calorimeter covers polar angle in the range from 20^{0} to 169^{0} .

The detection and identification of forward scattered projectiles and target-recoil particles such as protons, deuterons and He nuclei and also of neutrons and charged pions are carried out with the Forward Detector which covers the range of polar angles from 3⁰ to 17⁰. It consists of fourteen planes of plastic scintillators forming Forward Window Counter (FWC), Forward Trigger Hodoscope (FTH), Forward Range Hodoscope (FRH), Forward Range Interleaving Hodoscope (FRI) and Forward Veto Hodoscope (FVH), respectively and proportional counter drift tubes called Forward Proportional Chamber (FPC). Particles trajectories are reconstructed from the signals registered successively in FWC, FPC, FTH and FVH scintillator modules. Particles are identified based on measurement of energy loss in the detection layers of FRH, FWC and FTH. The registered energy loss allows to determine their total momentum which direction is reconstructed from the measurement of particles tracks by means of straw detectors constituting FPC. Respective components of the Forward Detector are presented in Fig. 6.1.

The ³He- η and ⁴He- η bound states considered in this thesis can be searched at WASA-at-COSY detection setup in proton-deuteron and deuteron-deuteron fusion reaction, respectively. The measurement will be carried out for the beam momentum slowly ramped around the η production threshold corresponding to the range of excess energy Q from about -60 MeV to 20 MeV. The existence of the η -mesic nucleus should be visible in the excitation function as a resonance-like structure below the He- η production threshold. The free η -helium bound states production reactions will be carried out in experiment based on measurement of four-momenta of the outgoing particles. WASA detector at COSY allows for simultaneous registration of all ejectiles with large acceptance, which eg. for the detection of the $dd \rightarrow ({}^{4}\text{He-}\eta)_{bs} \rightarrow {}^{3}\text{He}p\pi^{-}$ reaction equals about 60%. Spectators from the reactions will be registered mainly in the Forward Detector, while proton-pion pair from the resonance decay will be registered for the most part in the Central Detector. The detailed description of the reactions kinematics is given in Chapter 5.

6.2 COSY-TOF facility

The measurement of η -mesic tritium might be realised by means of the quasi-free reaction with the time-of-flight spectometer COSY-TOF, a ' 4π detector' installed at an external beamline of the COSY synchrotron. The detection setup is schematically presented in Fig. 6.2. Detailed description of each particular parts and the measurement technique might be found in [11, 13, 44].

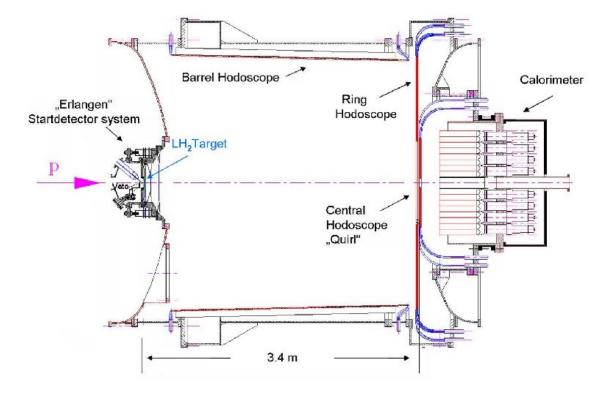


Figure 6.2: Scheme of COSY-TOF detection setup. Charged particles trajectories are registered in 'Erlangen' start detector system, while their identification is carried out with the Barrel, Ring and Quarrel detectors. The figure is adapted from [13].

The proton or deuteron beam accelerated in COSY is extracted and hits a target which contains liquid hydrogen or liquid deuterium [11, 12]. The target is installed in front of the 'Erlangen' start detector system consisting of four modular detectors (Starttorte, Microstrip detector, Small Hodoscope and Large Hodoscope) designed for a precision geometric charged particles tracks reconstruction. The detector covers a polar angular range from 3.4^{0} to 74^{0} . The time-of-flight of the charged particles outgoing after the interaction of the beam particles with the target, is measured with an accuracy of 0.25 ns by means of the stop detector situated in cylindric vacuum tank. This detector consists of Barrel detector as well as of two Endcap detectors called Quirl and Ring and covers angular range from 0.7^{0} to 76.7^{0} . Knowing the time-of-flight and the flight length between start and stop detectors, particles velocity is determined. The particle momentum can be calculated from the velocity and the mass hypothesis. Additionally, neutral particles which take part in the reactions and have not been detected can be analysed via momentum and energy conservation.

The search of η -tritium bound state can be carried out at COSY-TOF facility via the measurement of the excitation function of the $nd \to (T-\eta)_{bs} \to dp\pi^-$ reaction. The signal from $(T-\eta)_{bs}$ is expected below the threshold of the $nd \to T-\eta$ production [10, 55]. In the experiment deuteron beam will be used and the nd reaction will be analized based on the measurement of the four-momentum of spectator proton (p_{sp}) [10] from the $dd \to p_{sp}nd \to p_{sp}(T-\eta)_{bs} \to p_{sp}dp\pi^-$ reaction, which was schematically shown in Fig 4.2. The advantage of this quasi-free reaction is that the Fermi momentum distribution of nucleons inside the deuteron beam allows for the scan of energy around the η meson production threshold at a fixed value of the beam momentum. Deuterons, protons and pions being products of T- η bound states decays will be detected in a multi layer scintillator detectors by measuring their time of flight as well as direction.

7 Simulation results

In this chapter simulation results of the free and quasi-free η -mesic bound states production are presented. Monte-Carlo calculations were carried out by means of computer programme written in FORTRAN'90 language.

7.1 Simulation program scheme

The main purpose of simulations was the determination of the geometrical acceptances of WASA-at-COSY and COSY-TOF detectors for free and quasi-free reactions, respectively and comparing them for different models of nucleon momentum distribution inside atomic nuclei and different values of a bound states width.

In case of free reactions the simulation might be schematically described in following points for example of reaction (1) which kinematics is presented in details in Chapter 5:

1. The square of invariant mass of the whole system $\sqrt{s_{dd}}$ is distributed randomly according to the Breit-Wigner distribution which is given by formula (7.1) and shown in Fig. 7.1.

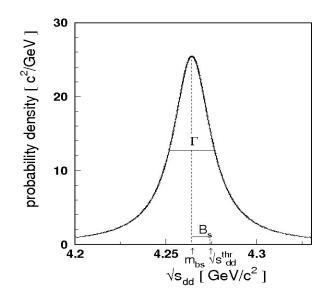


Figure 7.1: Breit-Wigner distribution of square invariant mass $\sqrt{s_{dd}}$.

$$N\left(\sqrt{s_{dd}}\right) = \frac{1}{2\pi} \frac{\Gamma}{\left(\sqrt{s_{dd}} - m_{bs}\right)^2 + \Gamma^2/4}$$
(7.1)

where: $m_{bs} = \sqrt{s_{dd}}^{thr} - B_s$ - a mass of η -mesic bound state,

 $\sqrt{s_{dd}}^{thr} = m_{\eta} + m_{^4He}$ - threshold square invariant mass,

- B_s a binding energy of an η -mesic bound state,
- Γ width of an $\eta\text{-mesic}$ bound state.

In the distribution shown in Fig. 7.1 it is assumed that binding energy equals $B_s=0.01$ GeV and a width is equal to 40 MeV what is in agreement with theoretical prediction [6]. In simulations a range of Γ from 7 to 40 MeV was studied.

2. The N^{*} resonance momentum is distributed isotropically in spherical coordinates of η -mesic nucleus $(p_F^*, \theta^*, \phi^*)$ with Fermi momentum distribution of nucleons inside ⁴He which was presented for three different models in Chapter 3. Next, it is transformed into Cartesian coordinates $(\vec{p}_F^*=(p_F^{*x}, p_F^{*y}, p_F^{*z}))$ using the following equations:

$$p_F^{*x} = p_F^* \cdot \sin\theta^* \cdot \cos\phi^* \tag{7.2}$$

$$p_F^{*y} = p_F^* \cdot \sin\theta^* \cdot \sin\phi^* \tag{7.3}$$

$$p_F^{*z} = p_F^* \cdot \cos\theta^* \tag{7.4}$$

Here the momentum value p_F^* is distributed according to the used model, and the direction is simulated isotropically in the space.

- 3. The ³He four momentum vector is calculated (based on spectator model assumption) in the center of mass frame and transformed using Lorentz transformation into laboratory frame. The angle $\theta_{^{3}He}$ is also calculated.
- 4. Based on $\sqrt{s_{dd}}$ and \vec{p}_F^* values, resonance mass m_{N^*} is calculated according to equation (5.9).
- 5. The proton and pion momentum vectors are simulated isotropically in the N^{*} frame in spherical coordinates and transformed into Cartesian coordinates. The absolute value of \vec{p}_{p,π^-}^{**} is fixed by equation (5.10).

- 6. The proton and pion four momentum vectors are transformed into the center of mass frame and next into laboratory frame by means of Lorentz transformation. The angles of outgoing proton and pion in LAB system are calculated.
- 7. The histograms of outgoing particles angle distributions and invariant mass distribution for all generated events are created.
- 8. Knowing angles of outgoing particles and the WASA-at-COSY detector geometry it is checked whether generated event can be registered.
- 9. The histograms of angular distributions and invariant mass distribution of outgoing particles for all accepted events are created.

The simulation of other three free η -helium bound states production reactions were carried out in a similar way.

The simulation of quasi-free reaction, realised with COSY-TOF detection setup is more complex due to the fact that neutron bound in beam deuteron takes part in the reaction of η -mesic tritium formation. The simulation scheme might be presented as follows:

- 1. The beam neutron momentum is distributed isotropically in spherical coordinates with Fermi momentum distribution of nucleons inside beam deuteron (the PARIS and CD-Bonn distributions are presented in Chapter 3) and transformed into Cartesian coordinates (p_n^*) .
- 2. The proton spectator four momentum vector as well as its angle with respect to the beam direction are calculated in the beam deuteron center of mass frame and transformed with Lorentz transformation into laboratory frame.
- 3. The neutron four momentum in the beam deuteron frame and in laboratory frame is calculated using (4.4), (4.5) and (5.18), (5.19) formulas, respectively.
- 4. The square of bound state invariant mass $\sqrt{s_{nd}}$ is calculated based on neutron four momentum and next events are accepted according to the probability described by the Breit-Wigner distribution.
- 5. The next points are analogous like in case of free reaction scheme. Moreover, the calculations are carried out for ten values of the deuteron beam momentum \vec{p}_{beam} in the range from 2.6 GeV/c to 3.5 GeV/c.

Simulations were conducted for all reactions listed in introduction. Three different values of the bound states width: $\Gamma = \{10, 25, 40\}$ MeV and three different Fermi momentum distributions of nucleons inside light atomic nuclei were studied.

7.2 Reactions products - angular distributions

The η -mesic nuclei, which are formed via deuteron-deuteron, proton-deuteron or neutron-deuteron fussion, decay according to the mechanism which is described in details in Chapter 5. The distribution of momentum vectors of reaction products depend on the bound state mass distribution and on the distribution of the nucleons momentum inside decayed nuclei. Angular distributions for the outgoing particles being products of reaction (1) are presented in Fig. 7.2.

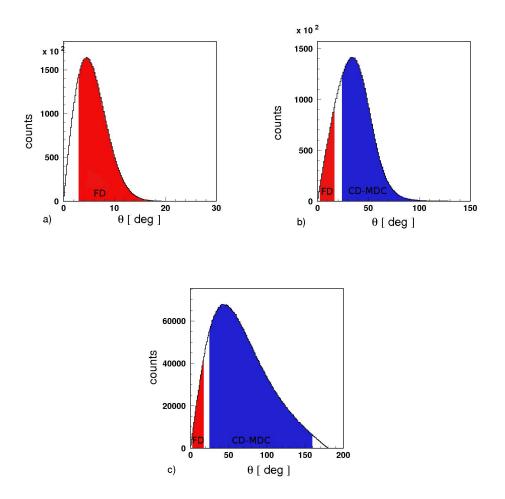


Figure 7.2: Simulated angular distributions of outgoing ³He (a), proton (b) and pion (c) formed via $dd \rightarrow ({}^{4}\text{He}-\eta)_{bs} \rightarrow {}^{3}\text{He}p\pi^{-}$ reaction. Figure shows results for 10⁸ generated events using the AV18 potential model for the Fermi momentum distribution of nucleons inside ⁴He.

In fact the detectors geometry does not give a possibility to register the whole range of outgoing particles angles. An angular ranges covered by respective components of WASA-at-COSY detection setup are presented in Fig. 7.2 with shaded areas.

7.3 Acceptance

In order to determine acceptance for respective reaction, the studied excess energy range was divided into small intervals. Next for each interval of $Q (Q = \sqrt{s} - \sqrt{s}^{thr})$ the number of events accepted by detector was divided by number of generated events. An event is accepted when all outgoing particles being reaction products can be registered in the detector. In simulations all possible combinations of particles registration in different part of detectors were considered. They are presented for particular reactions in Appendix B.

The acceptance for each reaction was determined for three different values of the bound states width Γ : 10MeV, 25MeV and 40MeV and for three models of nucleons Fermi momentum distributions inside ⁴He, ³He or T which are in details described in Chapter 3.

The WASA acceptance as a function of the excess energy Q is presented for two reactions of free ⁴He- η and ³He- η production: $dd \rightarrow (^{4}\text{He-}\eta)_{bs} \rightarrow ^{3}\text{He}p\pi^{-}$ and $pd \rightarrow (^{3}\text{He-}\eta)_{bs} \rightarrow dp\pi^{0} \rightarrow dp\gamma\gamma$ in Fig. 7.3 and Fig. 7.4, respectively. The acceptance is almost constant as a function of excess energy and it is independent of the value of Γ and model of Fermi momentum distribution within a few per cent. For two other reactions situation is analogous.

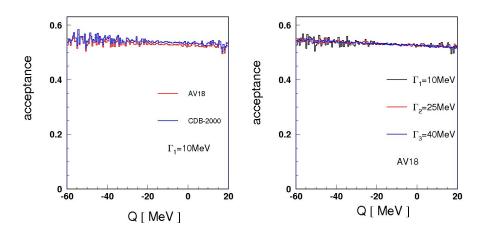


Figure 7.3: Geometrical acceptances of the WASA-at-COSY detector in case of $dd \rightarrow ({}^{4}\text{He}-\eta)_{bs} \rightarrow {}^{3}\text{He}p\pi^{-}$ reaction for the $\Gamma_{1}=10$ MeV width and AV18 and CDB-2000 models of nucleon Fermi momentum distribution inside ${}^{4}\text{He}$ (left) as well as for AV18 Fermi momentum distribution model and three different values of Γ (right).

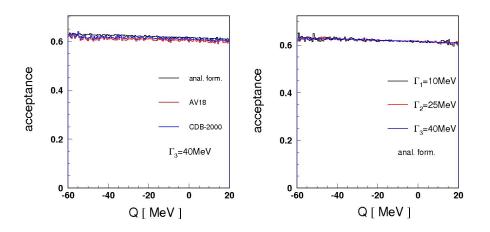


Figure 7.4: Geometrical acceptances in case of $pd \rightarrow ({}^{3}\text{He}-\eta)_{bs} \rightarrow dp\pi^{0} \rightarrow dp\gamma\gamma$ reaction for the $\Gamma_{3}=40$ MeV width and three different models of nucleon Fermi momentum distribution inside ${}^{3}\text{He}$ (left) as well as for analitic formula describing nucleon Fermi momentum distribution and three different values of Γ (right).

The average values of WASA geometrical acceptances for registering the considered free reactions were calculated using following formula:

$$A = \frac{\sum_{Q} \frac{N_{acc}(Q)}{N_{gen}(Q)}}{N} \tag{7.5}$$

where: $N_{acc}(Q)$ - the number of accepted events in a given interval of Q,

 $N_{gen}(Q)$ - the number of generated events in a given interval of Q,

N- the number of all ranges of summation.

The obtained results for different gamma values and different models of nucleon momentum distributions are presented in following tables:

[MeV/c]	AV18	CDB2000
Γ1	0.5296	0.5380
$\Gamma 2$	0.5301	0.5377
Γ3	0.5323	0.5402

Table 7.1: Average acceptances of WASA-at-COSY detector for the $dd \rightarrow ({}^{4}\text{He}-\eta)_{bs} \rightarrow {}^{3}\text{He}p\pi^{-}$ reaction for three different Γ values and AV18 and CDB-2000 models of nucleon momentum distribution inside ${}^{4}\text{He}$.

[MeV/c]	AV18	CDB2000
Γ1	0.3785	0.3889
Γ2	0.3758	0.3877
Γ3	0.3749	0.3866

Table 7.2: Average acceptances of WASA-at-COSY detector for the $dd \rightarrow ({}^{4}\text{He}-\eta)_{bs} \rightarrow dpp\pi^{-}$ reaction for three different Γ values and AV18 and CDB-2000 models of nucleon momentum distribution inside ${}^{4}\text{He}$.

[MeV/c]	anal. form.	AV18	CDB2000
Γ1	0.6175	0.6071	0.6139
$\Gamma 2$	0.6187	0.6091	0.6130
$\Gamma 3$	0.6188	0.6067	0.6135

Table 7.3: Average acceptances of WASA-at-COSY detector for the $pd \rightarrow ({}^{3}\text{He}-\eta)_{bs} \rightarrow dp\pi^{0} \rightarrow dp\gamma\gamma$ reaction for three different Γ values and three different models of nucleon momentum distribution inside ${}^{3}\text{He}$.

[MeV/c]	anal. form.	AV18	CDB2000
Γ1	0.5054	0.5059	0.5052
$\Gamma 2$	0.5083	0.5029	0.5042
$\Gamma 3$	0.5054	0.5070	0.5045

Table 7.4: Average acceptances of WASA-at-COSY detector for the $pd \rightarrow ({}^{3}\text{He}-\eta)_{bs} \rightarrow ppp\pi^{-}$ reaction for three different Γ values and three different models of nucleon momentum distribution inside ${}^{3}\text{He}$.

For the quasi-free reaction $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ the COSY-TOF acceptance was calculated for ten of beam momentum values for the range of $\vec{p}_{beam}=2.6 \text{ GeV/c}$ to 3.5 GeV/c. The excess energy distribution for $nd \rightarrow (T-\eta)_{bs}$ reactions determined by the Fermi momentum distribution of neutron inside deuteron is presented in Fig. 7.5 for p_{beam} equal to 2.6 GeV/c, 3.1 GeV/c and 3.5 GeV/c.

For each case, the number of $nd \to (T-\eta)_{bs}$ generated events as a function of the excess energy Q is represented by solid line while the excess energy distribution for accepted events is shown by dashed line. The threshold deuteron beam momentum for the $dd \to p_{sp}(T-\eta)_{bs}$ is equal 3.1 GeV/c for the case if the Fermi momentum in the beam deuteron is equal to 0.

Similarly like in case of free reactions, the COSY-TOF acceptance function is obtained by dividing the number of accepted events by the number of generated events for each of excess energy intervals. Respective results for three values of deuteron beam momentum are presented in Fig. 7.6 (a), (b) and (c).

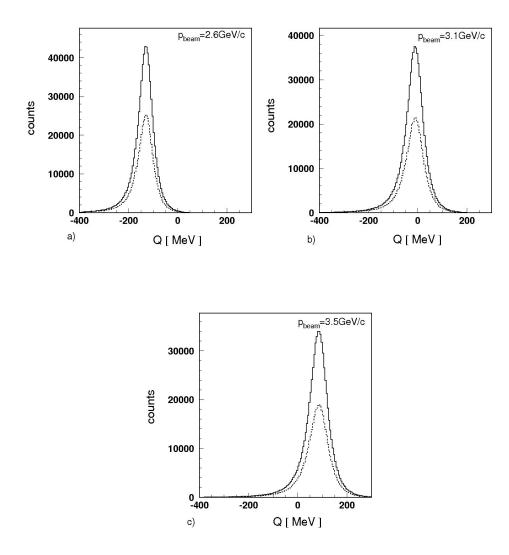


Figure 7.5: The number of generated (solid) and accepted $nd \rightarrow (T-\eta)_{bs} \rightarrow dp\pi^-$ events (dashed) as a function of excess energy Q with respect to quasi-free $nd \rightarrow (T-\eta)_{bs}$ reaction at deuteron beam momentum $p_{beam}=2.6 \text{ GeV/c}$ (a), $p_{beam}=3.1 \text{ GeV/c}$ (b) and $p_{beam}=3.5 \text{ GeV/c}$ (c).

The acceptance of ejectiles registration in the quasi-free reaction is not constant function of excess energy. It decreases for Q values corresponding to the Fermi momentum of neutron in the deuteron beam equal to zero and results from the fact that proton spectator is not accepted by detector geometry if its Fermi momentum value in deuteron frame equals $p_{sp}^*=0$. For a comparison, Fig. 7.6 (d) presents that the acceptance dependence of Q would be constant if the proton spectator was accepted.

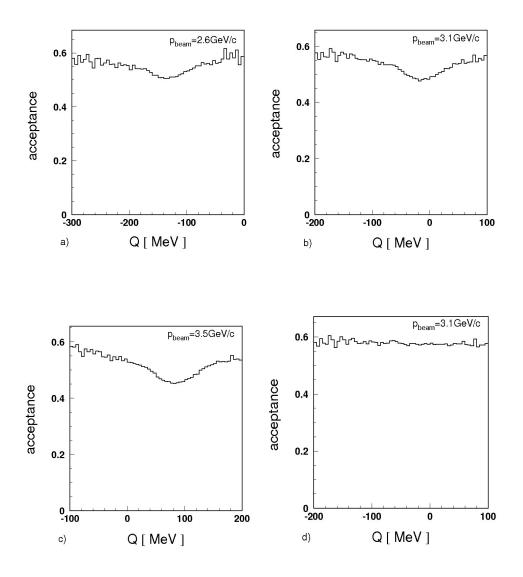


Figure 7.6: Geometrical COSY-TOF acceptances in case of the $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^$ reaction at $p_{beam}=2.6 \text{ GeV/c}$ (a), $p_{beam}=3.1 \text{ GeV/c}$ (b) and $p_{beam}=3.5 \text{ GeV/c}$ (c). For the simulations Paris model of nucleon Fermi momentum distribution inside deuteron and $\Gamma_1=10$ MeV bound state width and analitic formula describing nucleon Fermi momentum distribution inside T were used. Panel (d) represents the reaction acceptance for $p_{beam}=3.1 \text{ GeV/c}$ with assumption that the detector acceptance for proton spectator registration equals 1.

In order to determine the effective acceptance for registering the quasi-free $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ reaction in the near to threshold Q range from -60 MeV to 20 MeV when using the TOF detector the following formula is used:

$$A_{eff} = A \frac{N_{(-60,20)}}{N_{gen}}$$
(7.6)

where: A- the average acceptance given by formula (7.5),

 N_{qen} - the number of generated events,

 $N_{(-60,20)}$ - the number of generated events for Q \in (-60,20) MeV.

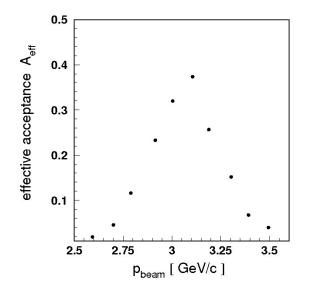


Figure 7.7: Effective acceptance for the registration of the quasi-free $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ reaction near the η production threshold (Q \in (-60,20) MeV) as a function of beam momentum.

The effective acceptance A_{eff} was calculated for ten values of the beam momentum. The dependence $A_{eff}(p_{beam})$ is presented in Fig. 7.7.

In the simulations of the $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ reaction it is assumed that the square of invariant mass of T- η nuclei is given by Breit-Wigner distribution. In this case an effective acceptance for the registration of the bound state decay products is calculated by formula:

$$A_{eff}^{BW} = A \frac{N_{(-60,20)}^{BW}}{N_{gen}^{BW}}$$
(7.7)

where: A- the average acceptance given by formula (7.5),

 N_{gen}^{BW} - the number of generated events accepted with probability calculated according to the Breit-Wigner distribution of $\sqrt{s_{nd}}$,

 $N^{BW}_{(-60,20)}$ - the number of generated events for Q \in (-60,20) MeV accepted with probability calculated according to the Breit-Wigner distribution of $\sqrt{s_{nd}}$

and is presented in Fig. 7.8 as a function of the beam deuteron momentum.

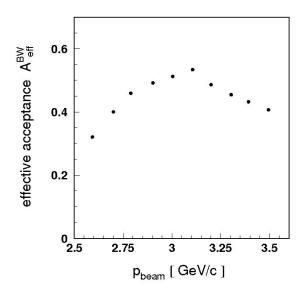


Figure 7.8: Effective acceptance for the registration of the quasi free $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ reaction near the η production threshold (Q \in (-60,20) MeV) as a function of beam momentum assuming a Breit-Wigner distribution of $\sqrt{s_{nd}}$ for the bound state width $\Gamma=10$ MeV.

From the dependence shown in above figure it results that the highest probability for the registration of considered quasi-free $dd \rightarrow p_{sp}(p_F = 0)(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^$ reaction is for the beam momentum $p_{beam}=3.1$ GeV/c corresponding to the $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ reaction threshold whereas for the beam momentum above and below the threshold the effective acceptance decreases. Above considerations were carried out for the Paris model of nucleon Fermi momentum distribution inside deuteron, $\Gamma_1=10$ MeV bound state width and analitic formula describing nucleon Fermi momentum distribution inside T. The calculations are consistent with the one for CD-Bonn model of nucleon momentum distribution inside deuteron with an accurancy better than 4% and are independent of models of nucleon Fermi momentum distribution inside tritium.

8 Summary and conclusions

The main aim of this thesis was to test the feasibility of the measurement of η -helium mesic nucleus production via reactions:

 $dd \to ({}^{4}\text{He-}\eta)_{bs} \to {}^{3}\text{He}p\pi^{-}$ $dd \to ({}^{4}\text{He-}\eta)_{bs} \to dpp\pi^{-}$ $pd \to ({}^{3}\text{He-}\eta)_{bs} \to dp\pi^{0} \to dp\gamma\gamma$ $pd \to ({}^{3}\text{He-}\eta)_{bs} \to ppp\pi^{-},$

with WASA-at-COSY detector and test the feasibility of the η -T bound state production via reaction:

$$nd \to (T-\eta)_{bs} \to dp\pi^-$$

realised through $dd \to p_{sp}(T-\eta)_{bs} \to p_{sp}dp\pi^-$ quasi-free reaction with COSY-TOF detection setup.

The reaction kinematics for free and quasi-free η -mesic bound states production as well as the spectator model assumptions were analysed and discussed. Moreover, the nucleon momentum distribution inside ⁴He, ³He, T and d, was presented for different models based on the analytic formulas and theoretical analysis for each of nuclei. Numerical data for those distributions are presented in Appendix A. The simulation were carried out and acceptances of WASA-at-COSY detection systems for free processes were calculated and compared for three assumed values of bound states width as well as for three different models of nucleon Fermi momentum distribution. In case of quasifree reaction the effective COSY-TOF acceptance as a function of beam momentum was determined.

The simulation results show that the acceptance as function of excess energy for the free reactions of η -helium production is in good approximation constant near the η production threshold and is independent of the bound state width value and model of Fermi momentum distribution. The calculations present that the absolute value of acceptance depends on the reaction channel. The most probable is registering of particles outgoing from the $pd \rightarrow ({}^{3}\text{He}-\eta)_{bs} \rightarrow dp\pi^{0} \rightarrow dp\gamma\gamma$ reaction. The average value of WASA geometrical acceptance is then equal to A=0.61.

For the quasi-free reaction $dd \to p_{sp}(T-\eta)_{bs} \to p_{sp}dp\pi^-$ of η -tritium formation the COSY-TOF effective acceptance is dependent on the beam momentum value. It reaches the highest value for the beam momentum of $p_{beam}=3.1 \text{ GeV/c}$ corresponding to the $dd \to p_{sp}(p_F=0)nd \to p_{sp}(p_F=0)T-\eta$ reaction threshold. Thus the measurement of quasi-free reaction products is the most efficient at the η production threshold.

In this thesis the geometrical acceptance for particular reactions was calculated. In the future, the efficiency of registration for the outgoing particles in each of reaction will be determined. Finally the experiments in which η -nuclei will be searched are interesting because of following issues:

- 1. Potential of discovering of η -mesic bound states. Observation of that state would allow to investigate interactions between the η meson and the nucleons inside a nuclear matter.
- 2. η -mesic bound systems would provide the information about $N^*(1535)$ [5] resonance and η meson properties in nuclear matter [6].
- 3. The existence of the bound states could give a possibility to study a flavour singlet component of the quark-gluon wave function of the η meson [8, 7].

The simulations presented in this thesis show that the η -helium nuclei measurement can be carried out at WASA-at-COSY detection setup, while the η -tritium bound states might be searched at COSY-TOF detector. As a result of simulation it is established that the most efficient measurement of $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ reaction at COSY-TOF detector can be done at the beam momentum of 3.1 GeV/c.

A Fermi momentum distributions-numerical data

In Chapter 3 Fermi momentum distributions of nucleons inside d, T, ³He and ⁴He nuclei were described and presented in Fig. 3.1, 3.2, 3.3. Numerical data for these distributions are given in the following tables:

p_F	$f(p_F)$	[c/MeV]		
[MeV/c]	Paris [30]	CDBonn [31]		
10	0.00218	0.00195		
20	0.00662	0.00581		
30	0.00997	0.00894		
40	0.01138	0.01028		
50	0.01126	0.00999		
60	0.01017	0.00975		
70	0.00881	0.00803		
80	0.00742	0.00685		
90	0.00624	0.00582		
100	0.00523	0.00483		
110	0.00427	0.00407		
120	0.00357	0.00336		
130	0.00301	0.00284		
140	0.00241	0.00236		
150	0.00194	0.00199		
160	0.00162	0.00167		
170	0.00138	0.00142		
180	0.00116	0.00119		
190	0.00096	0.00102		
200	0.00080	0.00087		
210	0.00071	0.00077		
220	0.00064	0.00067		
230	0.00054	0.00057		
240	0.00046	0.00048		
250	0.00044	0.00043		
260	0.00037	0.00038		
270	0.00032	0.00032		
280	0.00029	0.00028		
290	0.00027	0.00025		
300	0.00024	0.00023		
310	0.00021	0.00020		
320	0.00019	0.00018		
330	0.00016	0.00016		
340	0.00014	0.00015		
350	0.00013	0.00013		
360	0.00012	0.00012		
370	0.00010	0.00011		
380	0.00010	0.00010		
390	0.00008	0.00009		
400	0.00008	0.00008		

Table A.1: Fermi momentum distribution of nucleon inside deuteron according to Paris model and CDBonn model (Chapter 3). The distributions were normalized to unity in the momentum range from 0 to 400 MeV/c.

p_F			
[Gev/c]	anal. formula [33]	$\frac{f(p_F) \text{ [c/GeV]}}{\text{AV18+UrbIX [35, 36]}}$	CDB2000+TM [35, 36]
0.01	0.4788	0.4896	0.4877
0.02	1.7861	1.7752	1.7681
0.03	3.5812	3.4555	3.4418
0.04	5.4299	5.1298	5.1083
0.05	6.9442	6.4313	6.4083
0.06	7.8847	7.2795	7.2566
0.07	8.1972	7.6620	7.4559
0.08	7.9806	7.6485	7.6352
0.09	7.4157	7.3449	7.3401
0.10	6.6911	6.8532	6.8579
0.11	5.9512	6.2508	6.2654
0.12	5.2771	5.5925	5.6167
0.13	4.6944	4.9449	4.9778
0.14	4.1926	4.3187	4.3593
0.15	3.7476	3.7398	3.7862
0.16	3.3361	3.2234	3.2754
0.17	2.9434	2.7373	2.7934
0.18	2.5639	2.3459	2.4038
0.19	2.1996	1.9769	2.0363
0.20	1.8557	1.6787	1.7378
0.21	1.5384	1.4070	1.4653
0.22	1.2531	1.1897	1.2459
0.23	1.0029	0.9913	1.0451
0.24	0.7887	0.8398	0.8901
0.25	0.6096	0.6943	0.7410
0.26	0.4633	0.5935	0.6358
0.27	0.3462	0.4927	0.5306
0.28	0.2545	0.4219	0.4550
0.29	0.1840	0.3579	0.3860
0.30	0.1309	0.3036	0.3269
0.31	0.0916	0.2650	0.2833
0.32	0.0631	0.2264	0.2398
0.33	0.0428	0.2014	0.2101
0.34	0.0286	0.1794	0.1834
$0.35 \\ 0.36$	0.0188	0.1587 0.1460	$0.1581 \\ 0.1422$
	0.0121	0.1469	-
0.37 0.38	0.0078 0.0049	$0.1350 \\ 0.1249$	$0.1262 \\ 0.1123$
0.38	0.0049	0.1249 0.1188	0.1123 0.1028
0.39	0.0030	0.1188 0.1127	0.1028
0.40	0.0010	0.1127	0.0955

Table A.2: Fermi momentum distribution of proton inside ³He according to three different models: analytic formula (equation 3.1) (left), AV18 NN model+UrbanaIX three nucleon interaction (middle) and CDB2000 NN model+Tucson-Melbourne three nucleon interaction (right). The distributions were normalized to unity in the momentum range from 0 to 0.4 GeV/c.

		$f(m)$ $\left[\alpha/C \alpha V \right]$	
p_F [Gev/c]	anal. formula [33]	$\frac{f(p_F) \text{ [c/GeV]}}{\text{AV18+UrbIX [35, 36]}}$	CDB2000+TM [35, 36]
0.01	0.4788	0.5316	0.4392
0.01	1.7861	1.9188	1.6039
0.02	3.5812	3.7094	3.1551
0.03	5.4299	5.4606	4.7375
0.04	6.9442	6.7807	6.0219
0.05	7.8847	7.5975	6.9043
0.00	8.1972	7.973 7.9148	7.3554
0.07	7.9806	7.8206	7.334 7.4244
0.08	7.9800 7.4157	7.4358	7.2021
0.10	6.6911	6.8712	6.7825
0.10	5.9512	6.2074	6.2400
0.11	5.3312 5.2771	5.5055	5.6248
0.12	4.6944	4.8276	5.0248 5.0082
0.13	4.1926	4.1805	4.4049
0.14	3.7476	3.5912	3.8388
0.16	3.3361	3.0738	3.3299
0.10	2.9434	2.5893	2.8478
0.11	2.5639	2.2059	2.4546
0.10	2.1996	1.8456	2.0831
0.10	1.8557	1.5583	1.7797
0.20	1.5384	1.2975	1.5023
0.21	1.2531	1.0913	1.2781
0.23	1.0029	0.9036	1.1073
0.24	0.7886	0.7620	0.9136
0.25	0.6096	0.6261	0.7606
0.26	0.4633	0.5332	0.6523
0.27	0.3462	0.4403	0.5440
0.28	0.2545	0.3758	0.4662
0.29	0.1840	0.3176	0.3951
0.30	0.1309	0.2684	0.3341
0.31	0.0916	0.2338	0.2892
0.32	0.0631	0.1991	0.2443
0.33	0.0428	0.1769	0.2137
0.34	0.0286	0.1574	0.1862
0.35	0.0188	0.1391	0.1601
0.36	0.0122	0.1287	0.1438
0.37	0.0078	0.1183	0.1274
0.38	0.0049	0.1095	0.1131
0.39	0.0030	0.1042	0.1034
0.40	0.0018	0.0989	0.0937

Table A.3: Fermi momentum distribution of neutron inside T according to three different models: analytic formula (equation 3.1) (left), AV18 NN model+UrbanaIX three nucleon interaction (middle) and CDB2000 NN model+Tucson-Melbourne three nucleon interaction (right). The distributions were normalized to unity in the momentum range from 0 to 0.4 GeV/c.

B Acceptance-supplement

The following tables show all possible combinations of particle registration for each of considered reactions. Abbreviations 'FD', 'CD-MDC' and 'CD-EC' denote Forward Detector, Mini Drift Chamber and Electromagnetic Calorimeter of WASA-at-COSY detector, respectively.

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0.46 0.0607 0.2260 0.1439 0.47 0.0458 0.2224 0.1368	-						
0.47 0.0458 0.2224 0.1368							
0.49 0.0254 0.2153 0.1226							
0.50 0.0187 0.2133 0.1177							

Table A.4: Fermi momentum distribution of neutron inside ⁴He according to three different models: analytic formula (equation 3.2) (left), AV18 NN model+UrbanaIX three nucleon interaction (middle) and CDB2000 NN model+Tucson-Melbourne three nucleon interaction (right). The distributions were normalized to unity in the momentum range from 0 to 0.5 GeV/c.

particle	case 1	case 2	case 3	case 4
³ He	FD	FD	FD	FD
proton	FD	CD-MDC	FD	CD-MDC
π^{-}	FD	CD-MDC	CD-MDC	FD

Table B.1: Possibilities of particles registration in the $dd \rightarrow ({}^{4}\text{He}-\eta)_{bs} \rightarrow {}^{3}\text{He}p\pi^{-}$ reaction.

	pa	article	case	e 1	case 2	2	case :	3	case 4	1	case 5	5
	de	uteron	Fl)	CD-MI	DC	FD		FD		FD	
	pr	oton1	FI) C	CD-MI	DC	CD-MI	DC	CD-MI	DC	CD-MI	DC
	pr	oton2	Fl) c	CD-MI	DC	CD-MI	DC	FD		CD-MI	DC
		π^{-}	FI) c	CD-MI	DC	CD-MI	DC	FD		FD	
						I				1		
	cas	e 6	cas	e 7	cas	e 8	cas	e 9	case	e 10	case	e 11
	F	D	F	D	F	D	F	D	CD-N	MDC	CD-N	ADC
(CD-I	MDC	F	D	F	D	F	D	CD-N	MDC	F	D
	\mathbf{F}	D	CD-1	MDC	F	D	CD-N	MDC	CD-N	MDC	CD-N	ADC
	CD-I	MDC	CD-1	MDC	CD-N	MDC	F	D	F	D	CD-N	ADC
		case	12	cas	e 13	cas	se 14	ca	se 15	cas	se 16	
		CD-N	ADC	CD-	MDC	CD-	MDC	CD	-MDC	CD	-MDC	

case 12	case 15	case 14	case 15	case 10
CD-MDC	CD-MDC	CD-MDC	CD-MDC	CD-MDC
CD-MDC	FD	FD	FD	CD-MDC
FD	FD	CD-MDC	FD	FD
CD-MDC	CD-MDC	$^{\mathrm{FD}}$	FD	FD

Table B.2: Possibilities of particles registration in the $dd \rightarrow ({}^{4}\text{He-}\eta)_{bs} \rightarrow dpp\pi^{-}$ reaction.

particle	case 1	case 2
deuteron	FD	FD
proton	CD-MDC	FD
gamma1	CD-EC	CD-EC
gamma2	CD-EC	CD-EC

Table B.3: Possibilities of particles registration in the $pd \rightarrow ({}^{3}\text{He}-\eta)_{bs} \rightarrow dp\gamma\gamma$ reaction.

	particle case		1	case 2		case 3		case 4		case 5	
	proton1 FI		C	CD-MDC		FD		FD		FD	
	proton2	FD	C	D-MD	$C \mid 0$	CD-MDC		CD-MDC		CD-MD	C
	proton3	FD	C	D-MD	$C \mid 0$	CD-MD	\mathbf{C}	FD		CD-MD	C
	π^{-} FI		C	CD-MD		CD-MDC		FD		FD	
case 6		case 7		case 8		case 9		case 10		case 11	
FD		FD		FD		FD		CD-N	CD-MDC		ADC
CD-MDC		FD		FD		FD		CD-N	CD-MDC		D
FD		CD-MDC		FD		CD-MD0		C CD-MDC		C CD-MDC	
CD-MDC		CD-MDC		CD-MDC		C FD		FD		CD-ME	
	case	e 12	case 13		case 14		case 15		ca	se 16	
	CD-MDC		CD-I	CD-MDC		CD-MDC		CD-MDC		-MDC	
	CD-N	MDC	FD		FD			FD		-MDC	
	F	D	FD		CD-MDC			FD		FD	
	CD-N	MDC	CD-MDC		$_{\rm FD}$		FD]	FD	

Table B.4: Possibilities of particles registration in the $pd \to ({}^{3}\text{He-}\eta)_{bs} \to ppp\pi^{-}$ reaction.

particle	case 1						
proton _{sp}	START and STOP DETECTORS						
deuteron	START and STOP DETECTORS						
proton	START and STOP DETECTORS						
π^{-}	START and STOP DETECTORS						

Table B.5: Possibilities of particles registration in the $dd \rightarrow p_{sp}(T-\eta)_{bs} \rightarrow p_{sp}dp\pi^-$ reaction.